

Pavement Design Systems and Pavement Performance models

Mechanistic Models for Road Design

NordFoU 2007-2009

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Administration (SRA)

Rutting and unevenness in roads have been a problem in many thousand years



And still, rutting and unevenness in roads are great problems today



If we could predict future rutting and unevenness, when a new road is ready, it would give a great help to minimize these problems!

Background

Road building

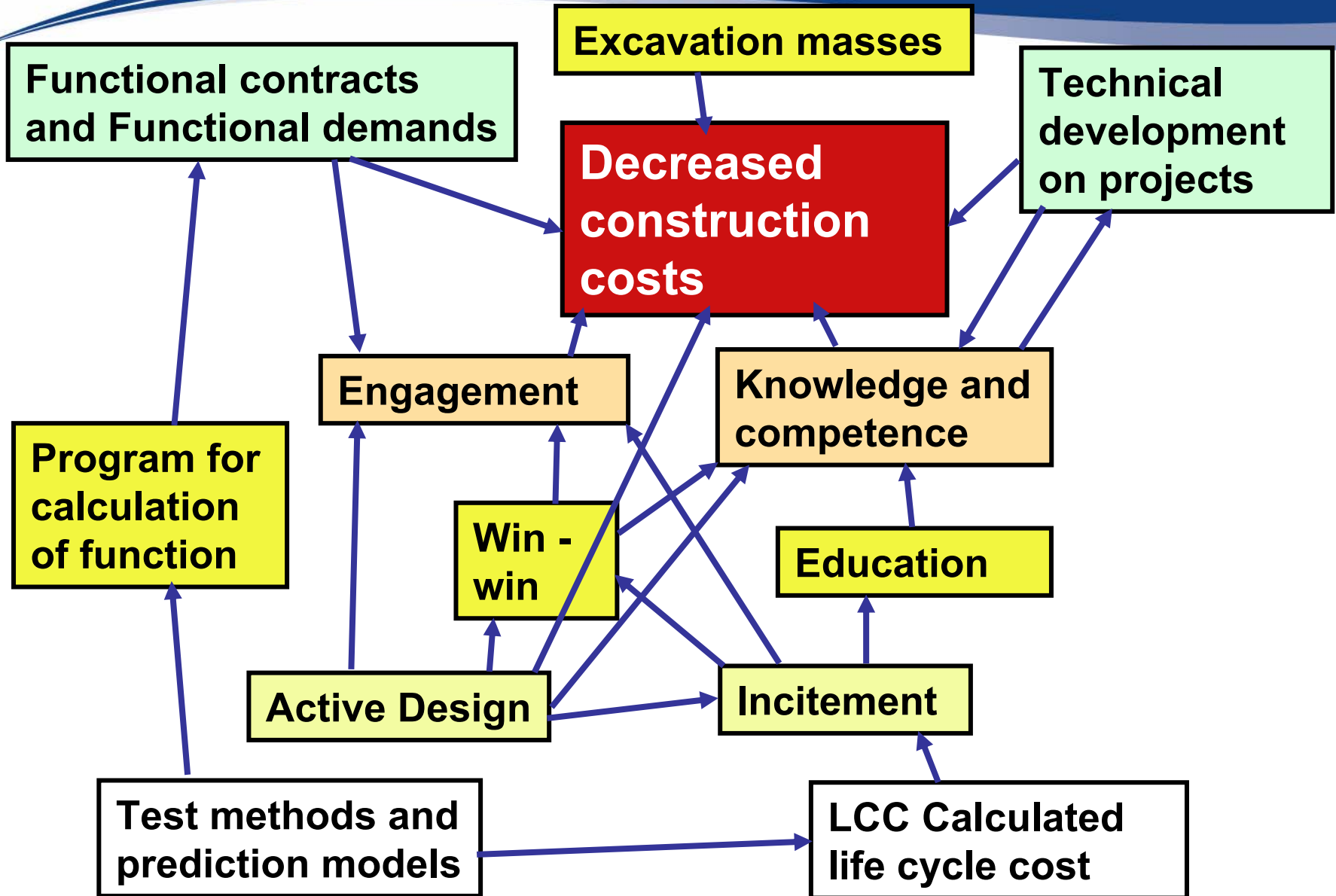
Investment cost	New technique 3 % per year or 15 % in 5 years	System costs 5%	Unnecessary costs 10 %	Error costs 10 %
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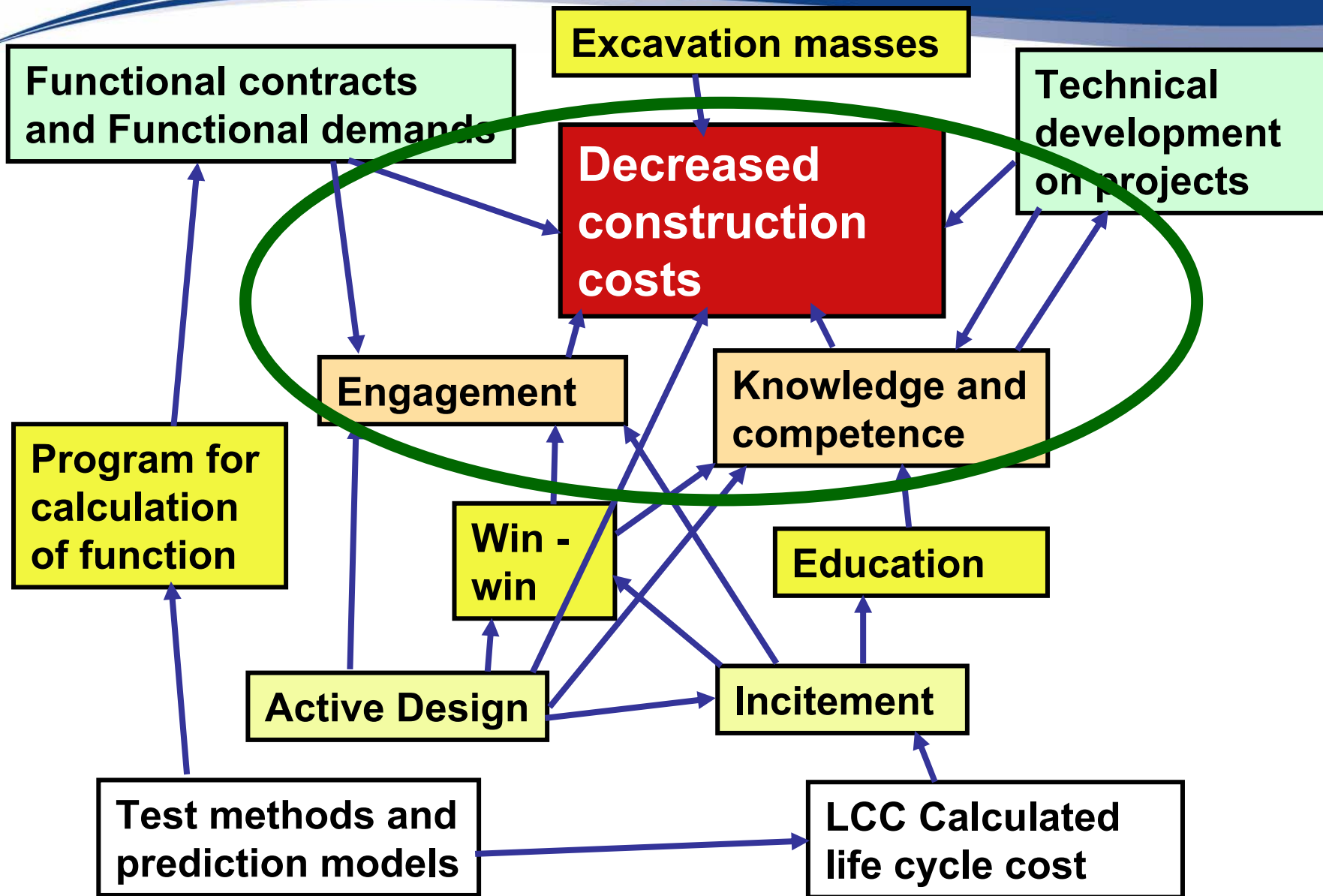
**saving POTENTIAL
(inside 5 years) 40 %!**

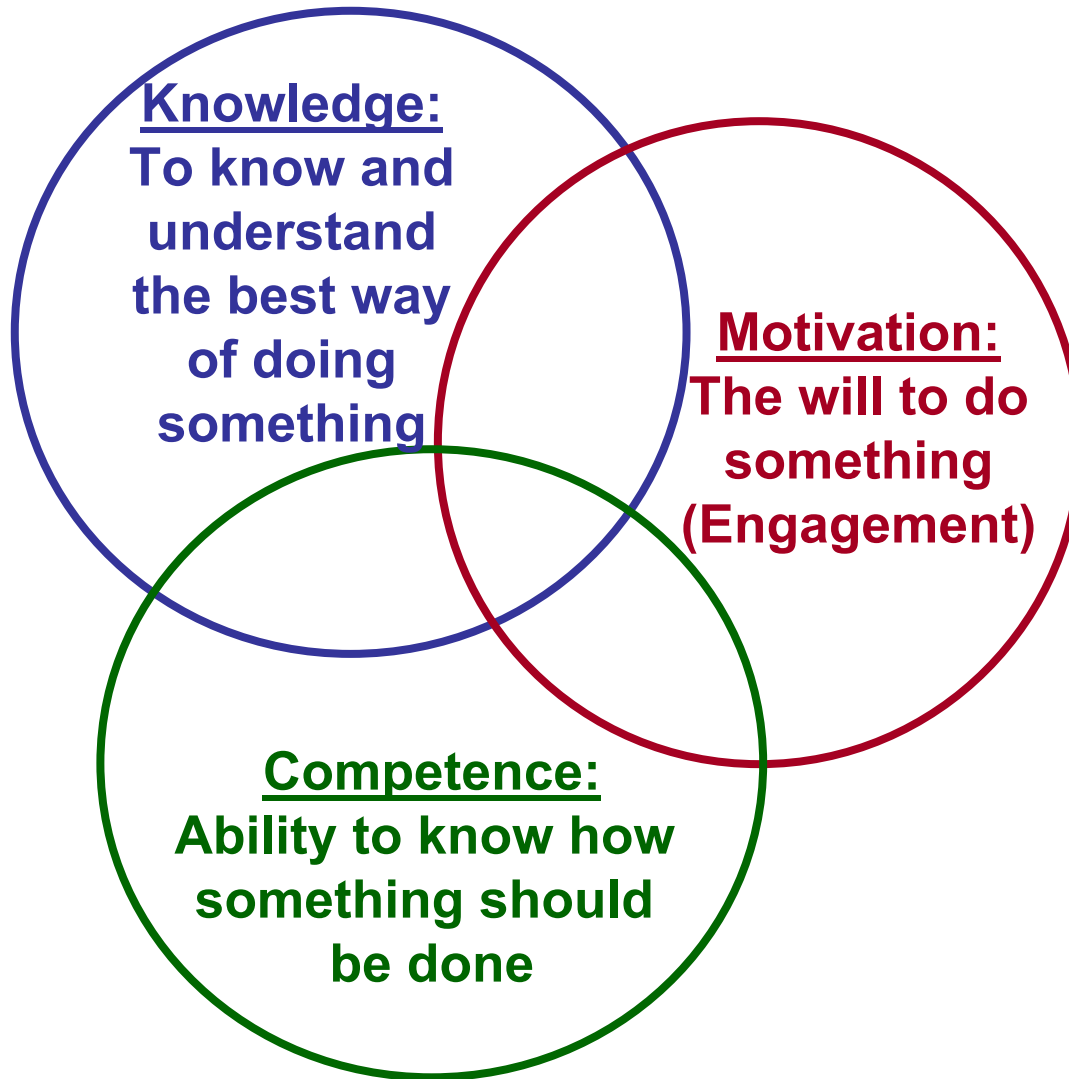
**Investigation
from Chalmers
University of
Technology**

A cartoon illustration of a helicopter with a CD-ROM for a rotor blade, flying over a globe. The helicopter is yellow with a blue rotor hub and a purple tail boom. The CD-ROM is silver with a purple center. The globe is light blue with a white equator. The background is white with a red banner at the top containing the text 'on of research results'.

