



Performance Prediction Models in MMOPP

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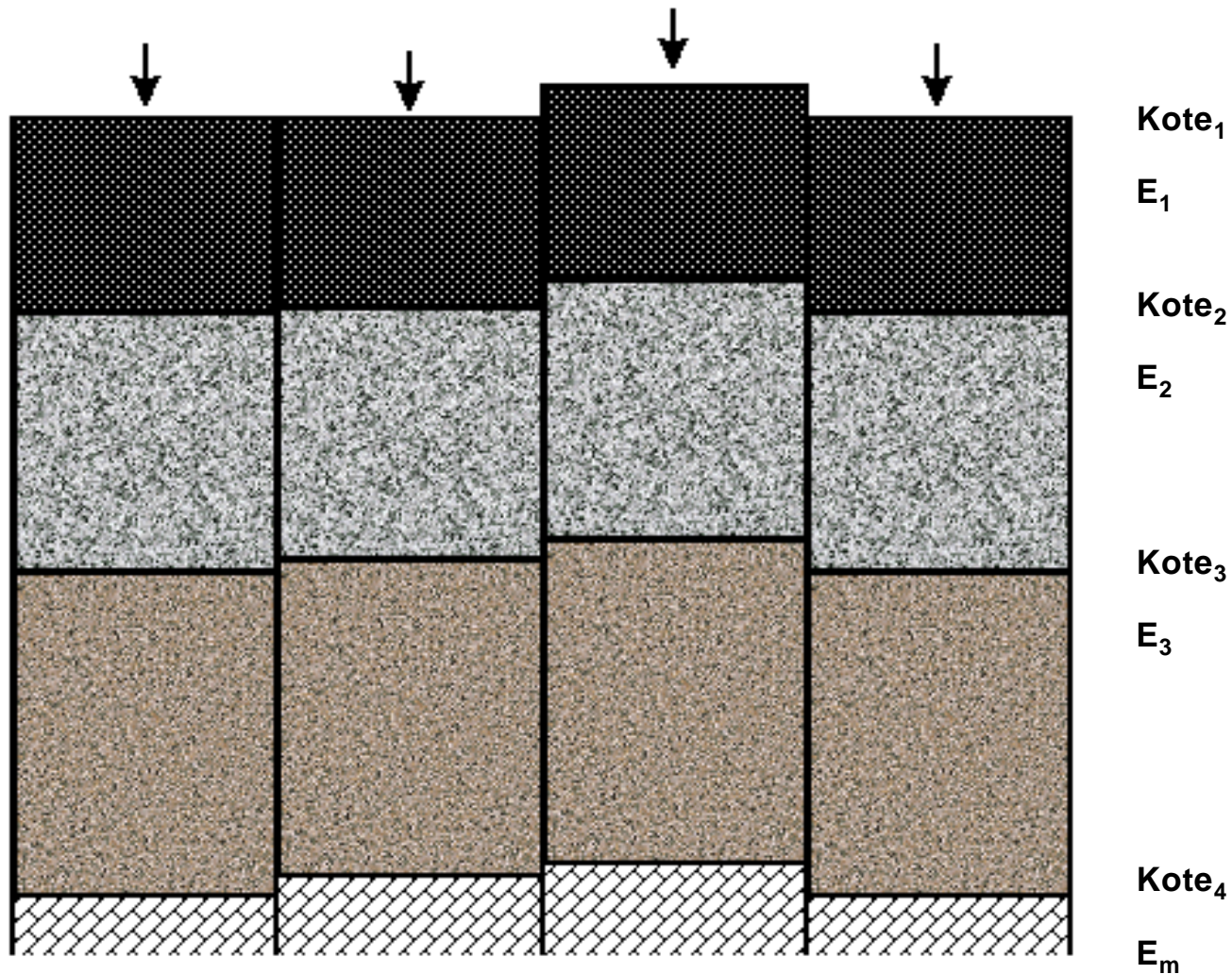
MMOPP

- Mathematical Modelling of Pavement Performance
- Design at three levels:
 - Pavement catalogue
 - Analytical-empirical method
 - Simulation and optimisation

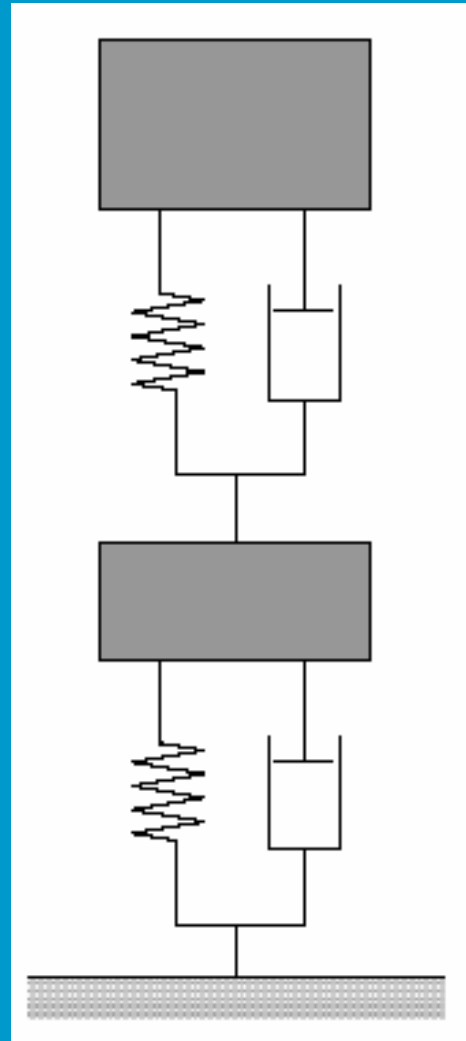
Design by simulation

- Models for:
 - Pavement: longitudinal profile, thicknesses, E-values
 - Load: reaction between wheel and pavement
 - Climate: temperature and E-value
 - Pavement response: stress, strain, deflection
 - Asphalt deterioration
 - Permanent deformation