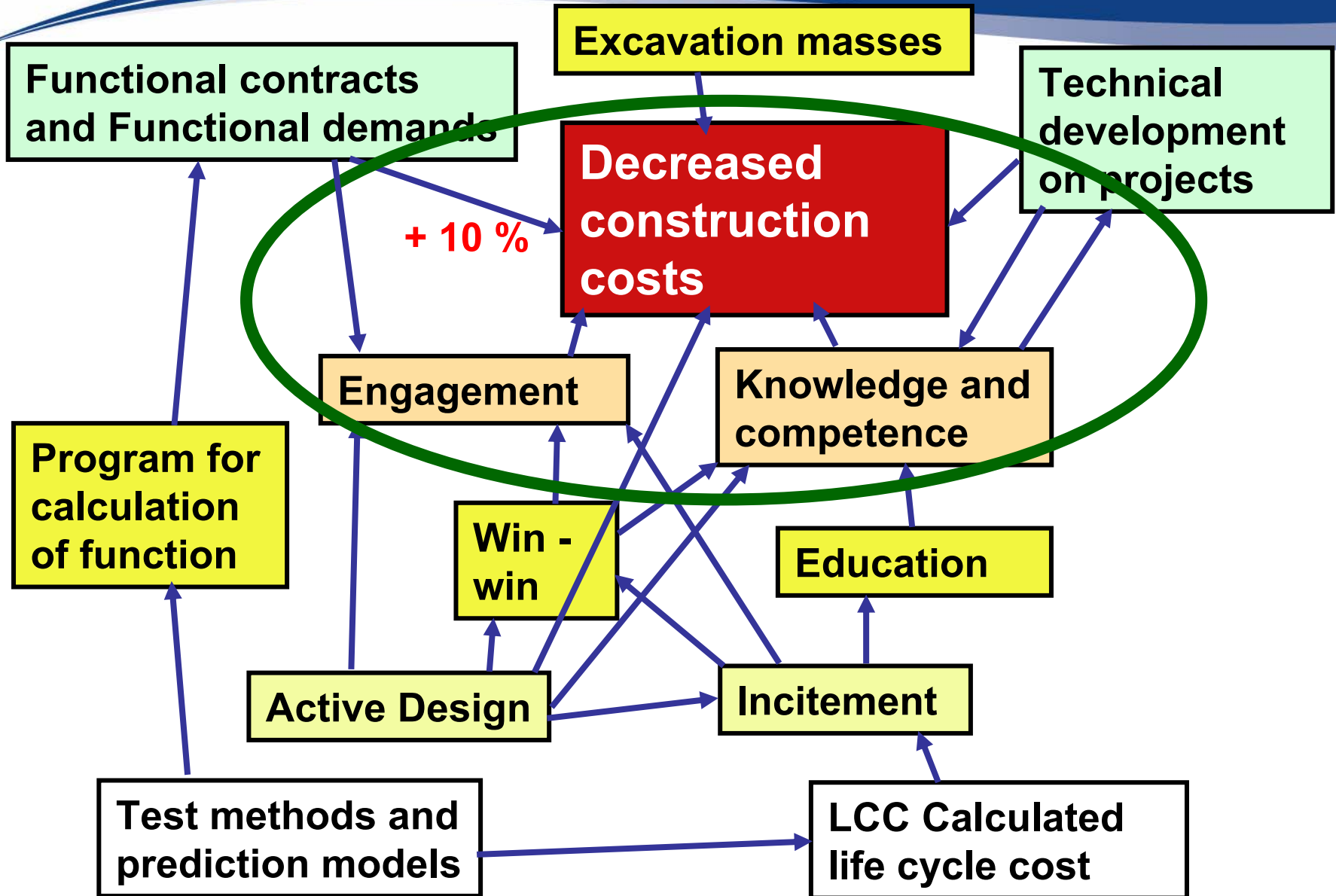


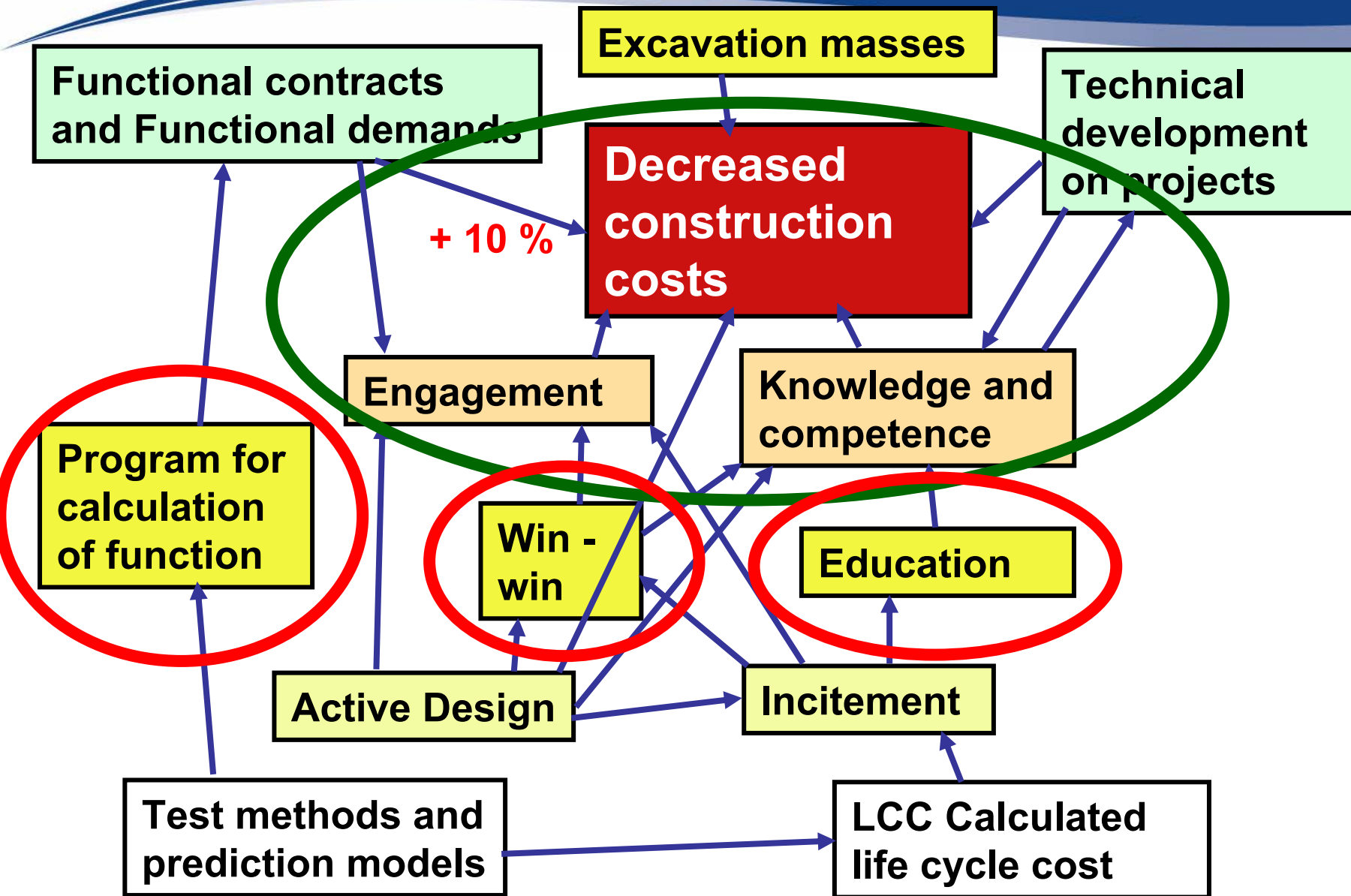


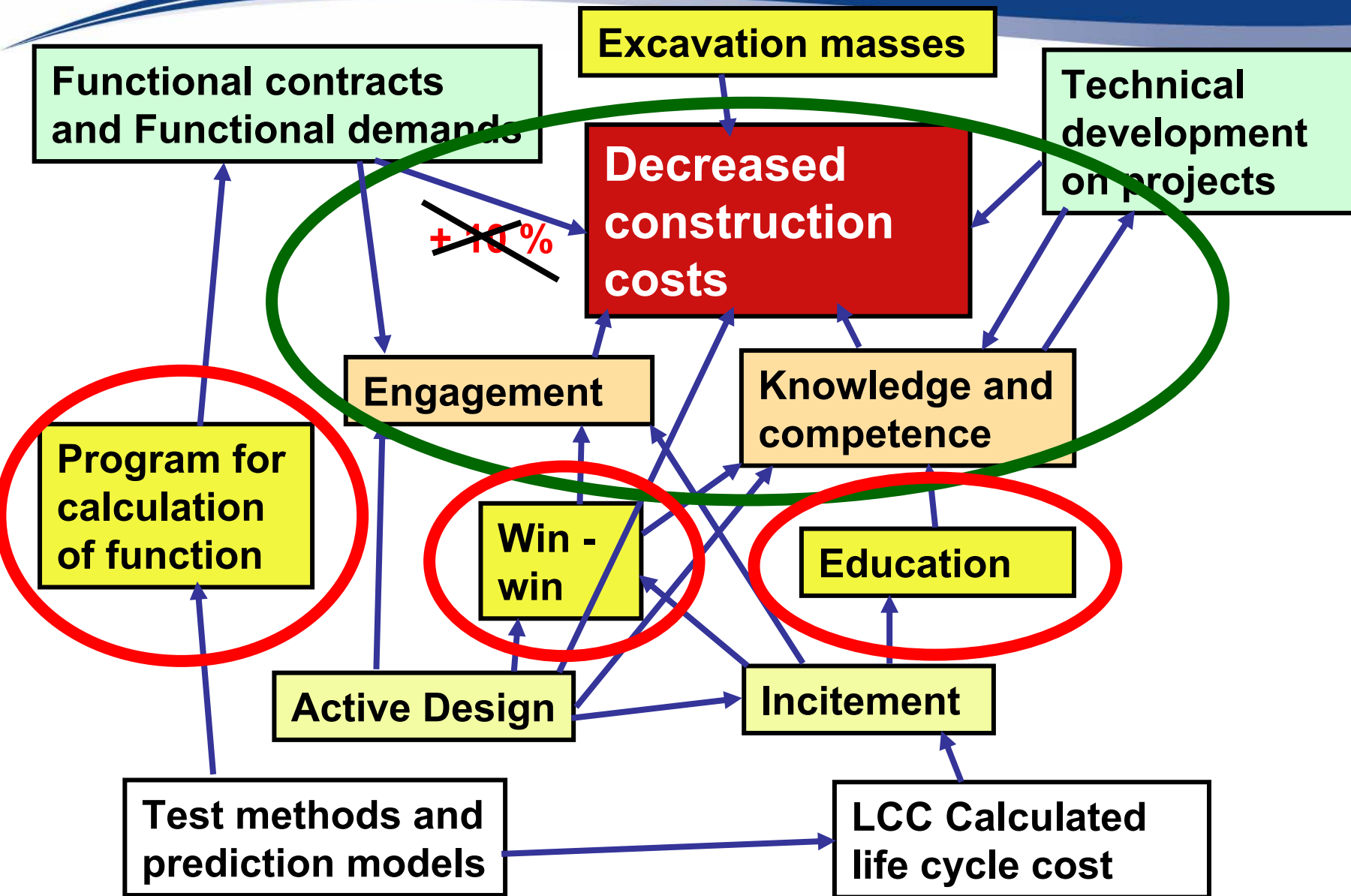


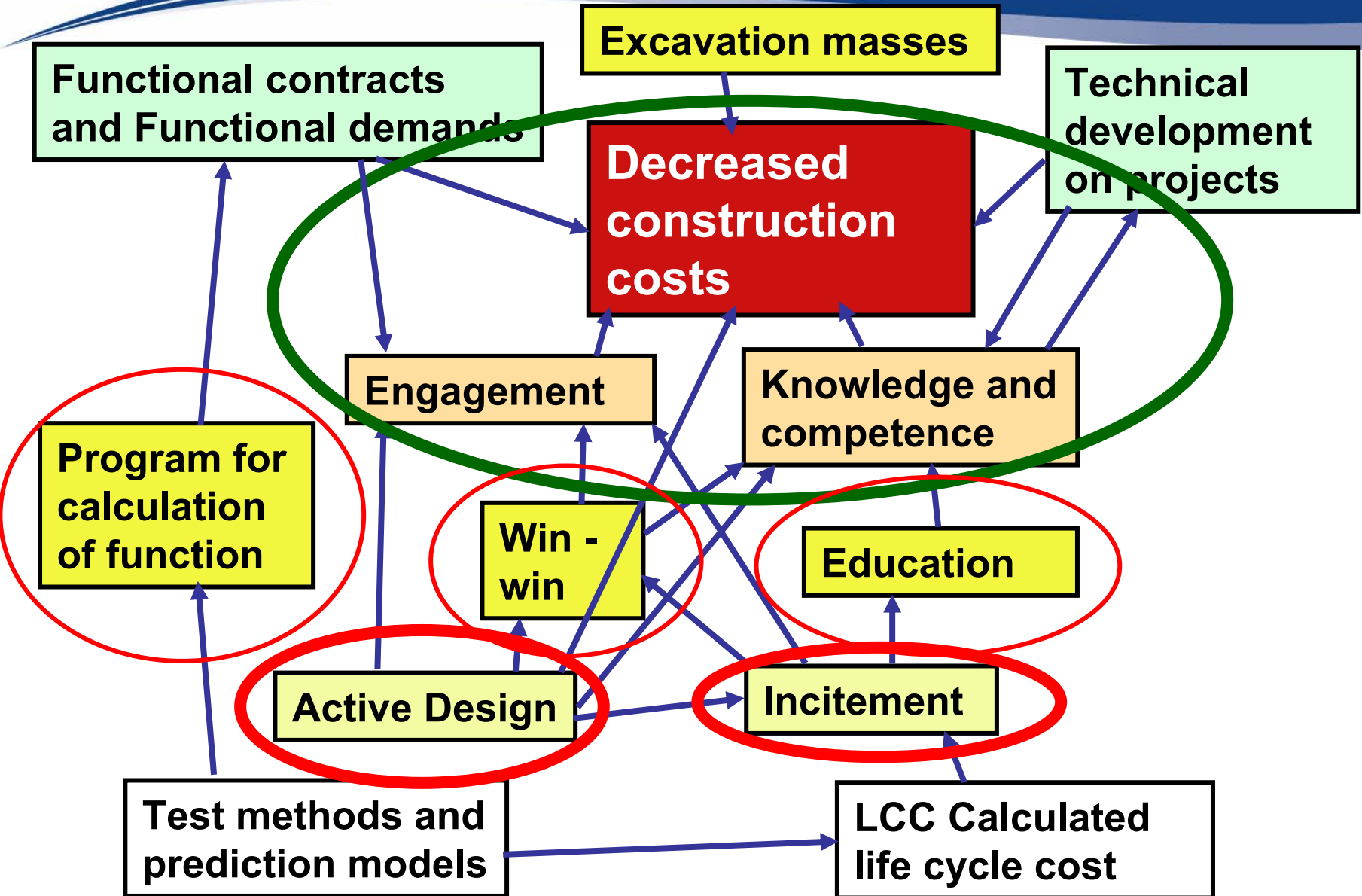


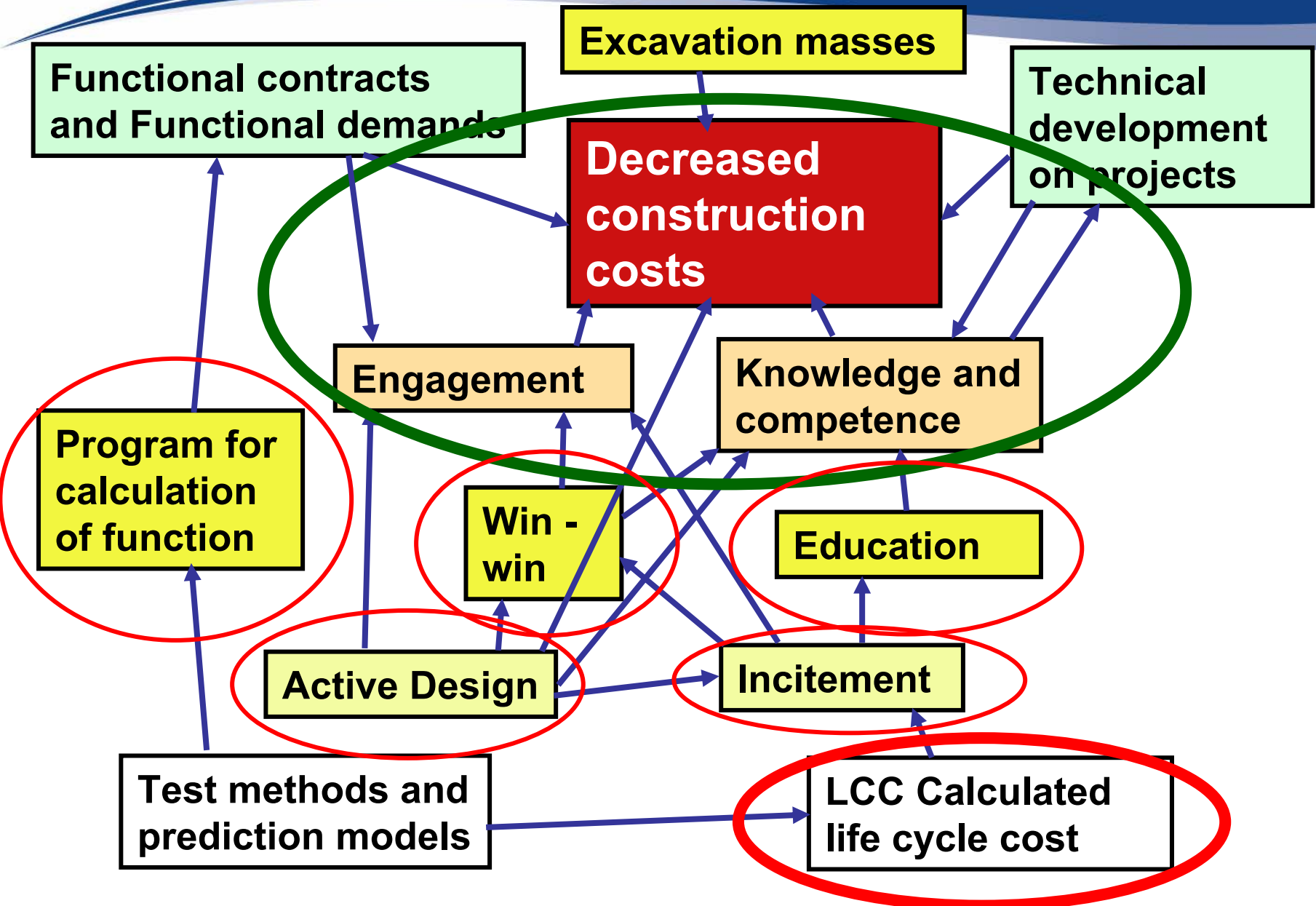
All these three circumstances must be a reality, if it should be a habit to work with the Win – win concept. Preferably for all persons who are working in a project