Design by simulation



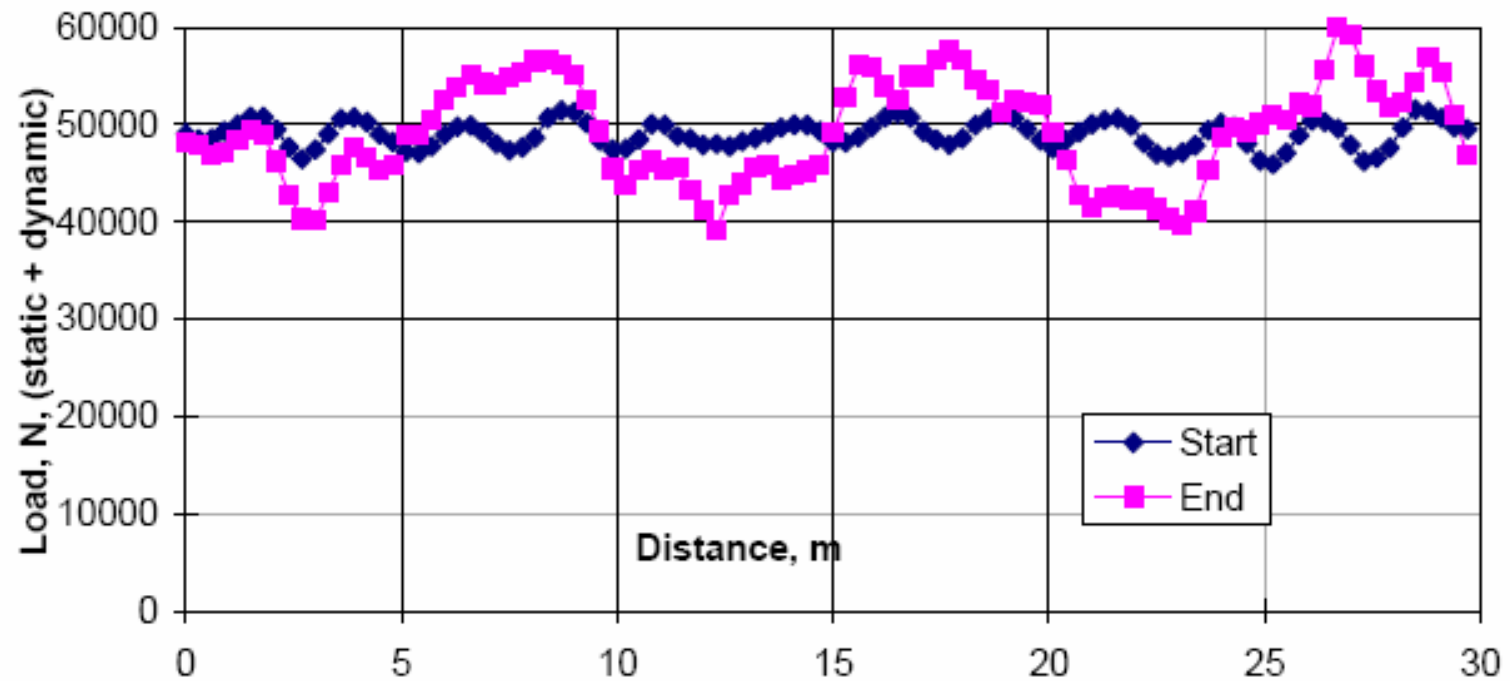
Load simulation



Suspension system

Axle and wheel

Variation of load



Climate model

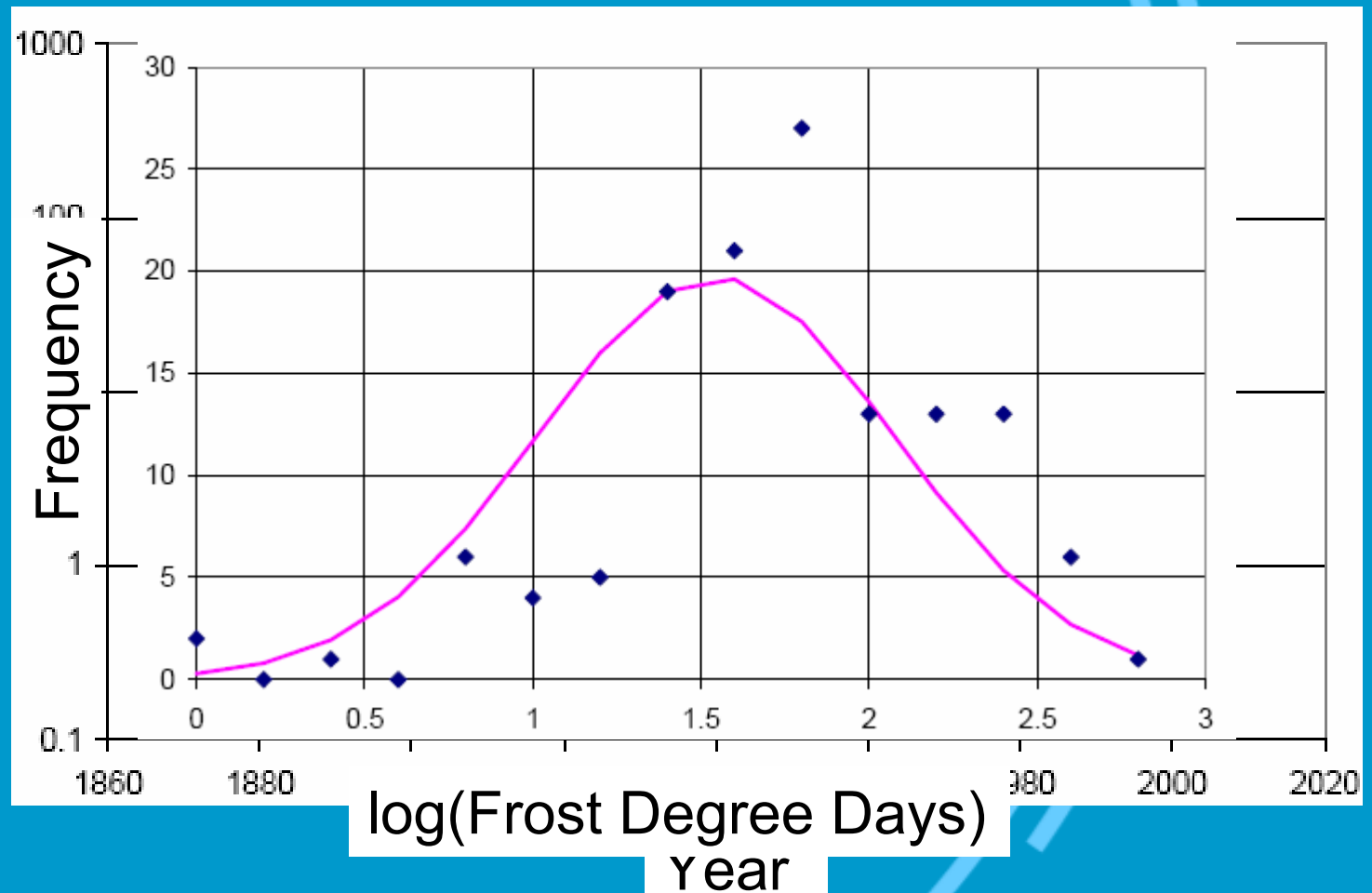
- Material E moduli in different climate seasons
- Depth of frost penetration

Climate seasons

Period	Days	Temperature	E_1	E_2	E_3	E_m
-	-	°C	factor	factor	factor	factor
Winter	49	-2	4	4.2	10	20
Winter thaw	10	1	3.7	0.33	10	20
Spring thaw	15	1	3.7	0.67	0.7	0.6
Late spring	46	4	3.1	1.0	0.85	0.8
Summer	143	20	1.0	1.0	1.0	1.0
Heat wave	10	50	0.3	1.0	1.0	1.0
Fall	92	7	2.6	1.0	1.0	1.0

Climate model

log(Frost Degree Days)



Response model

- Method of Equivalent Thicknesses
- 4-layer system



Structural deterioration (crackring)