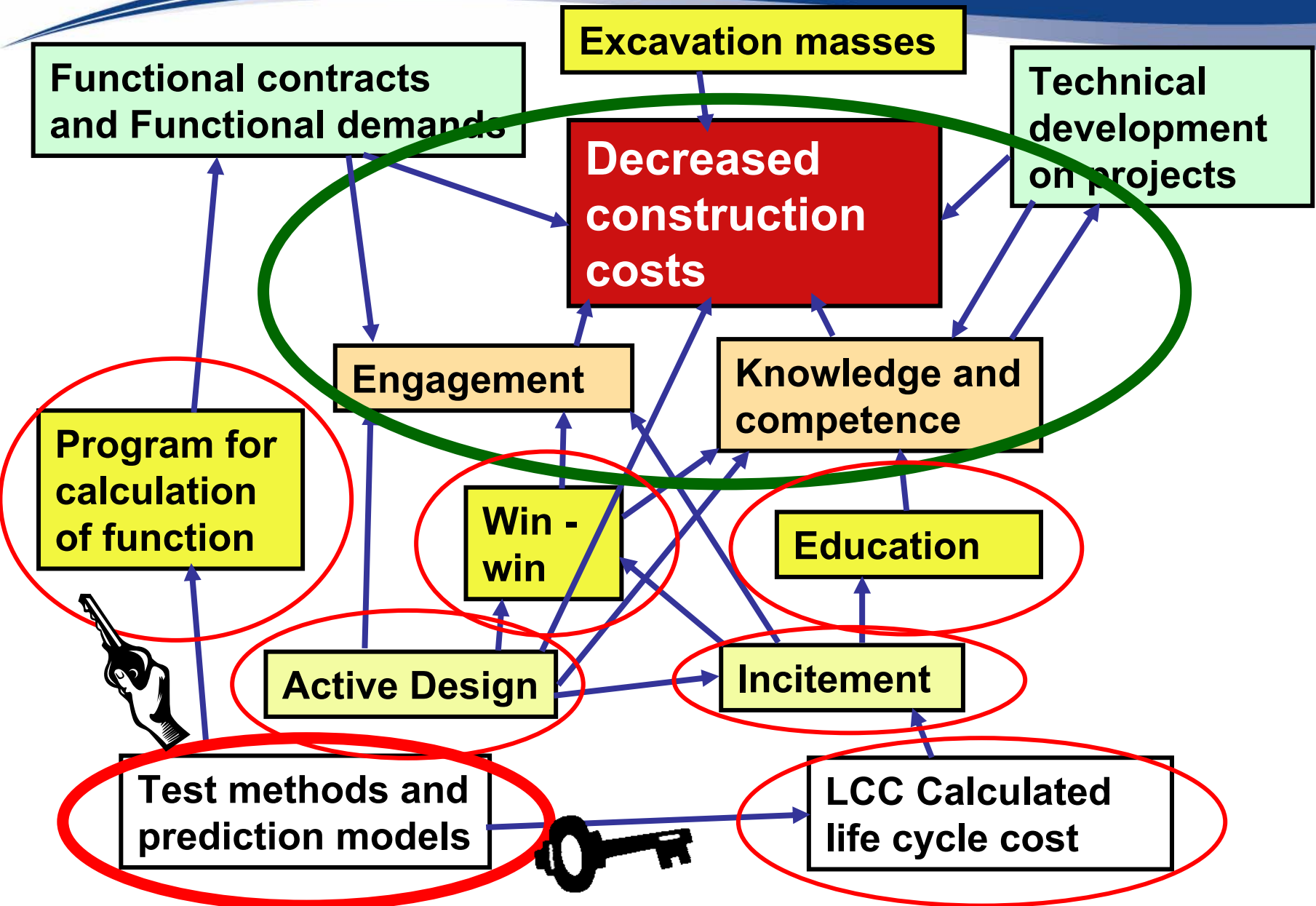






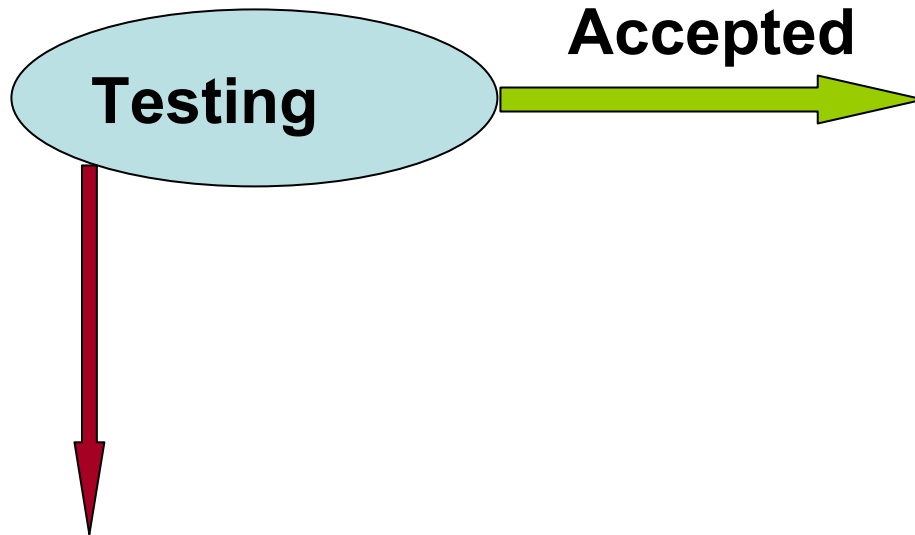






Implementation of new technique

Normal rules today

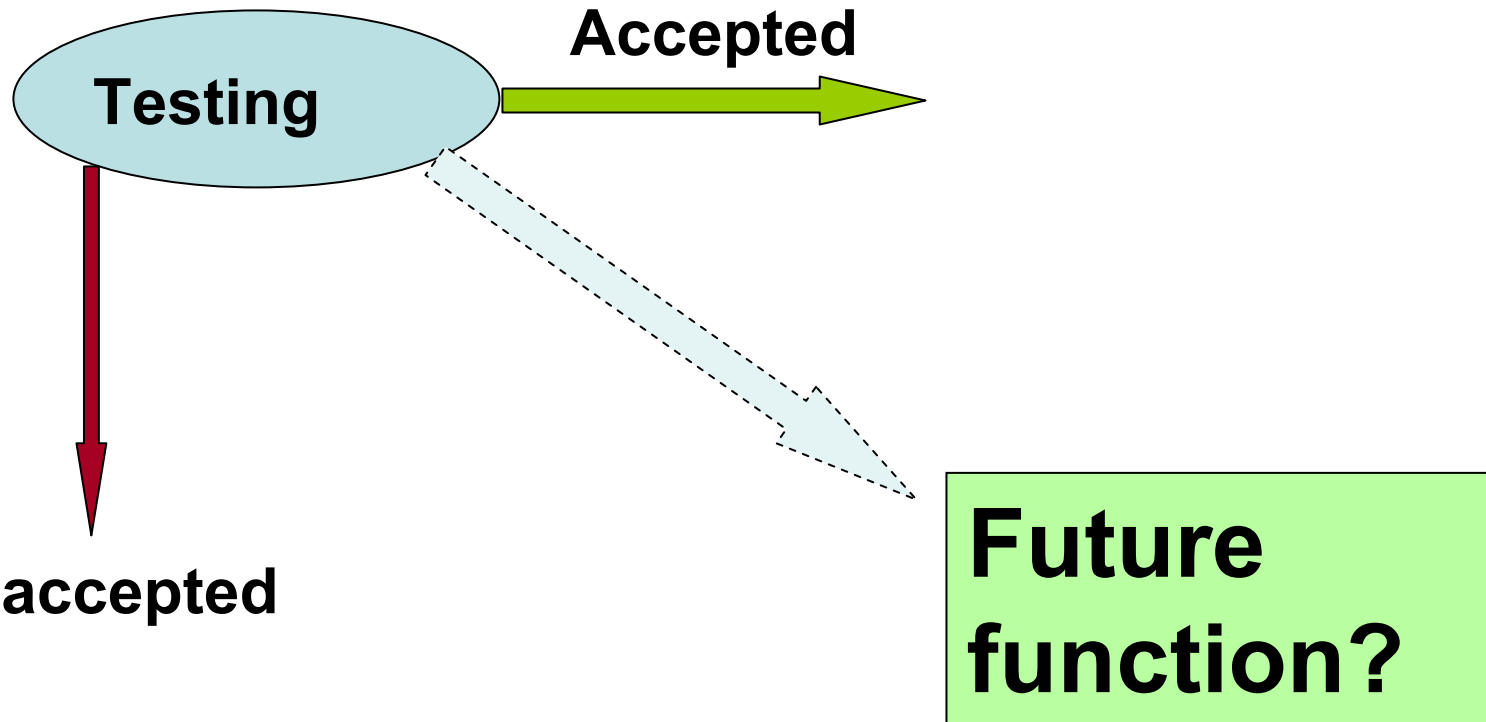


Accepted

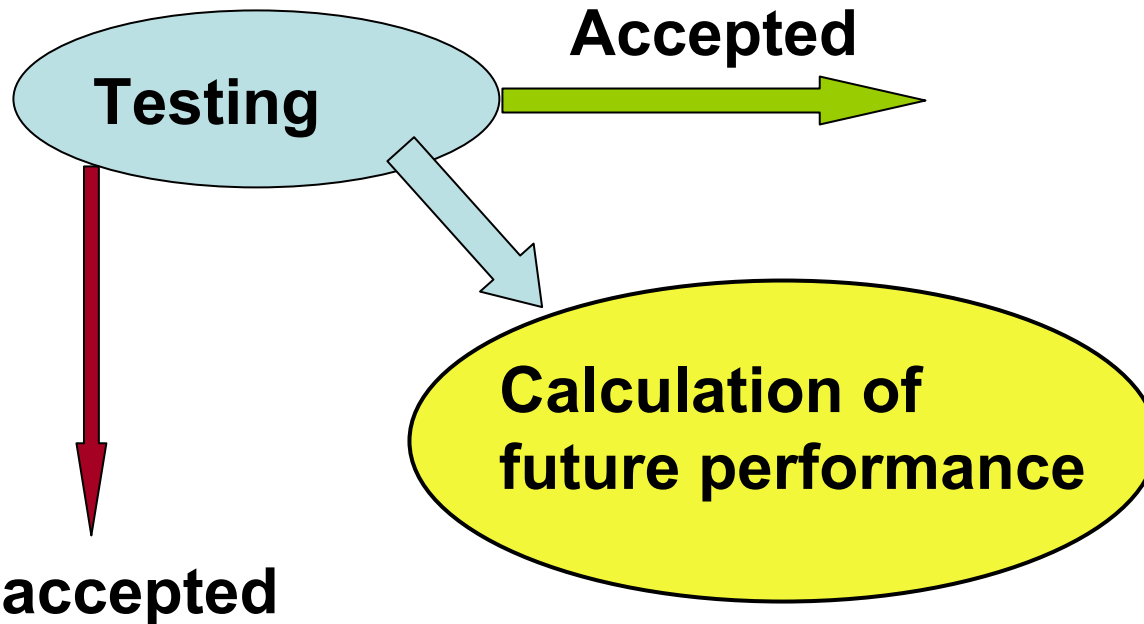
Testing

Not accepted

Normal rules today

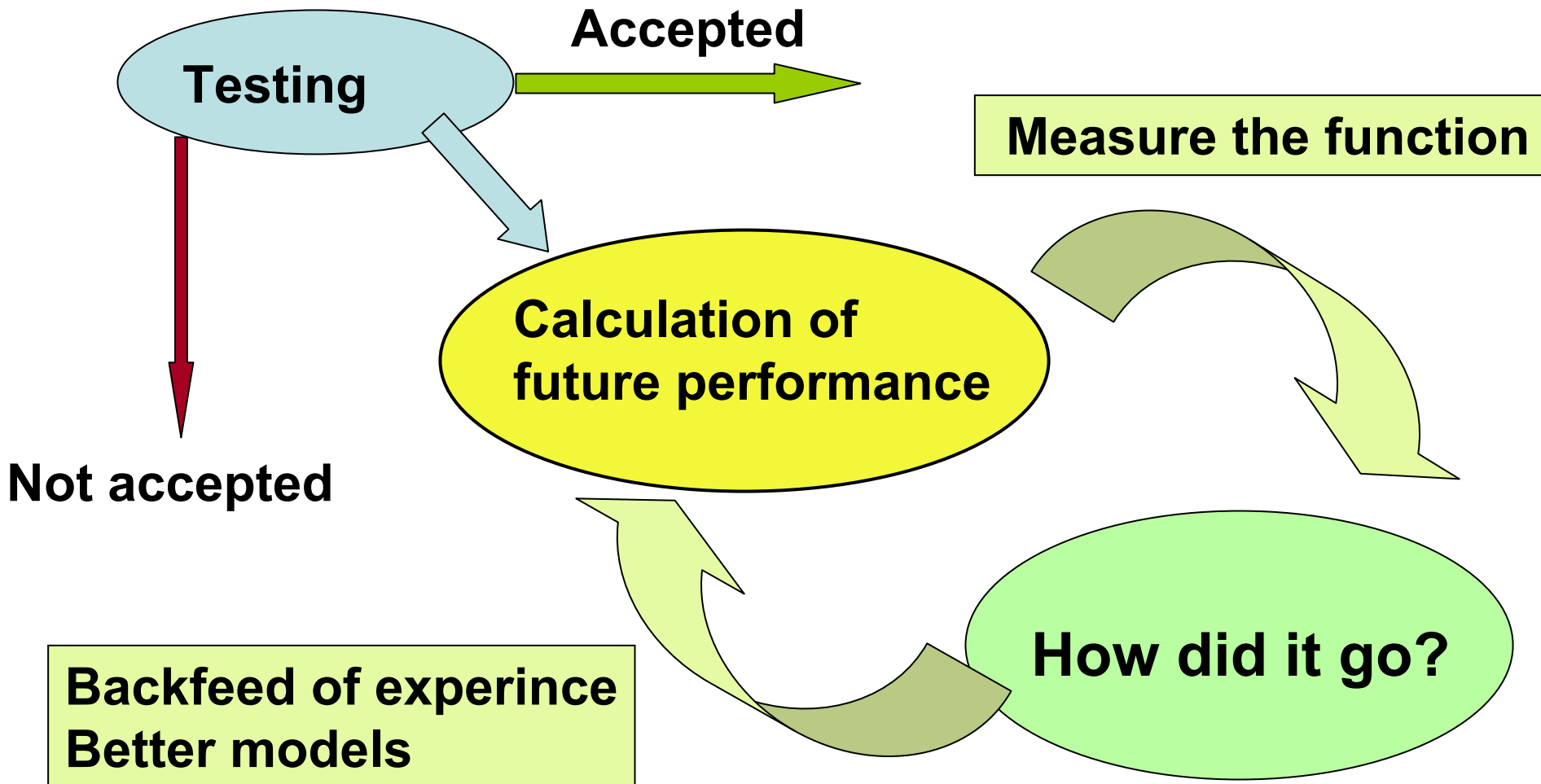


It is possible to work like this today!

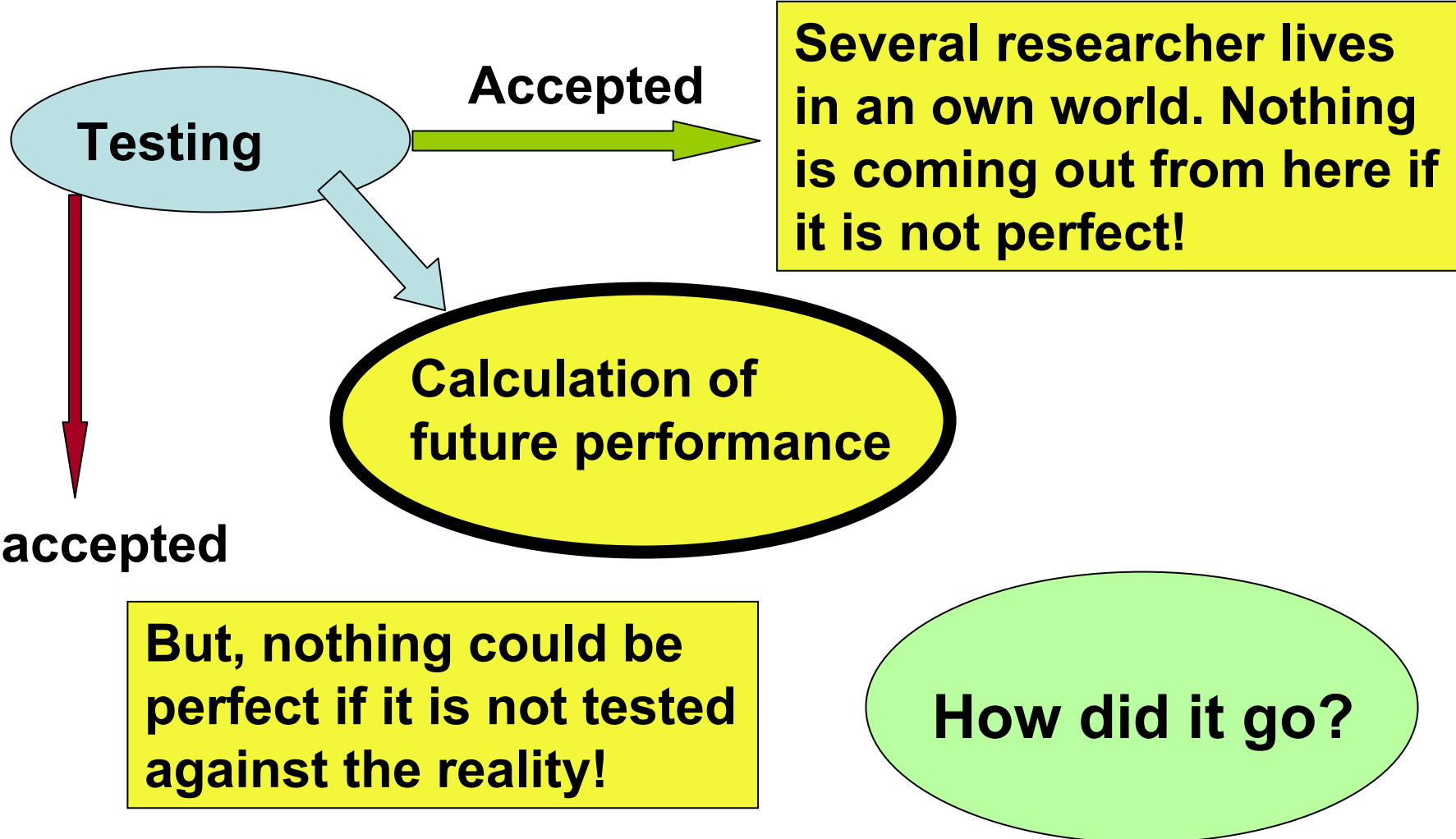


Test results, material characteristics or quality on execution, are used together with values on traffic, climate and moisture in order to calculate future function

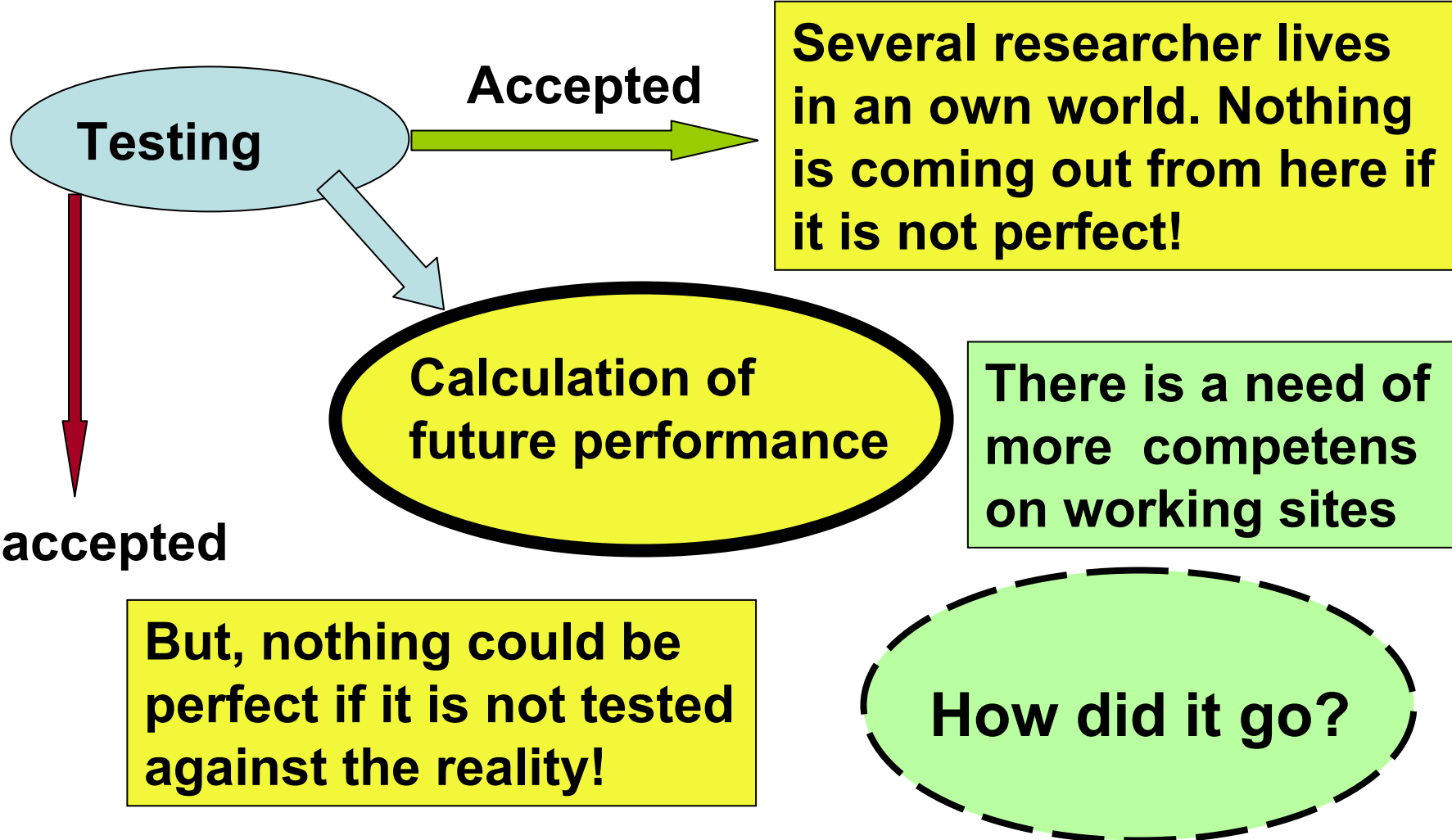
An ideal way of working!



Why doesn't this work today?



What is the problem today?



Active Design

ACTIVE DESIGN

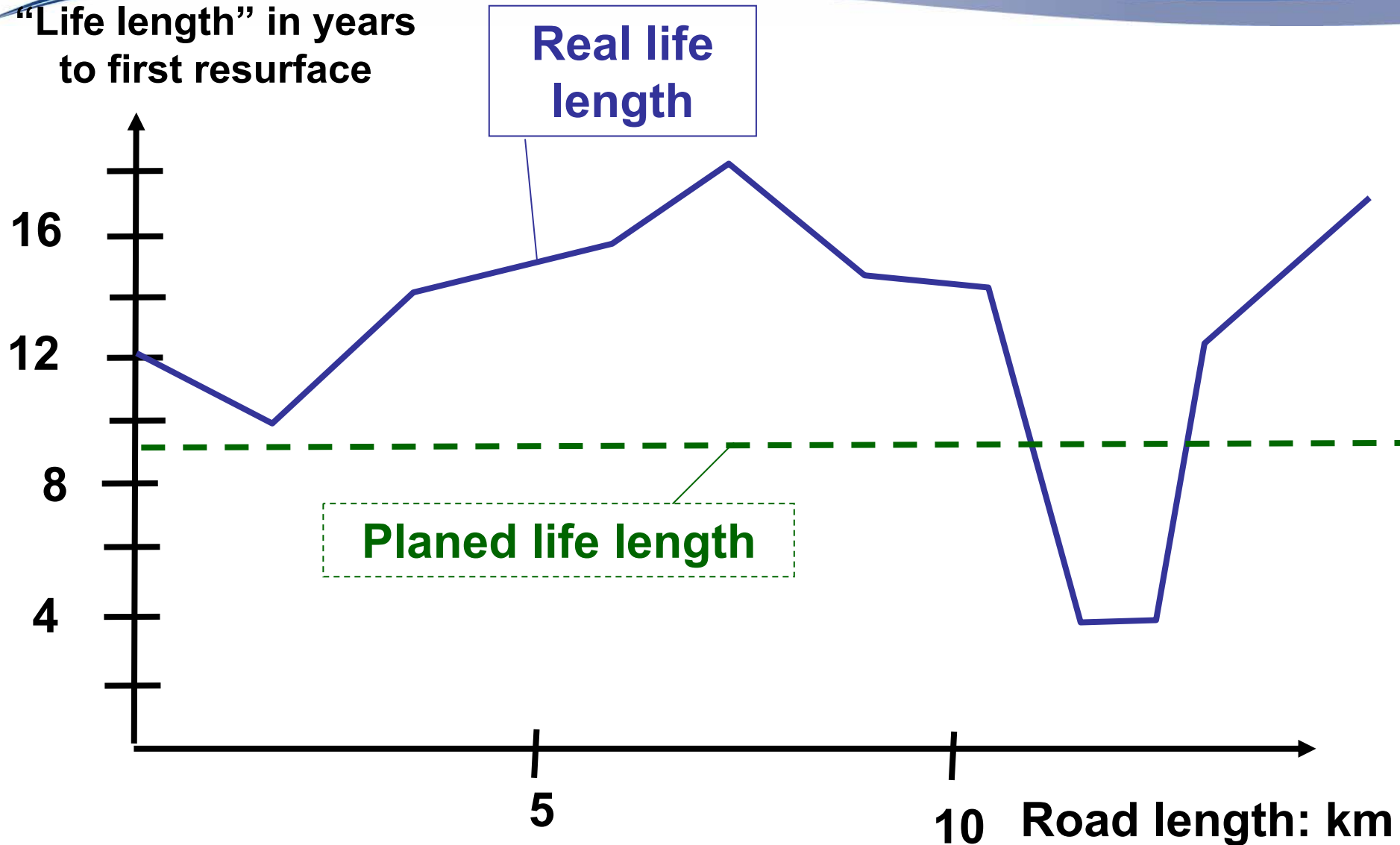
Soil and rock, used in road construction has an uneven quality: Design after real quality!

Use the best material close to the subgrade surface to get better bearing capacity

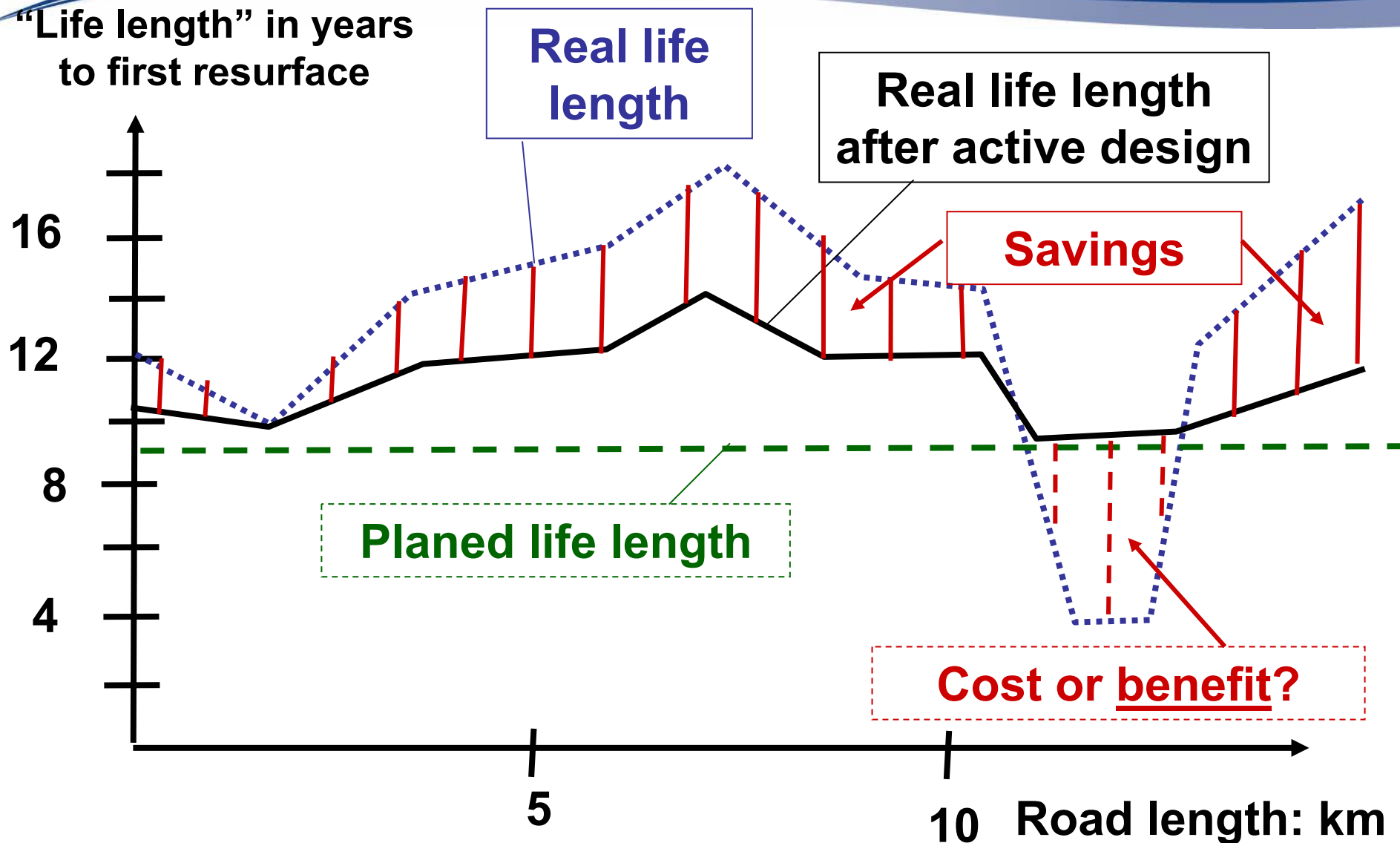
Calculate future function from test results on site in order to choose the optimal alternative

Incentive for better quality gives resources for improvement of the competence and technical development, and it also gives a strong motivation to produce with an improved quality

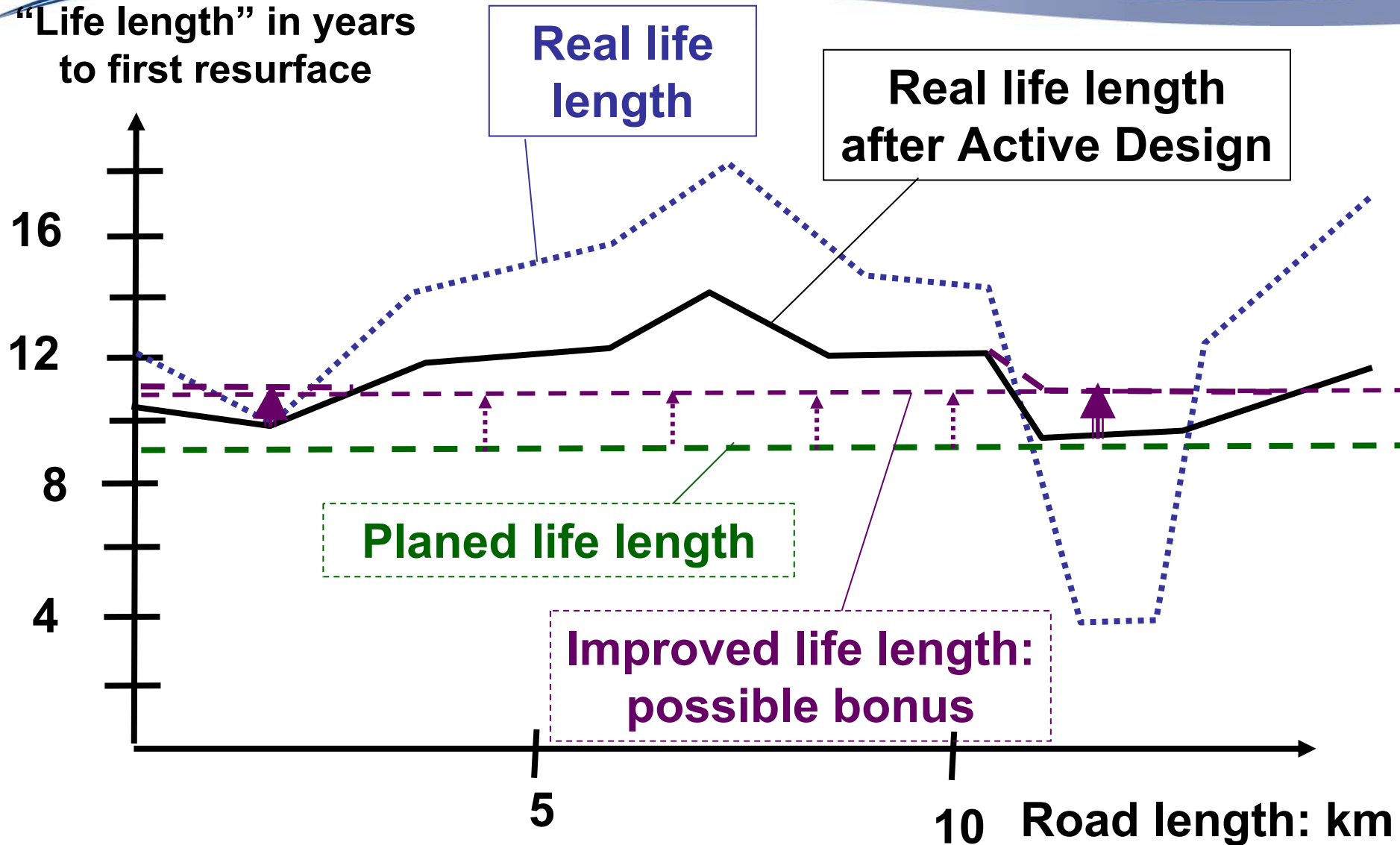
“Life length” in years
to first resurface