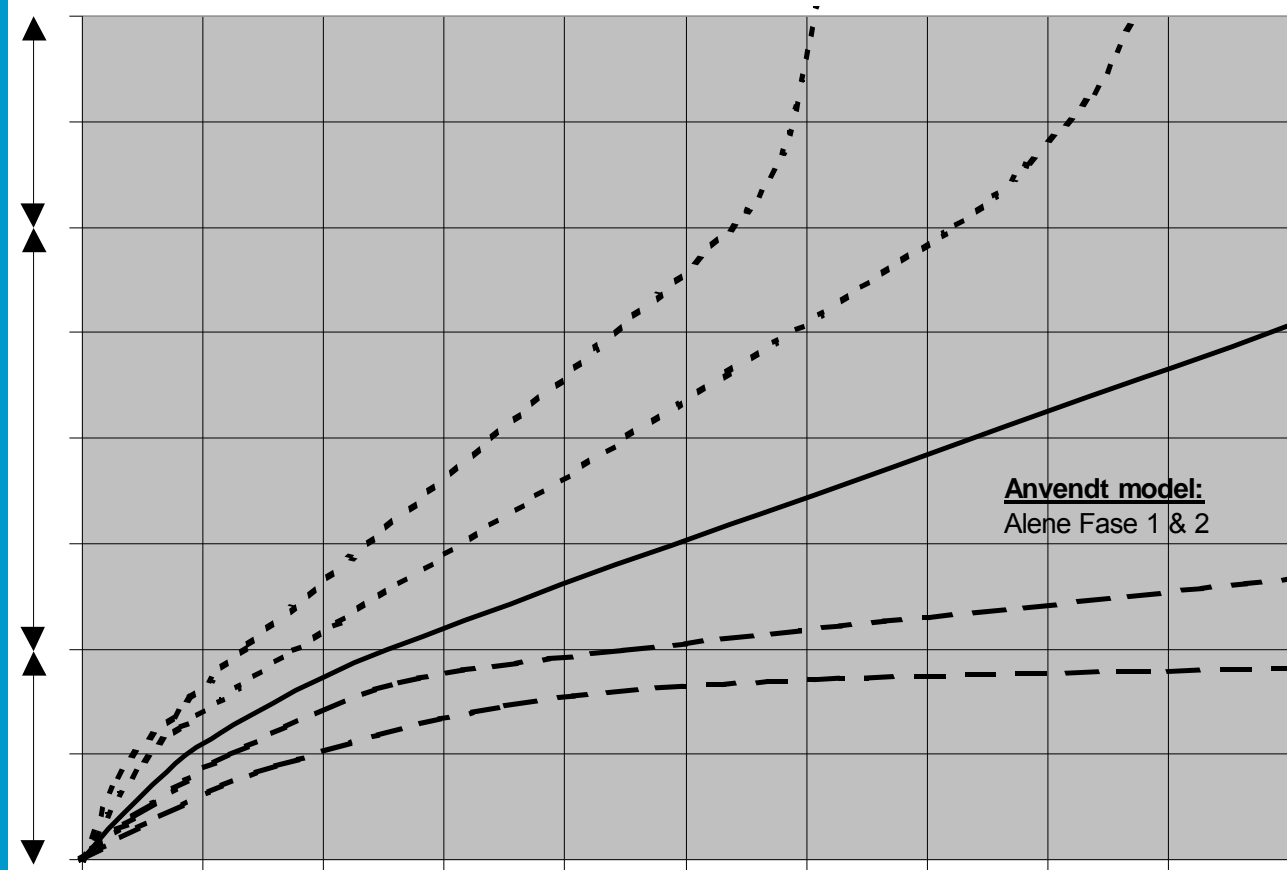
$$E_{after} = E_{before} \left(1 - 0,5 \left(\frac{\varepsilon_{calc}}{\varepsilon_{allowble,1million} (VB / 10\%)} \right)^n \frac{dN}{K_{temperature} CP_{factor}} \right)$$

Permanent deformation

Phase 3
Increasing
strain rate

Phase 2
Constant
strain rate

Phase 1
Decreasing
strain rate



Plastic strain models

Phase 1

(for $\varepsilon_p < \varepsilon_0$)