“Life length” in years
to first resurface

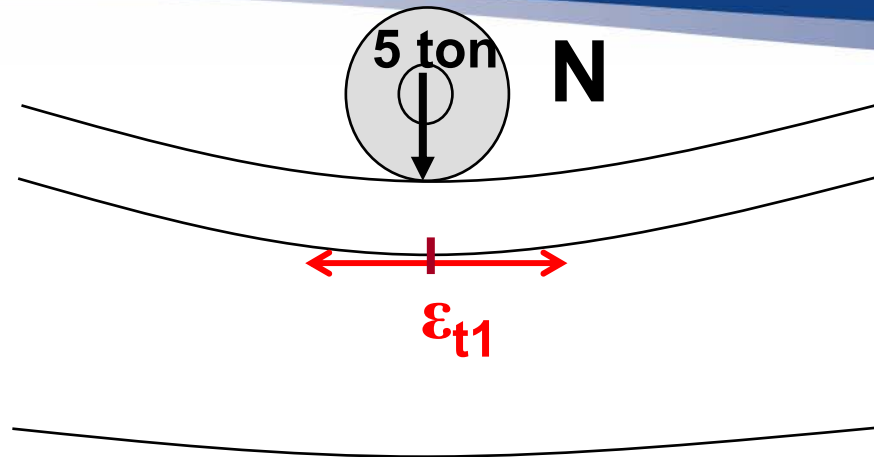


“Life length” in years
to first resurface



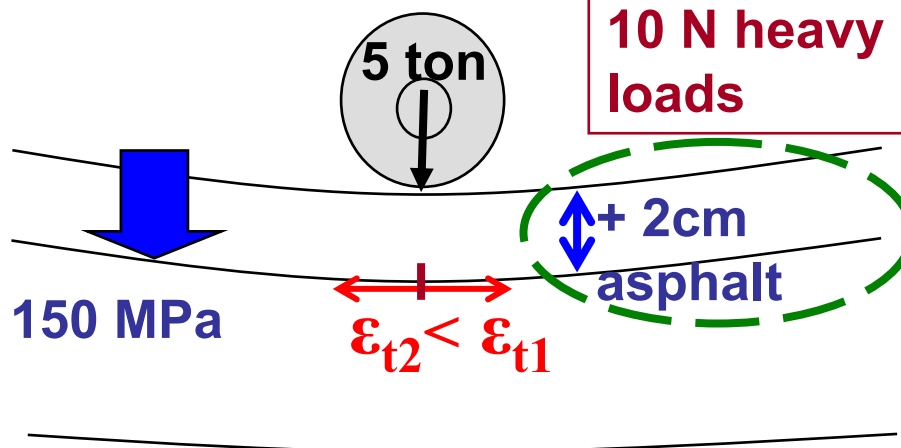
FATIGUE OF PAVEMENT

Improved life length; lower ϵ_{t1} to ϵ_{t2}

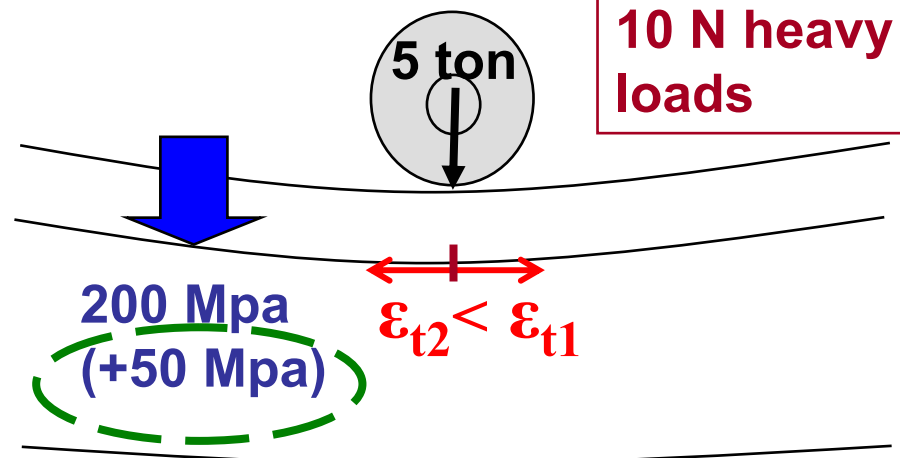


N heavy loads

ϵ = strain in bottom of asphalt

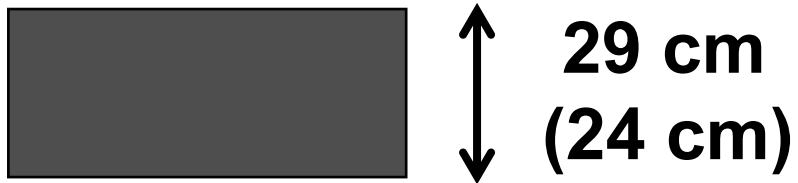


Alt 1: Thicker pavement, 2 cm, cost ca 2 Euro/m²

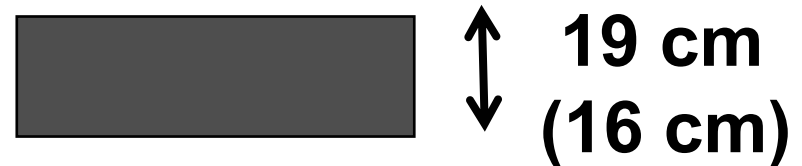


Alt 2: Extra compaction, cost ca 0,2 – 0,4 Euro/m²

Swedish standard before 1974



Soil subgrade



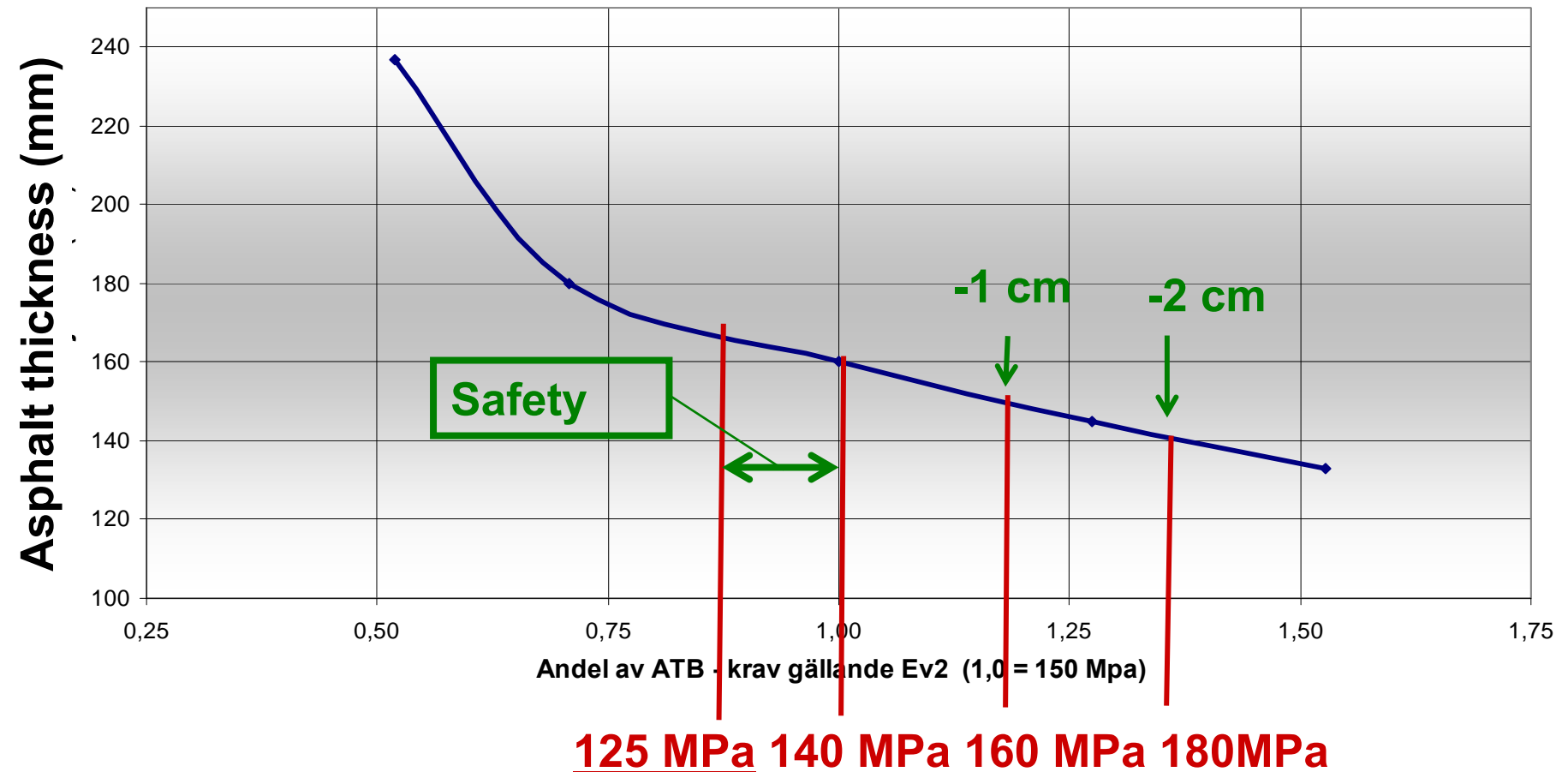
Rock subgrade



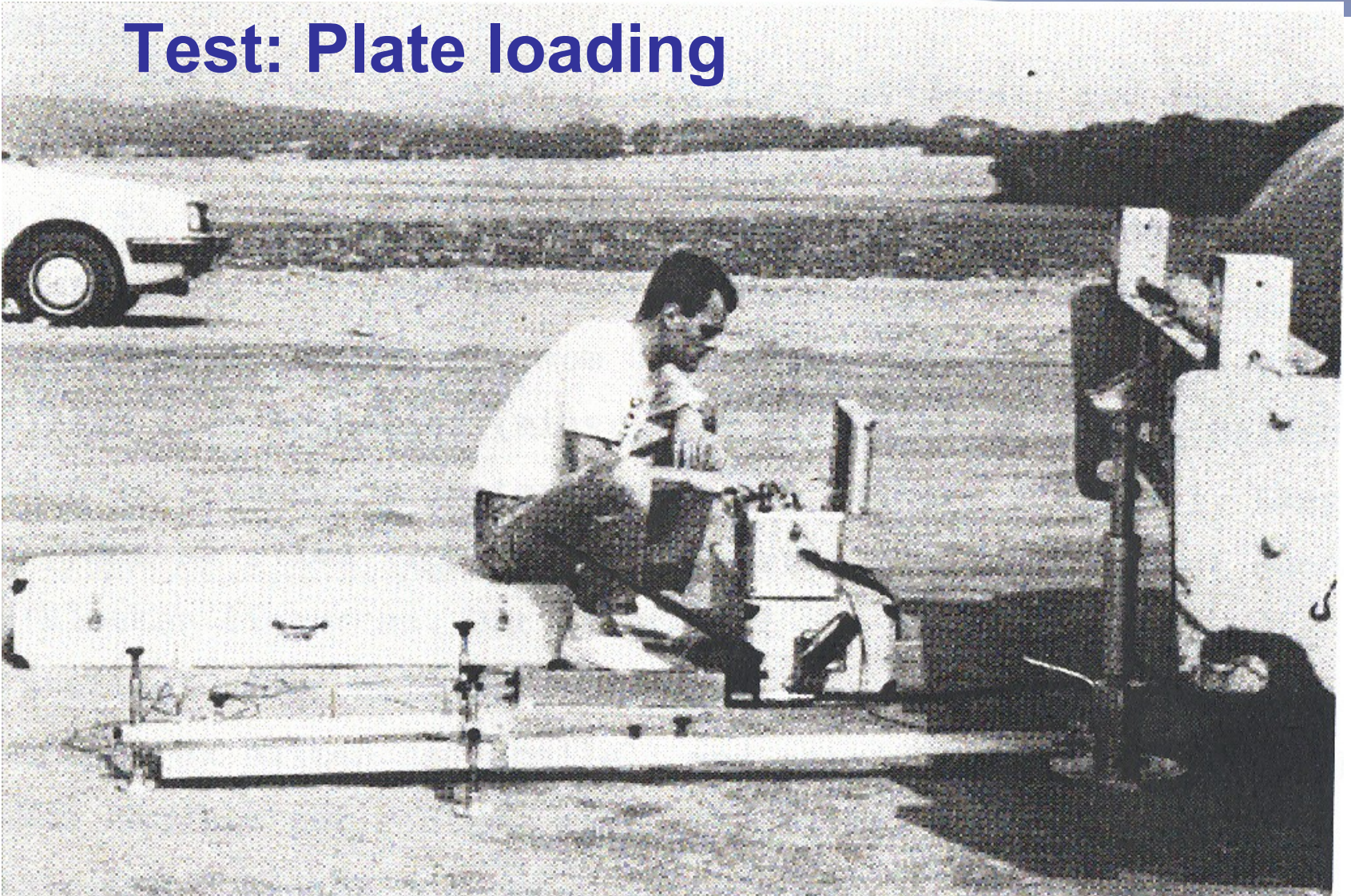
**Thickness highest class
(second highest class)**

QUALITY LEVELS

Change in pavement thickness with surface covering measurement on the compactor

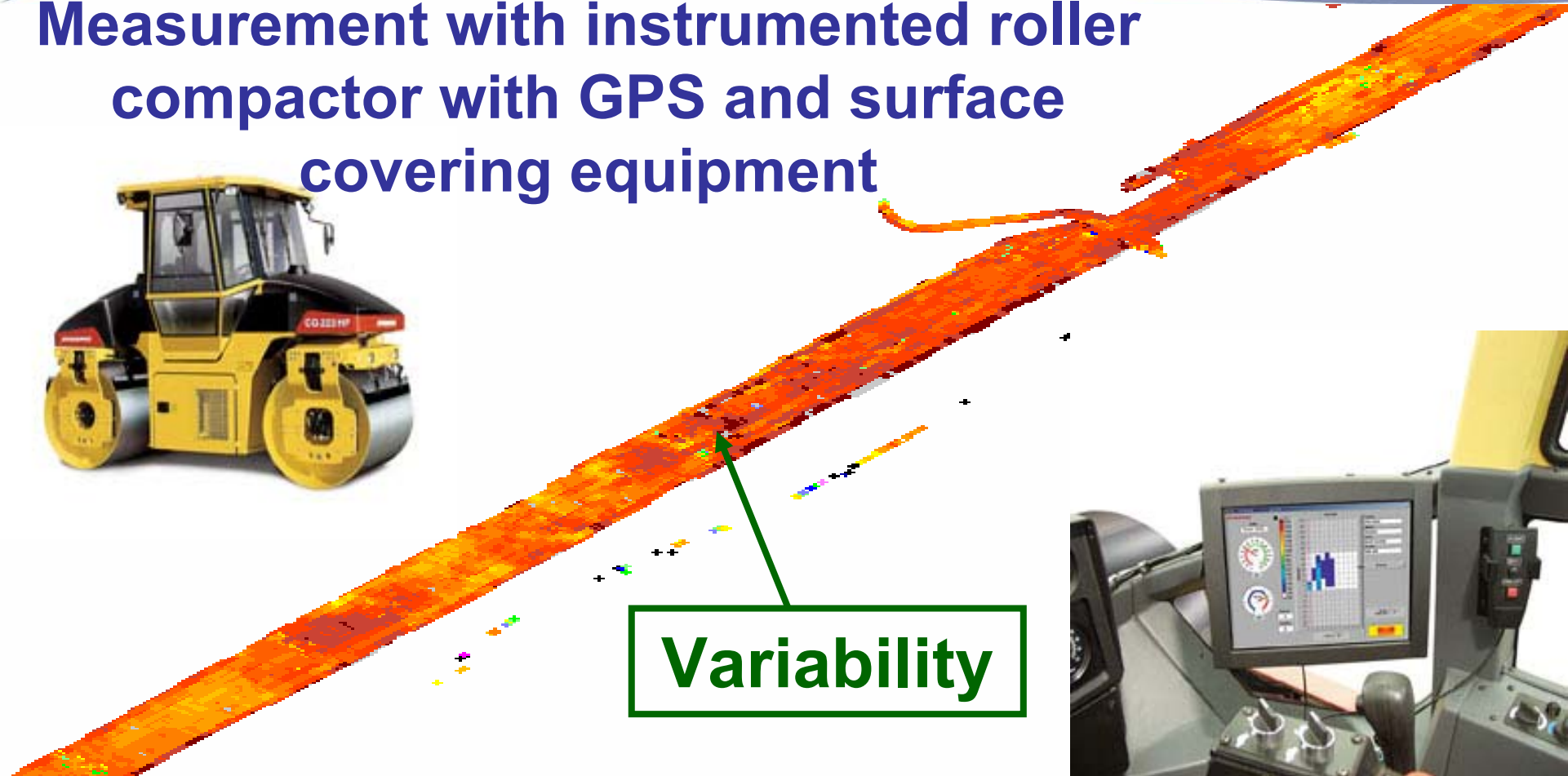


Test: Plate loading



Equipment for measuring bearing capacity with plate loading

Measurement with instrumented roller compactor with GPS and surface covering equipment



Variability



III

IV

100

64

78

92

106

120

134

148

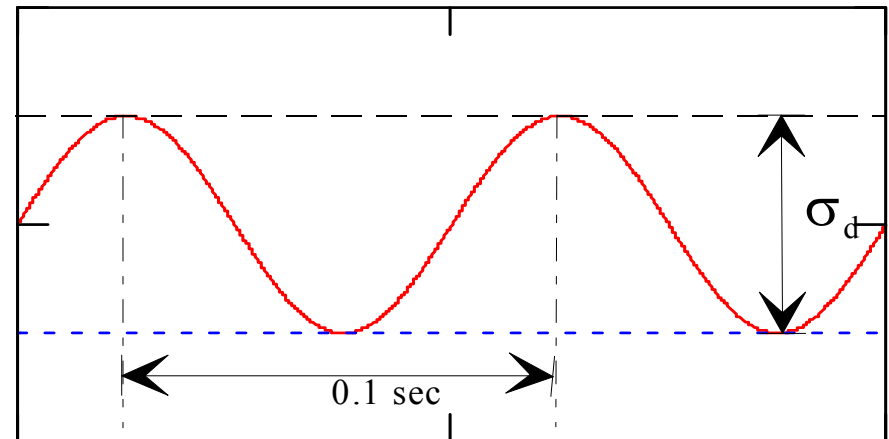
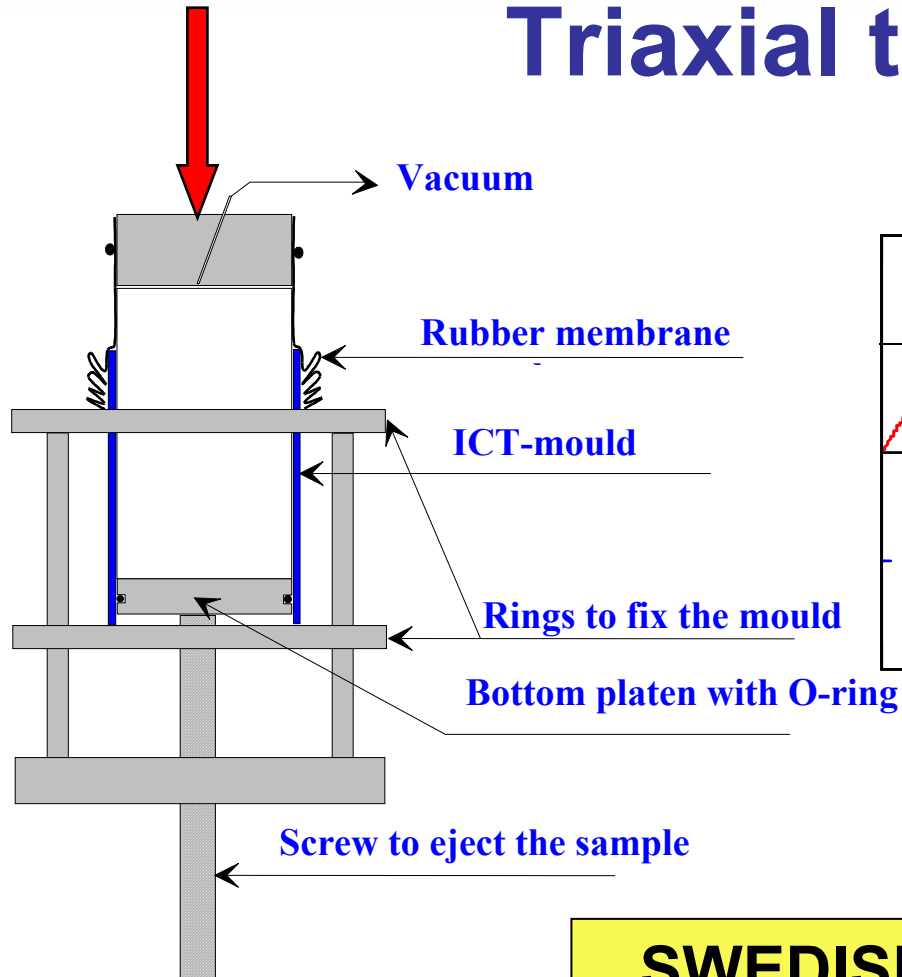
162