$$\varepsilon_p = AN^B \left(\frac{\sigma_1}{\sigma'} \right)^C$$

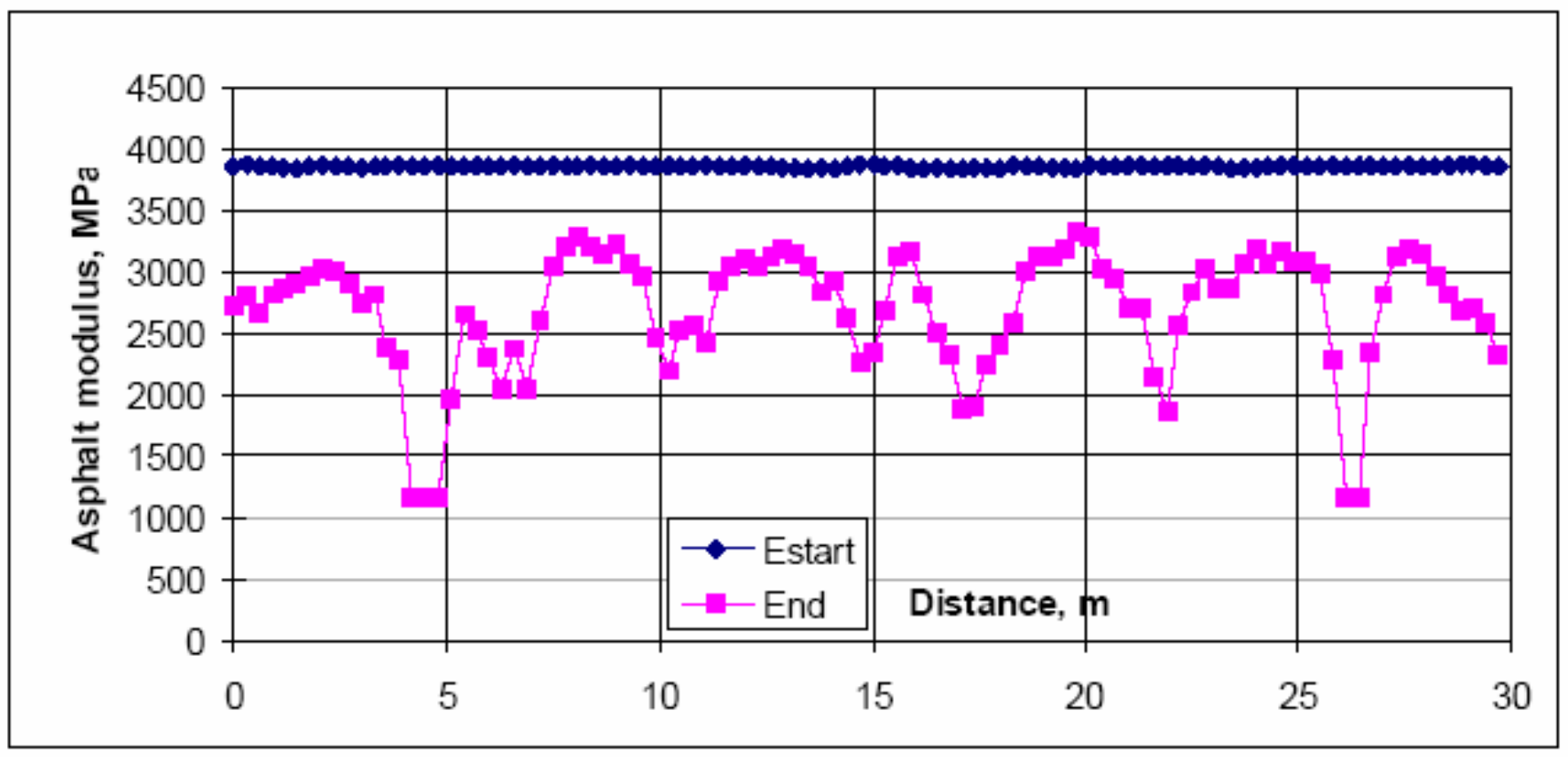
Phase 2

(for $\varepsilon_p > \varepsilon_0$)

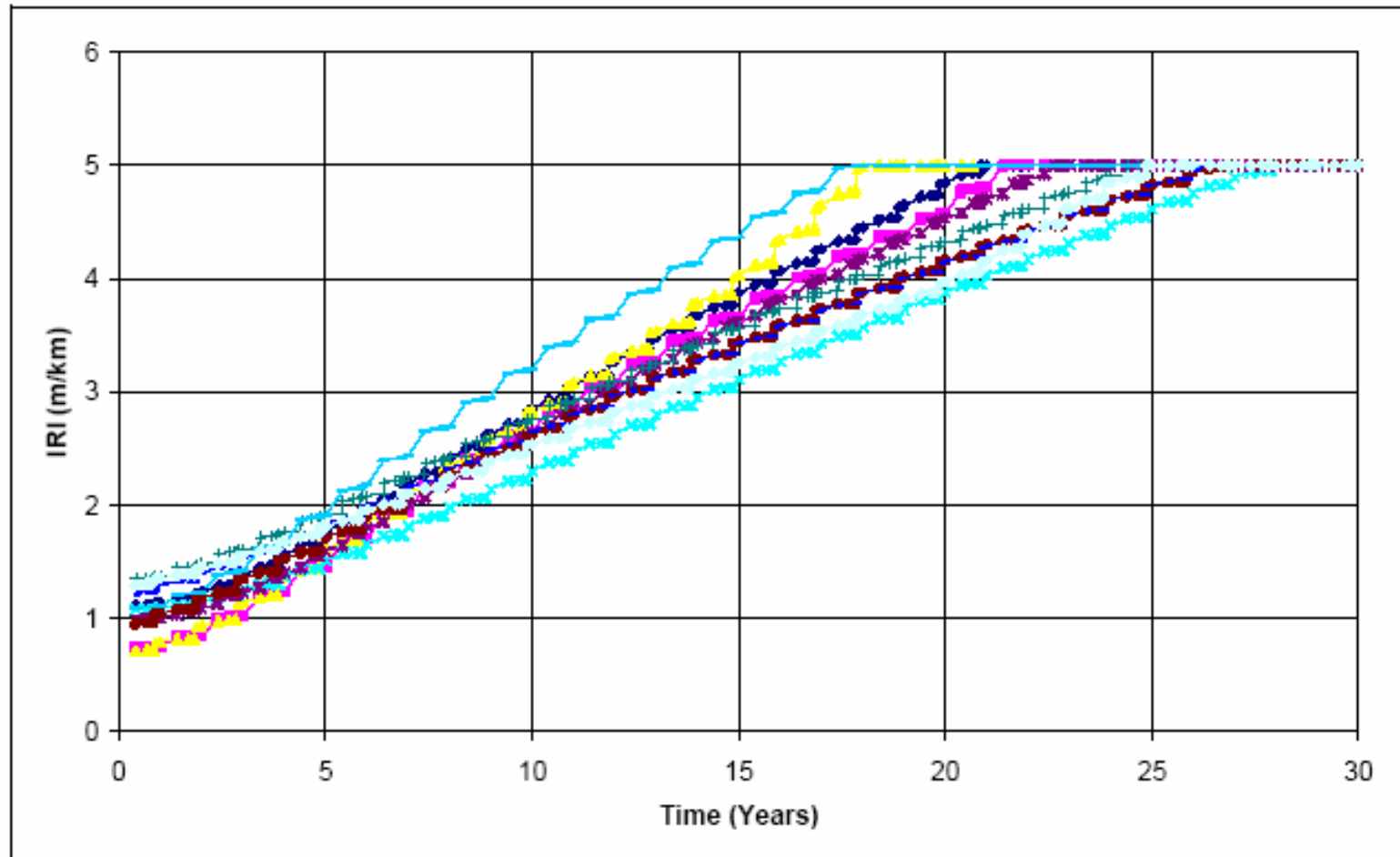
$$\varepsilon_p = \varepsilon_0 + (N - N_0) A^{\frac{1}{B}} B \varepsilon_0^{1 - \frac{1}{B}} \left(\frac{\sigma_1}{\sigma'} \right)^{\frac{C}{B}}$$

$$N_0 = \varepsilon_0^{\frac{1}{B}} A^{\frac{-1}{B}} \left(\frac{\sigma_1}{\sigma'} \right)^{\frac{-C}{B}}$$