176

190

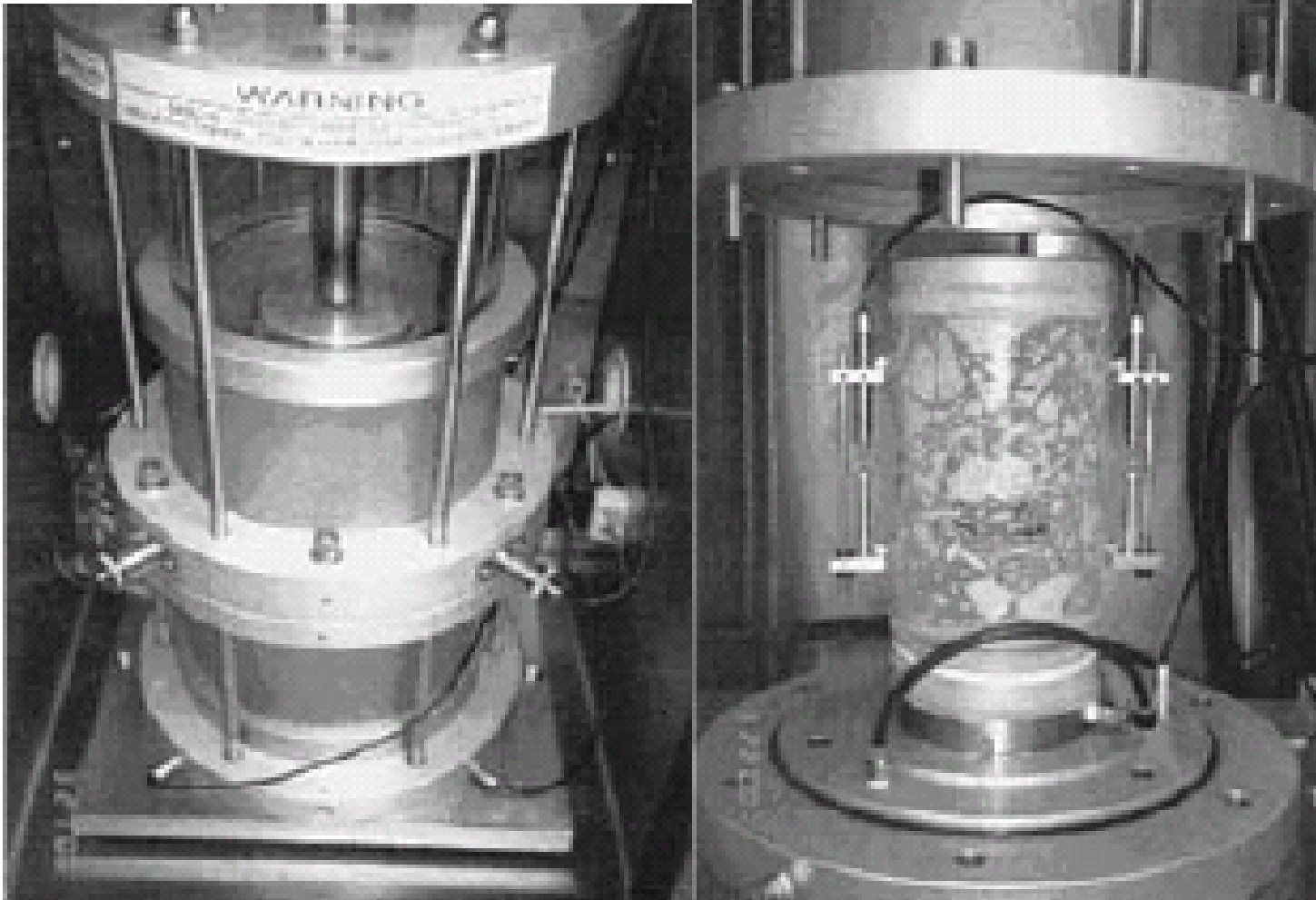
204

Triaxial test



SWEDISH STANDARD
SS-EN 13286-7:2004
Appointed 2004-02-13

Equipment for Triaxial tests

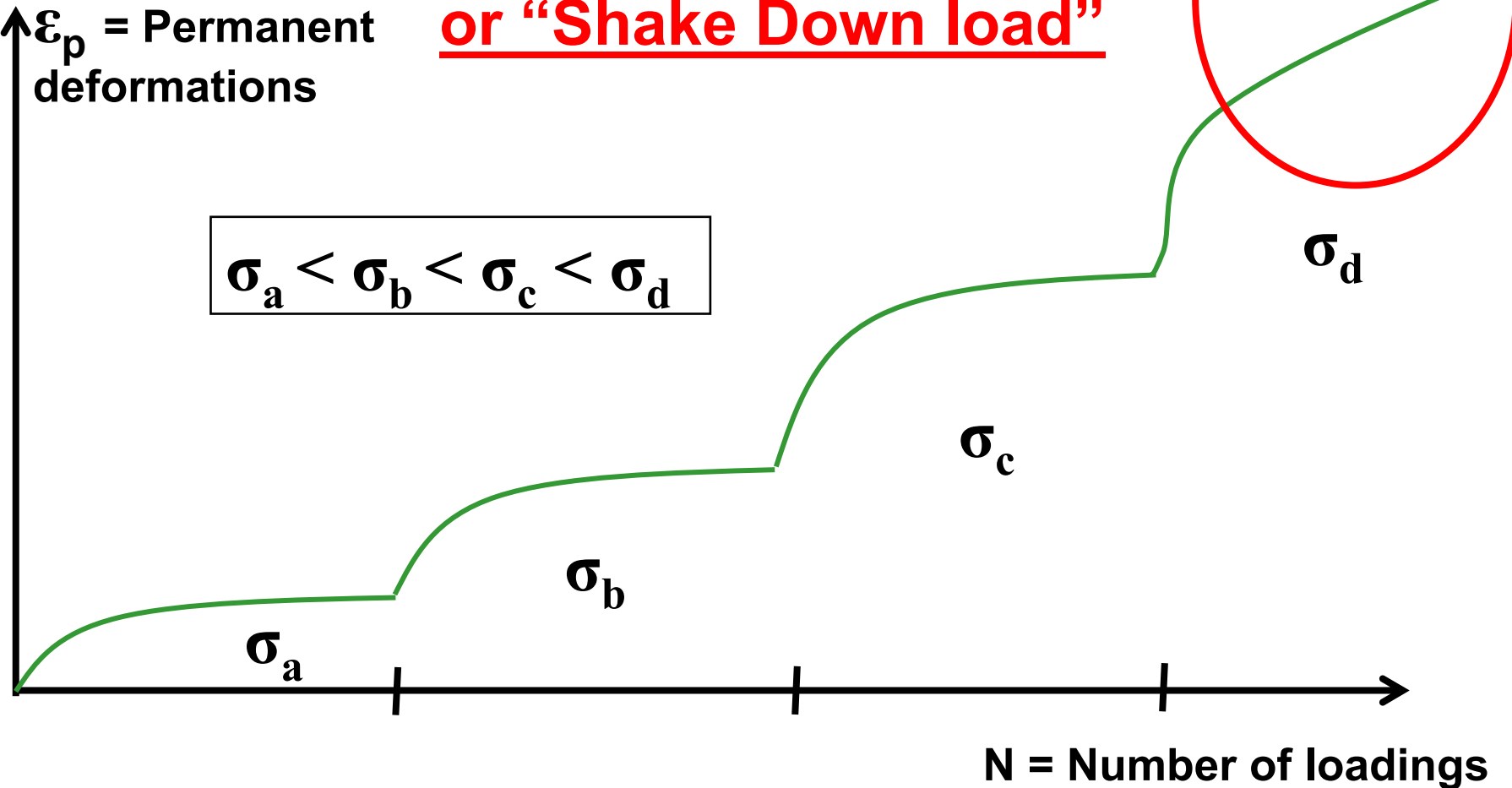


Triaxial test "Fatigue load"

ϵ_p = Permanent
deformations

or "Shake Down load"

$$\sigma_a < \sigma_b < \sigma_c < \sigma_d$$



Triaxial tests on unbound layers

Gives following data / material characteristics:

- **Unlinear static elasticity modulus (resilient modulus)**
- **Unlinear dynamic elasticity modulus (resilient modulus)**
- **Fatigue strength ("Shake Down" load)**
- **Input data for calculation of permanent deformations**

In the project “Active Design” SRA co-operates with the contractors (SBUF) and consultants in order to use new knowledge for mechanistic design.

This knowledge is taken from research in Sweden and other countries above all from SAMARIS and Design Guide

MATERIAL MODELS

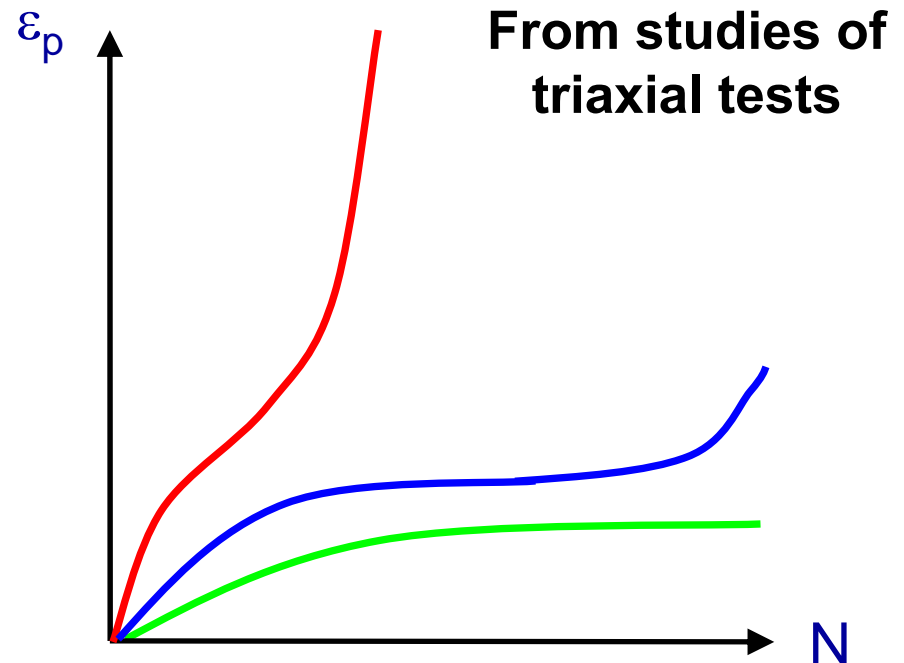
Rutting in unbound materials

**Shake Down load
(Dresden)**

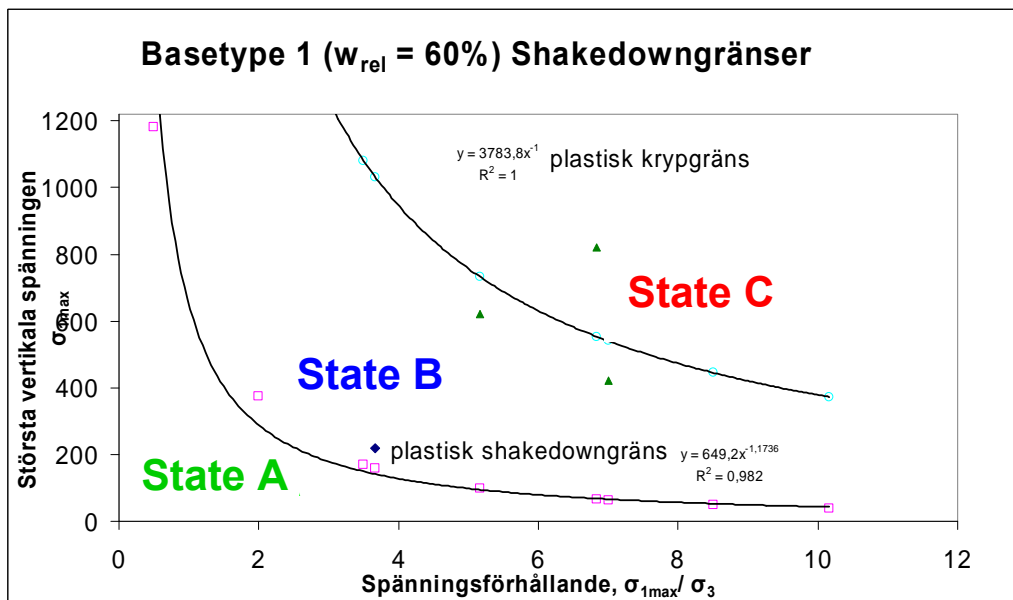
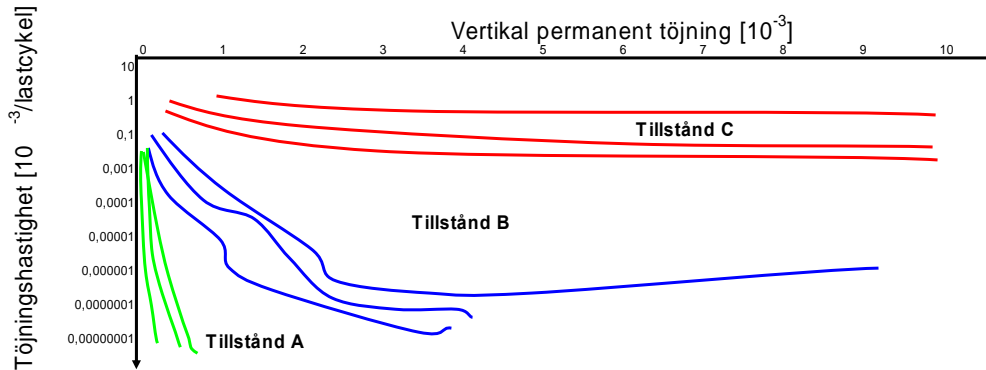
Decision of critical stress conditions in unbound layers

- Shakedown concept
 - Stable state (little rutting)
 - Unstable state (severe rutting)

- State A (stable behaviour)
- State B (unstable behaviour)
- State C (collapse)



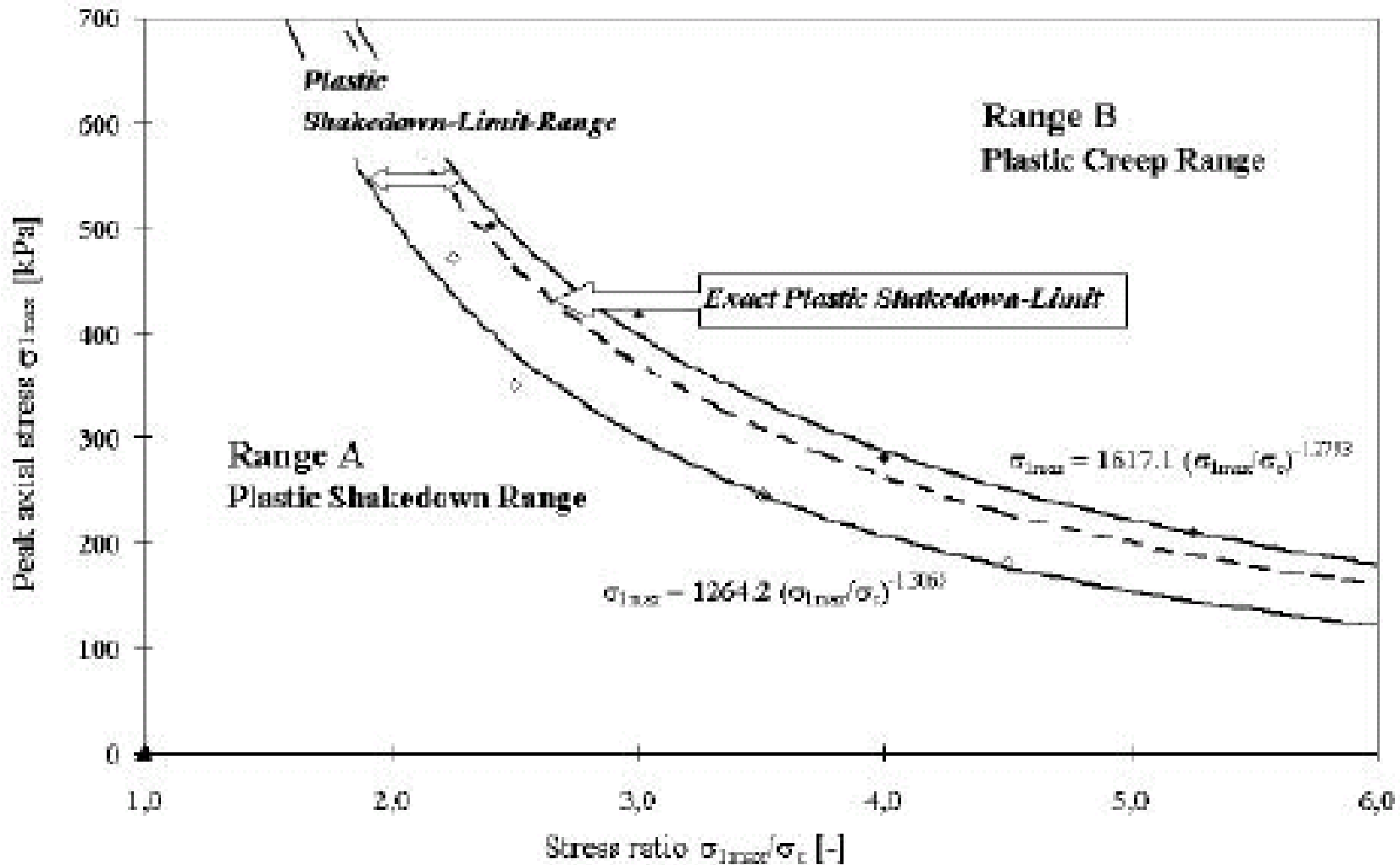
The Shake Down concept



$$\sigma_{1,max} = \alpha \cdot \left(\frac{\sigma_{1,max}}{\sigma_c} \right)^\beta$$