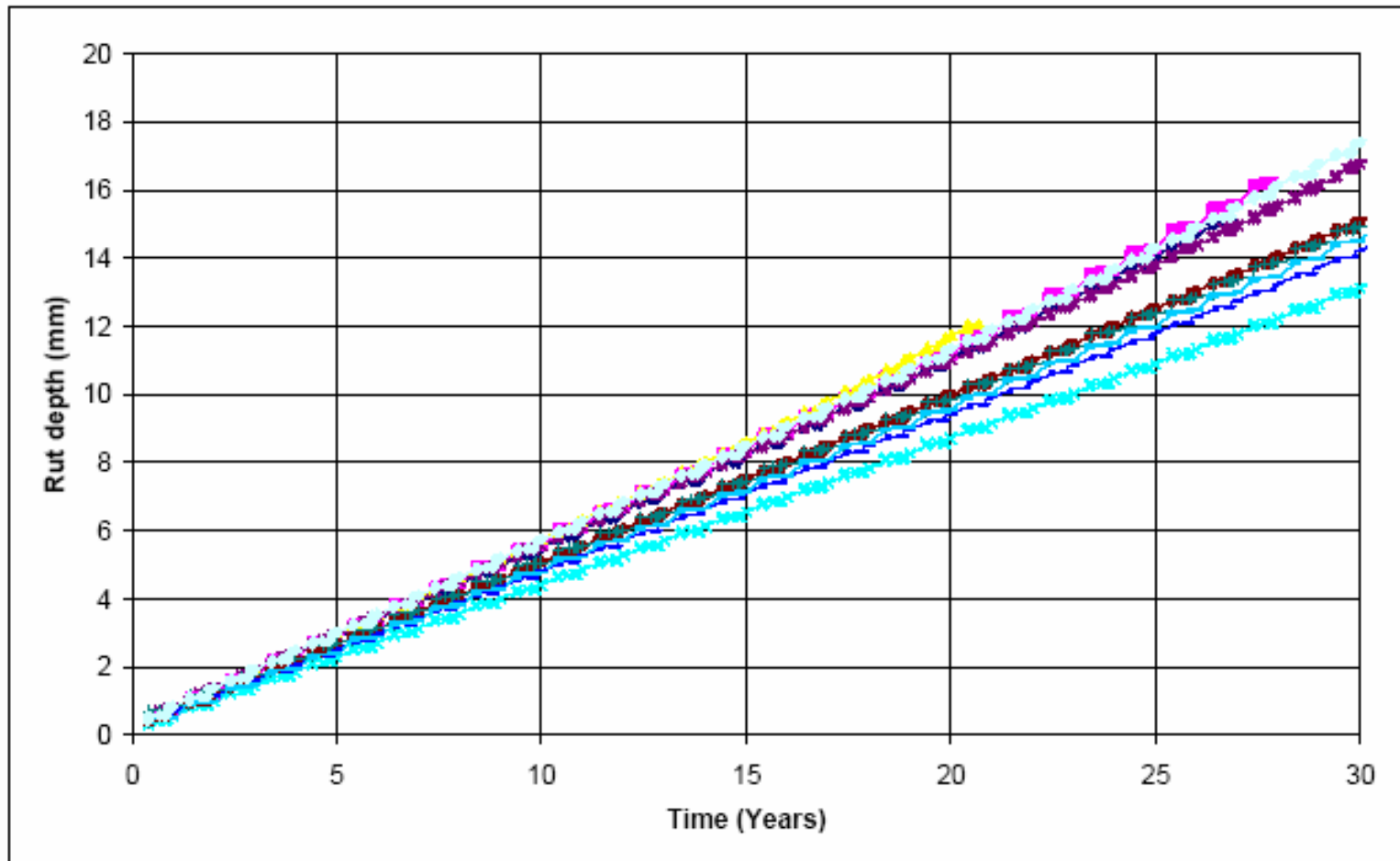
Asphalt modulus variation



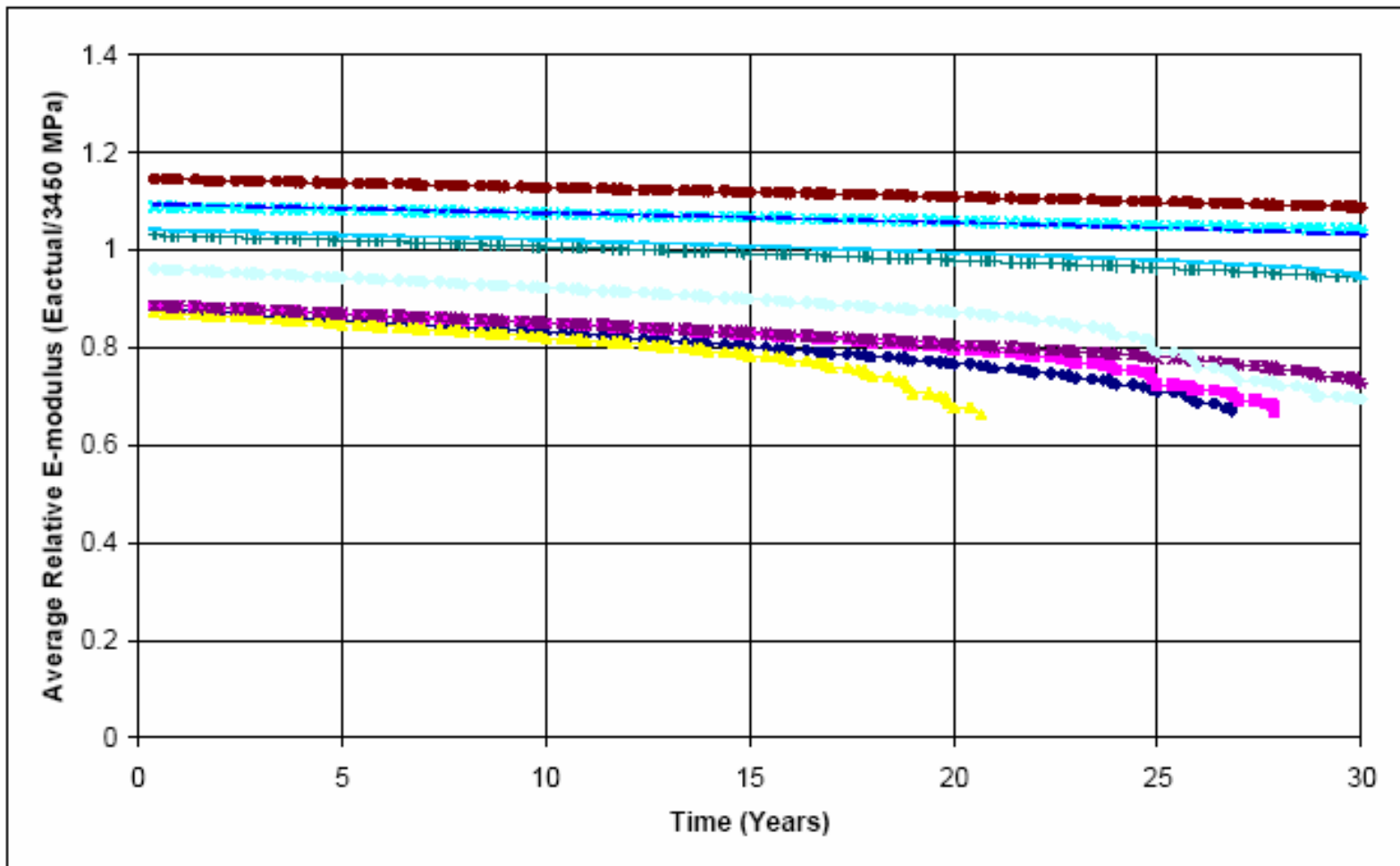
Roughness variation



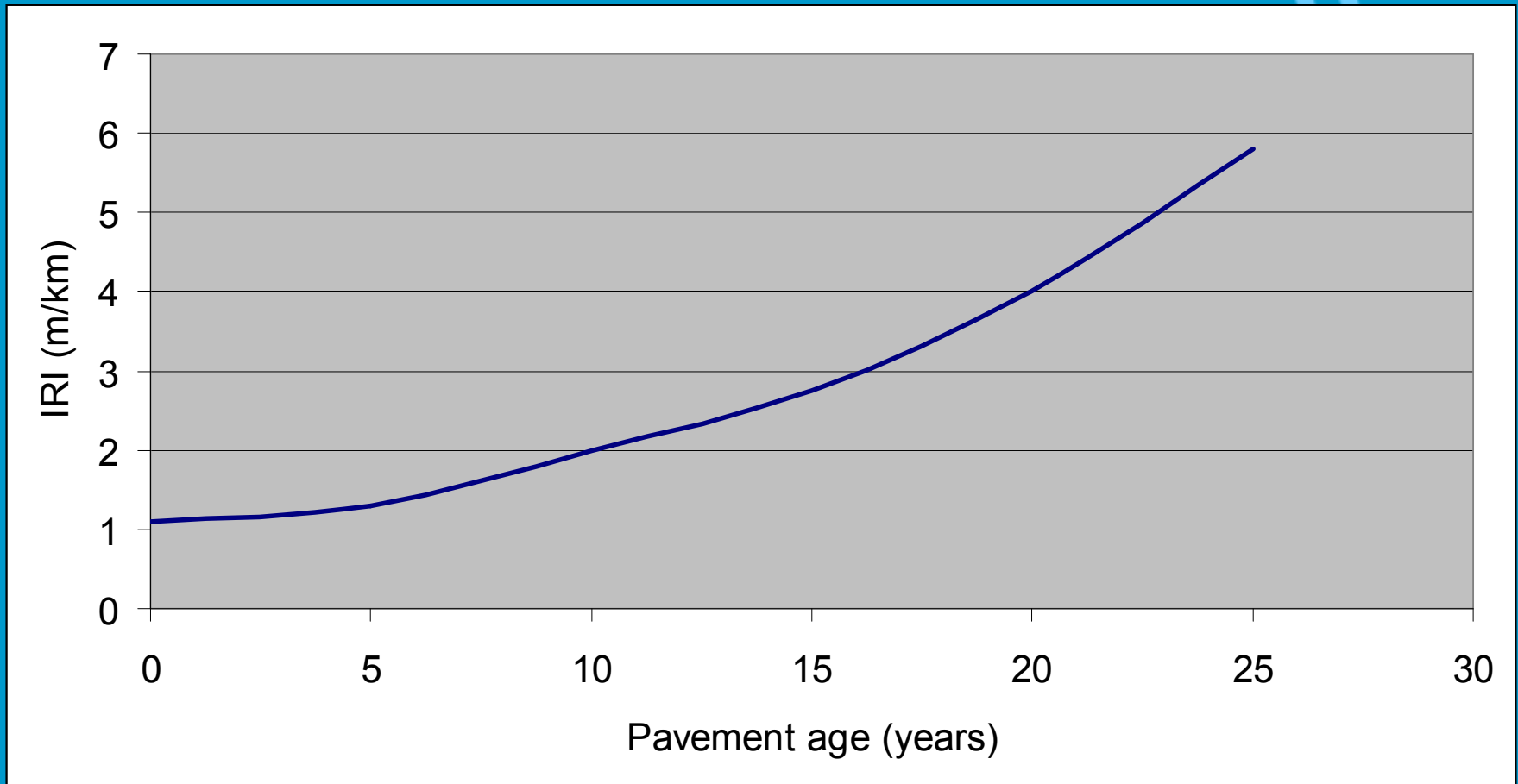
Rut depth development



Relative asphalt modulus



Roughness development - 1



Roughness development - 2