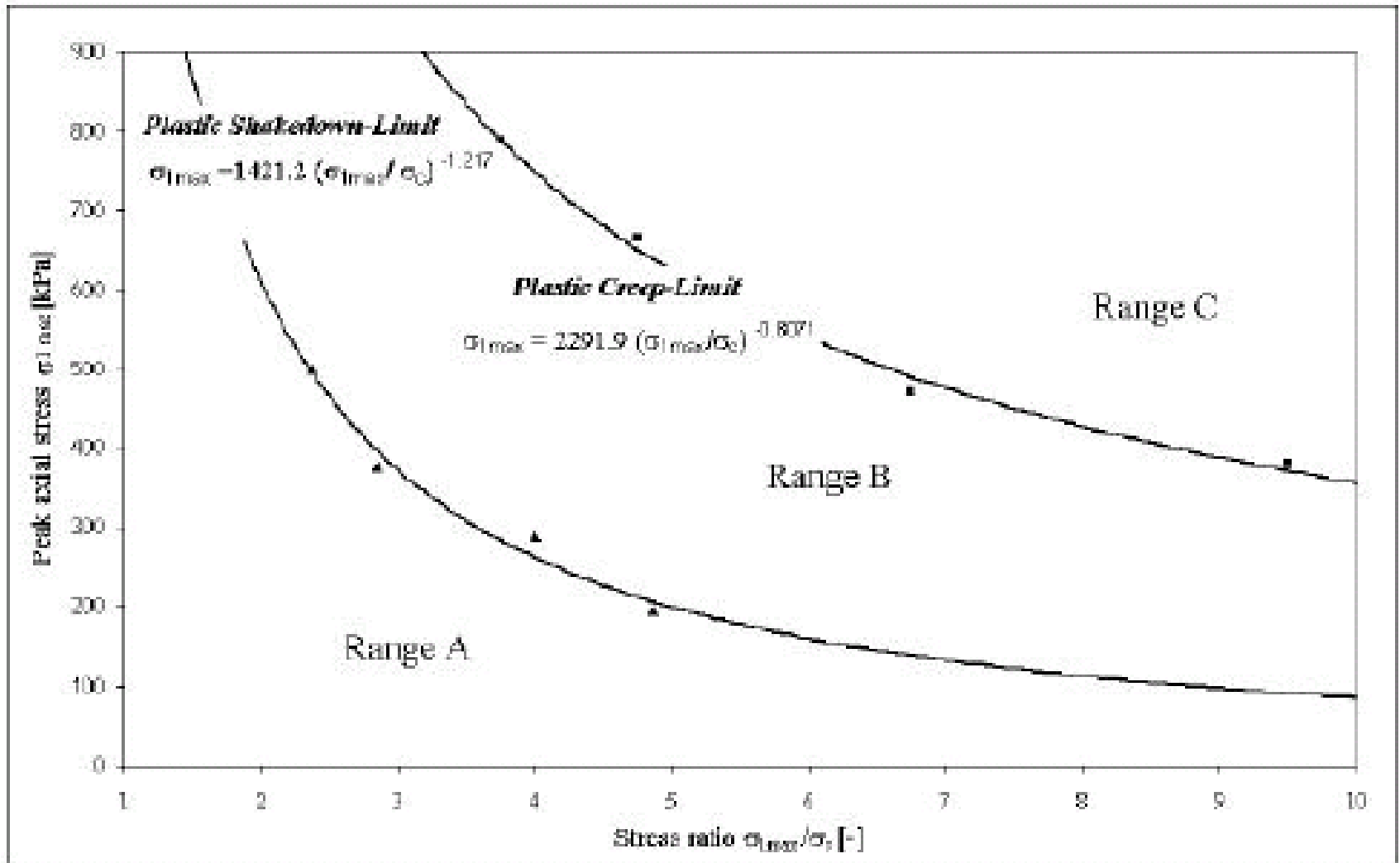
Shake down load

From Sabine Werkmeister doctor thesis



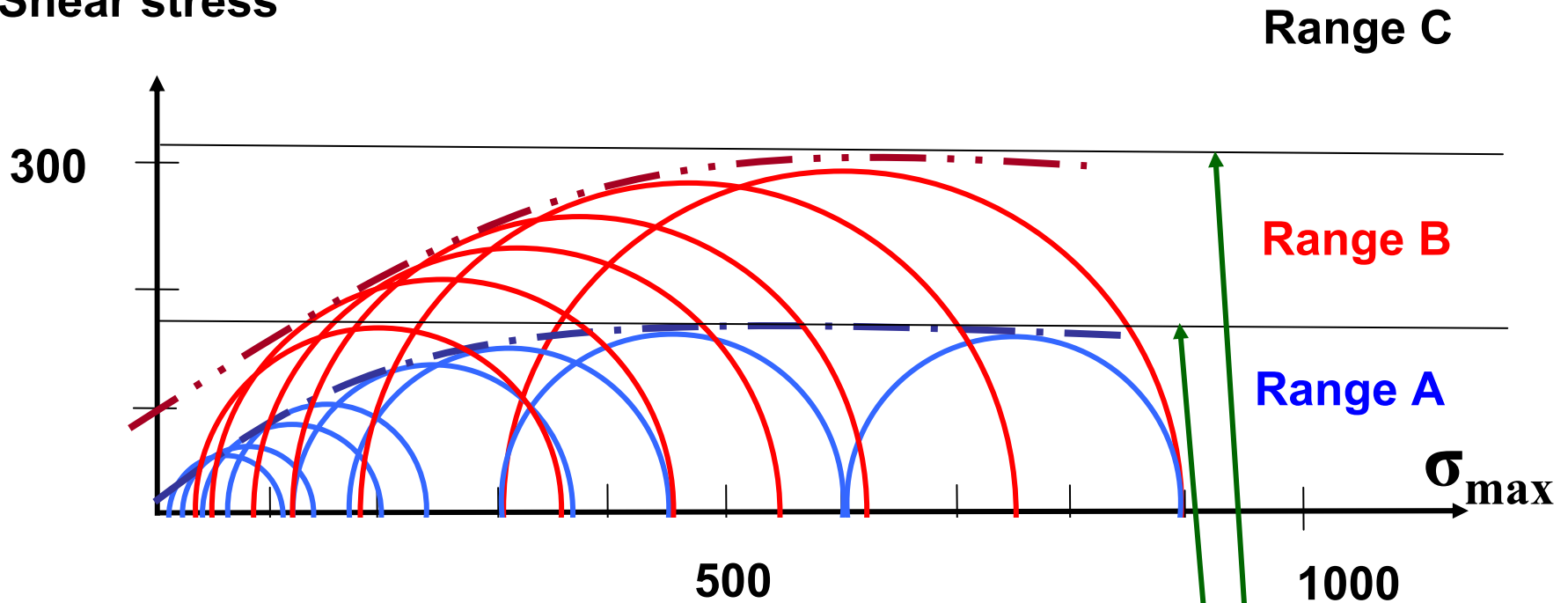
Shake down load

From Sabine Werkmeister doctor thesis



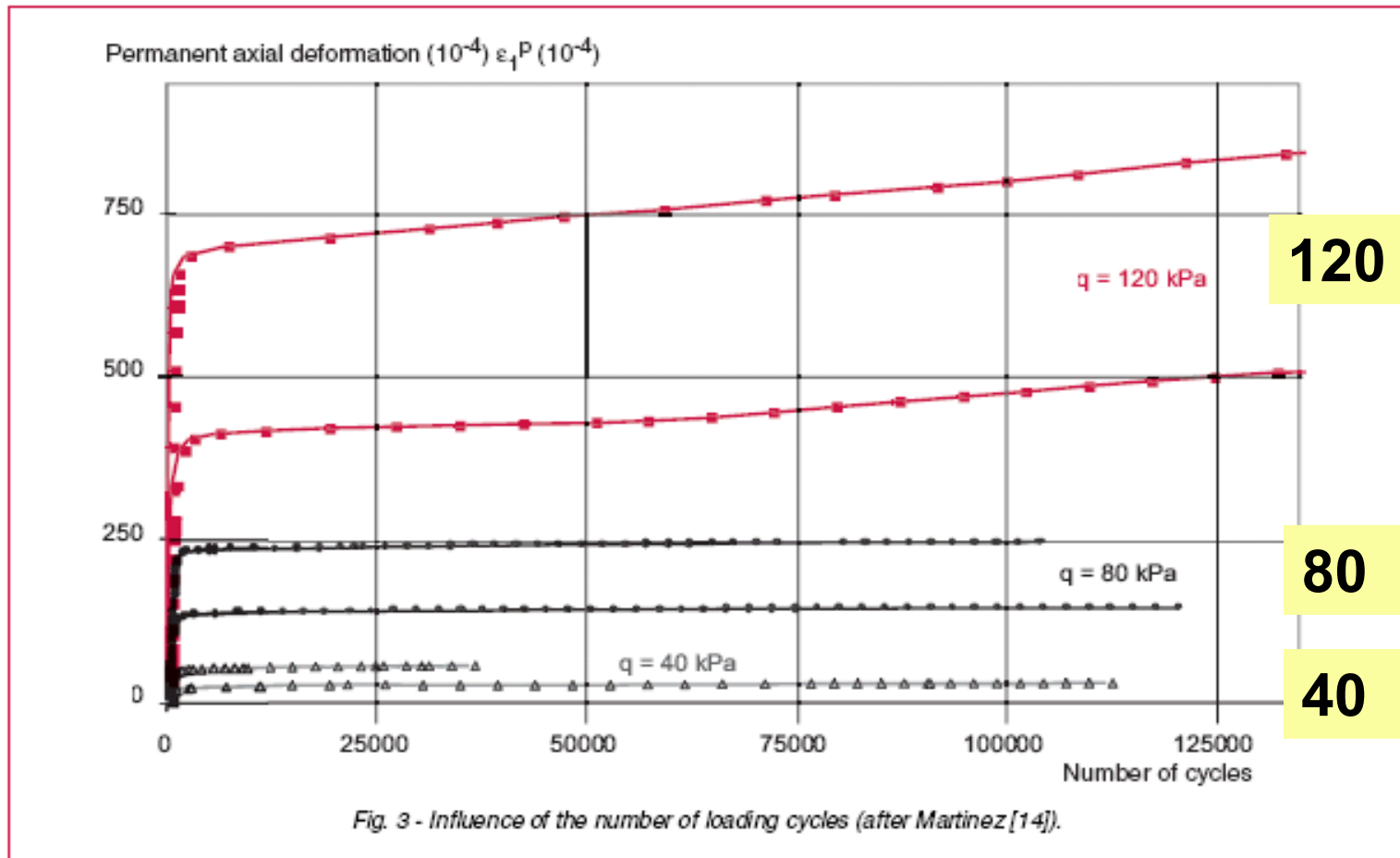
Shake down load

Shear stress



Possible kriterium

Permanent deformations, depending on shear stress (tests from SAMARIS)

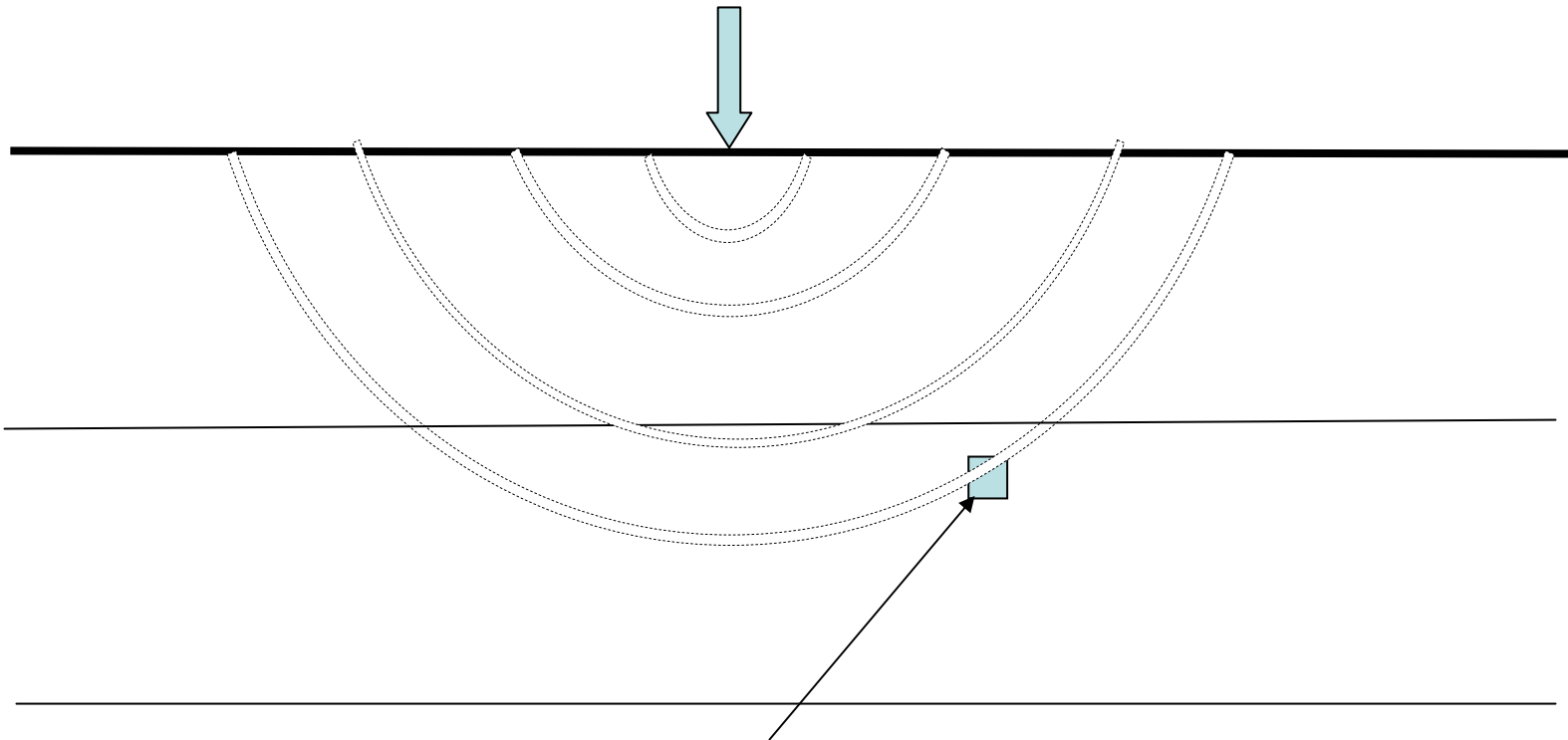


Mechanistical background

TABLES

Number/Amount/Quality Thickness	Heavy traffic	Amount of frost	Subgrade material	Other
Asphalt				
Base				
Sub base				

MULTILAYER MODELS



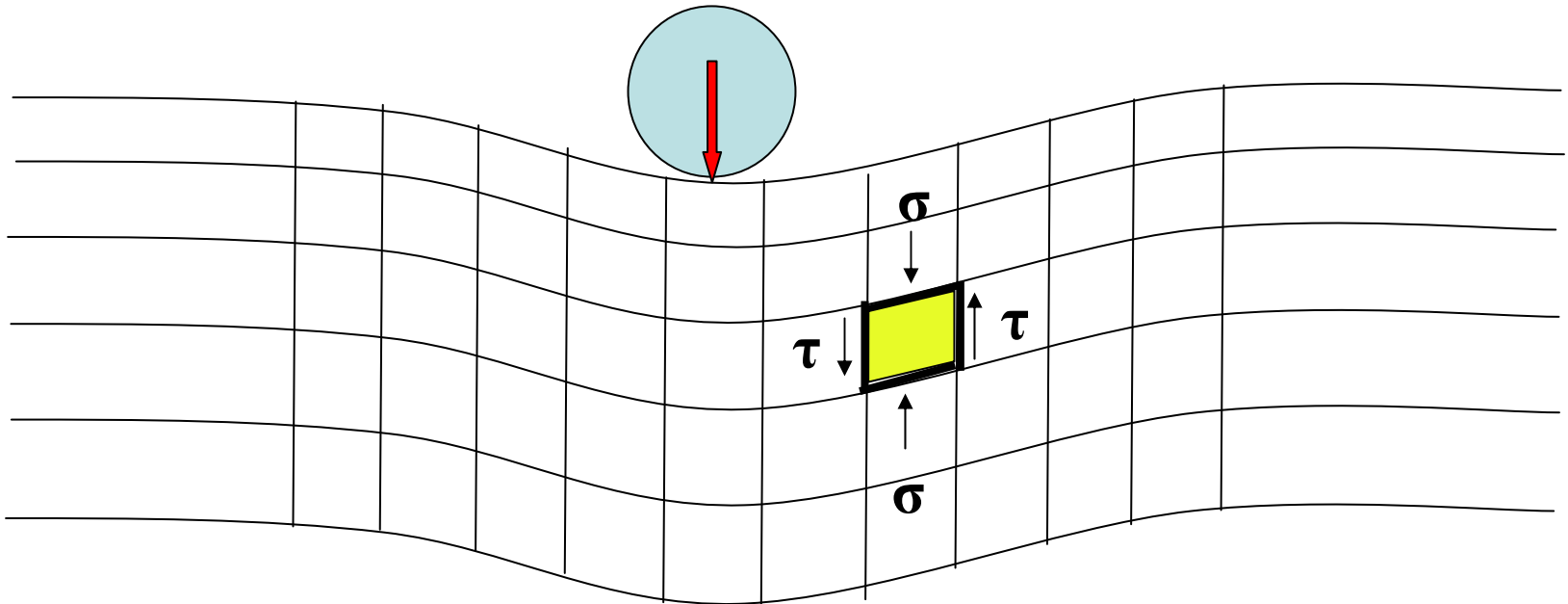
Elastic stress and strain could be calculated in different positions

MULTILAYER MODELS

Prerequisites:

- **The material is linear elastic**
- **The material can take tensile stress, even if it is wrong (unbound material)**
- **The material has no weight**
- **The material has infinite extension in all directions**

FINIT ELEMENT MODELS (FEM)



Every little part must be in stress equilibrium and deform in such a way that all pieces fits together.

FINIT ELEMENT MODELS (FEM)

Prerequisites:

- **Different material models could be used**
- **The material can take tensile stress or not (unbound material)**
- **The weight of the material could be included in the calculations**
- **The real geometry of the road can be simulated**

Unbound layer: Simulated E-modulus

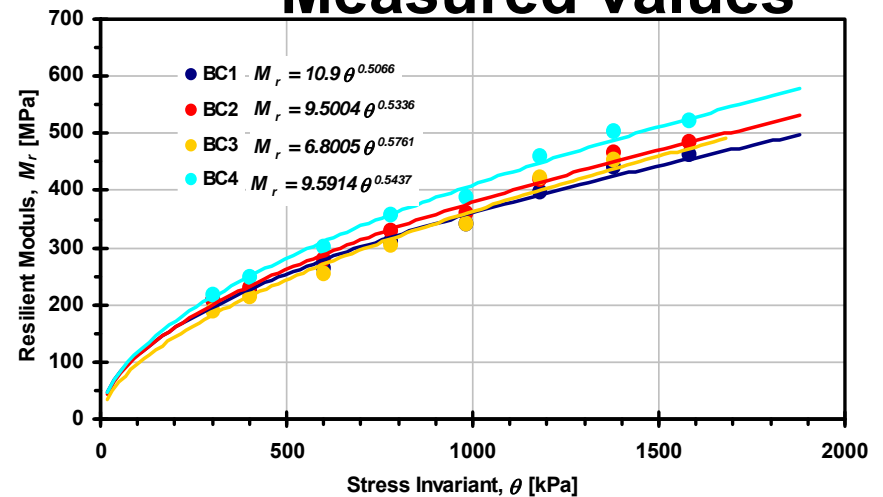
 M_r MPa

$$M_r = k_1 \Theta^{k_2} \text{ (Seed et al.)}$$

The Swedish Code:
Linear elasticity

VagFEM

Measured values


 Θ kPa

**Different material
gives different
resilient modulus**

**Exemple
from Norway
and Finland**

**Stress
dependant
resilient
modulus**

Materiale	Resilientmodul (MPa)			
	$\theta=100$ kPa	$\theta=200$ kPa	$\theta=300$ kPa	$\theta=400$ kPa
Andalen knust fjell 0 – 32 mm	262	390	493	662
Hedrum knust fjell 22 – 64 mm	227	328	406	532
Steinskogen knust fjell 22 – 64 mm	240	331	400	507
Åndalen knust fjell 22 – 64 mm	255	362	445	577
Hordaland knust fjell 22 – 64 mm	137	213	277	385
Åndalen knust fjell 0 – 32 mm (NGI pros.)	219	320	398	526
Åndalen knust fjell 22 – 64 mm (NGI pros.)	230	348	443	602

Design Guide

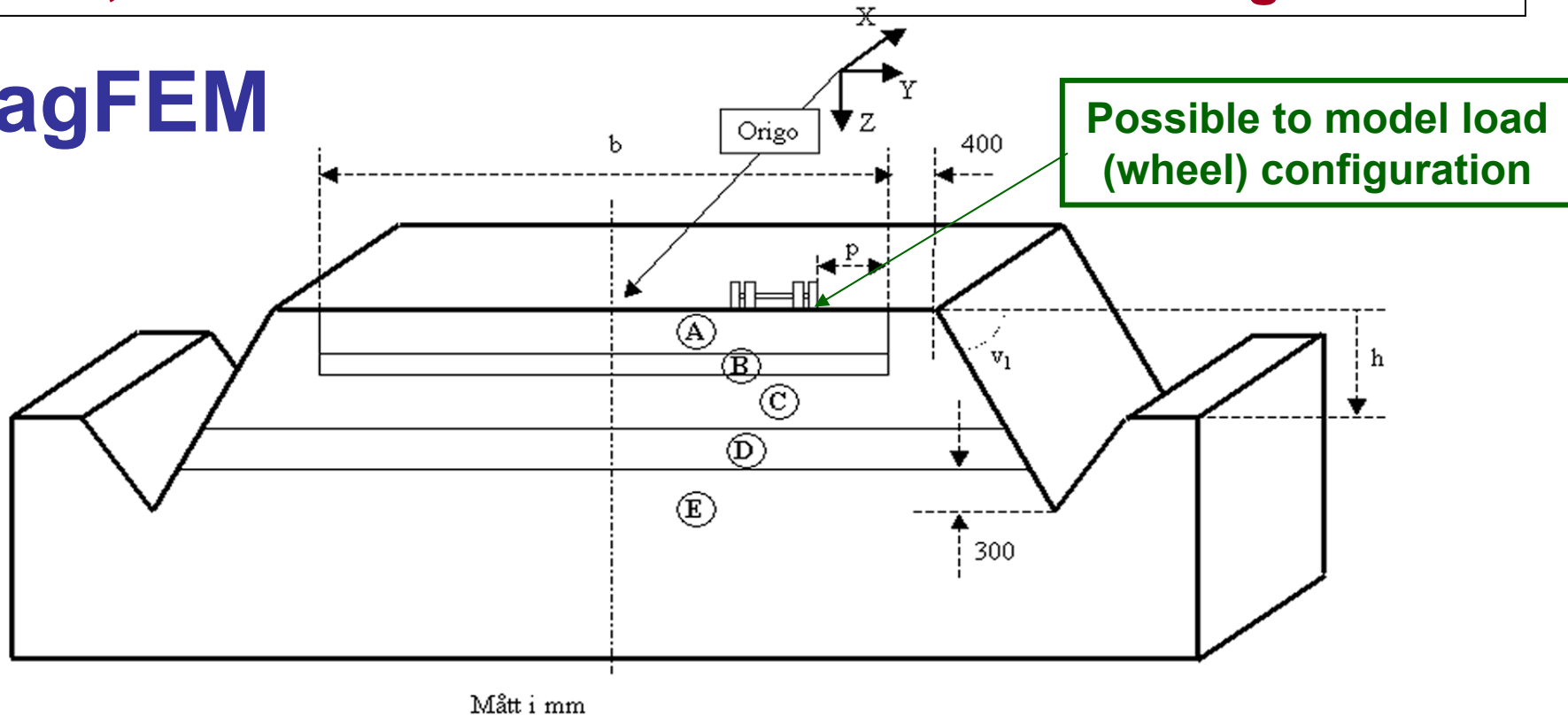
Why is it difficult to use Design Guide?

- It do not take the real material characteristics into consideration
- It makes separete calculations for each month during 20 years, which means at least 280 calculations. This takes a very long time to run in a computer

USER FRIENDLY PROGRAMS

VagFEM is a 3D finite element program, built on ABAQUS, and run in a large computer. The result is coming back as a PDF-file inside 20 minutes. The input data is very easy to handle, it could be done in 3 minutes on a working site.

VagFEM



Inre släntlutning

Höjd omgivande mark [mm]

SKIKT A

Typ

Tjocklek [mm]

SKIKT B

Typ

Tjocklek [mm]

SKIKT C

Typ

Tjocklek [mm]

SKIKT D

Typ

Tjocklek [mm]

SKIKT E

Typ

Lasthantering

Axellast

Däcktryck [kPa]

Placering [mm]

SKIKT A

Bundet linjärt

Tjocklek 110 [mm]

Densitet [kg/m³]Poissons tal [1]Elasticitetsmodul [MPa]**SKIKT B**

Asfaltsgrus linjärt

Tjocklek 130 [mm]

Densitet [kg/m³]Poissons tal [1]Elasticitetsmodul [MPa]**SKIKT C**

Obundet linjärt

Tjocklek 400 [mm]

Densitet [kg/m³]Poissons tal [1]Elasticitetsmodul [MPa]**SKIKT D**

Inget

Tjocklek 0 [mm]

SKIKT E

Obundet linjärt

Densitet [kg/m³]Poissons tal [1]Elasticitetsmodul [MPa]Komplett resultatfil ☐Generera fil för permanent deformation ☐

Fortsätt till nästa steg

Återställ

Hjälp

Starta beräkningen

Tillbaka till föregående steg

Hjälp

Projekt

Namn på beräkningen

SKIKT C

Typ

Tjocklek [mm]

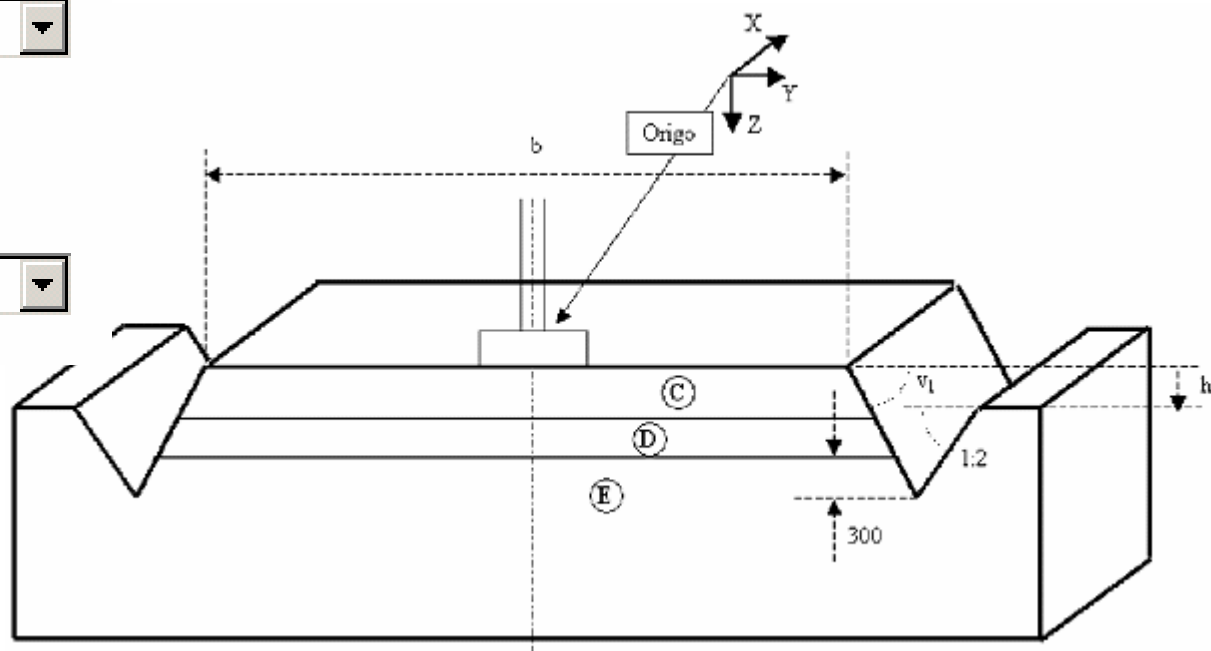
SKIKT D

Typ

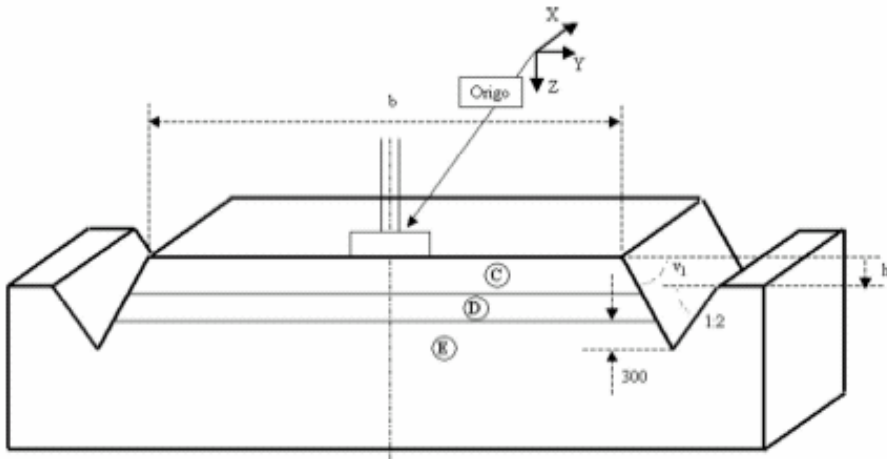
Tjocklek [mm]

SKIKT E

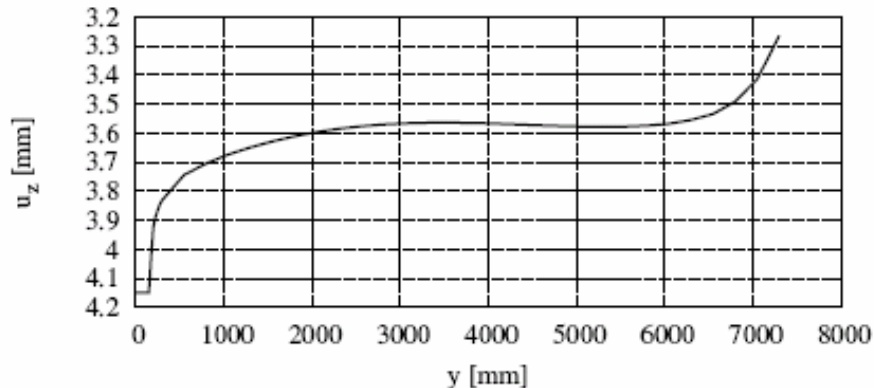
Typ



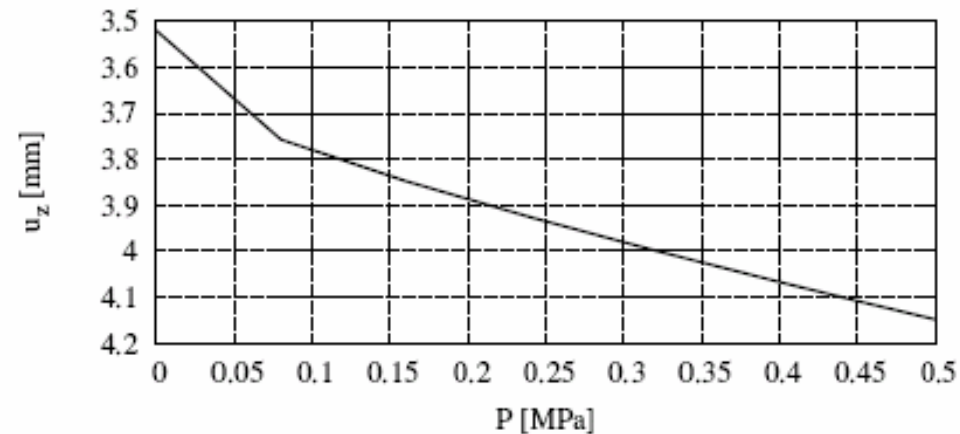
VagFEM – Plate Loading – Resilient modulus



Geometry for plate loading test



Deflection beside the plate at full load (compare FWD)

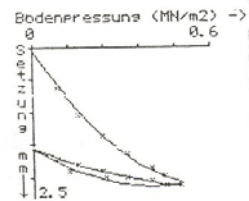


Deflection under the plate at various load steps

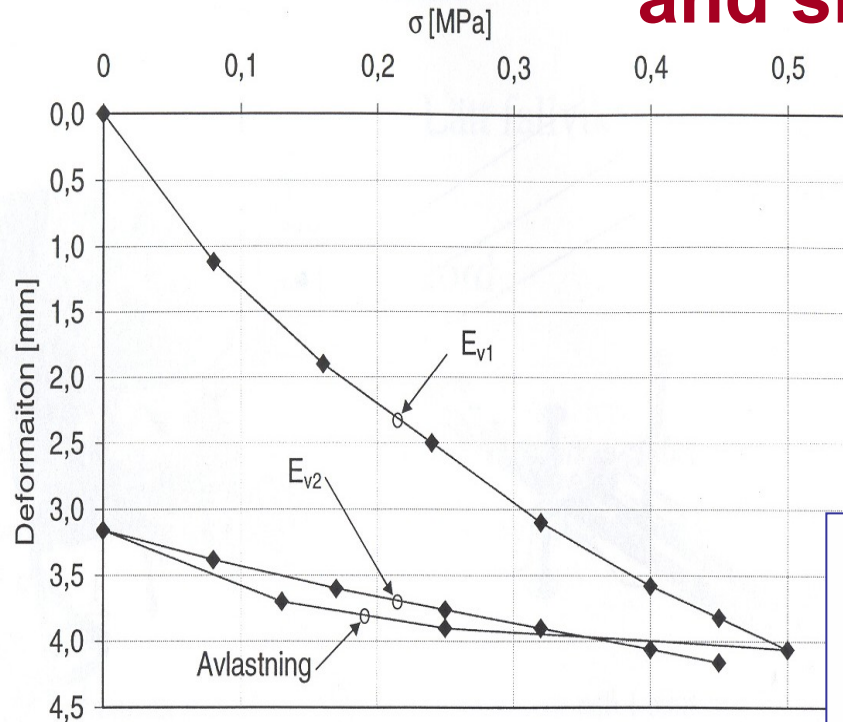
Test: Plate loading

Result from Plate loading and simulation in VagFEM

PLATTENDRUCKVERSUCH nach DIN 18134	
Projekt: HEBERG/LANGAS	
Meßstelle: 022/003 U10.2 T26	
Datum: 09.08.91 10:54	
Plattendurchm.: 300 mm	
Laensenverh.: 1:2.0	
Normal- span- nung	Setzung
MN/m2	0.01 mm
*** Belastung ***	
0.08	721
0.16	1141
0.24	1461
0.32	1751
0.40	1981
0.45	2121
0.50	2271
*** Entlastung ***	
0.25	2151
0.13	2031
0.08	1651
*** Belastung ***	
0.08	1831
0.16	1941
0.24	2021
0.32	2151
0.40	2211
0.45	2281

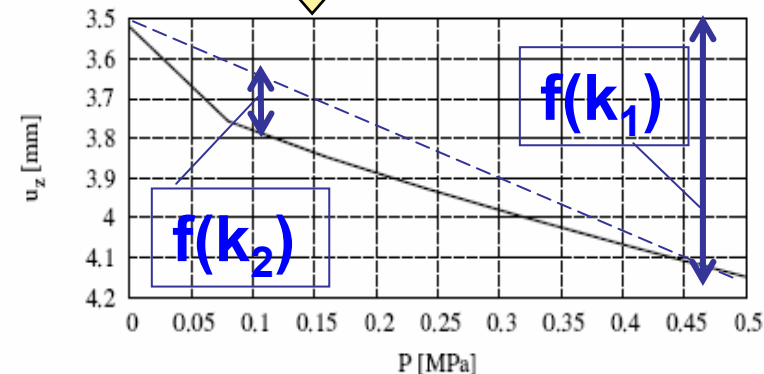


Ergebnisse: neue DIN		
Kurve	a1	a2
1	5.87	-3.85
2	1.45	-0.46
Ev1	= 57.00 MN/m2	
Ev2	= 184.44 MN/m2	
Ev2/Ev1	= 3.24	



Resilient Module

$$Mr = k_1 \Theta^{k_2}$$

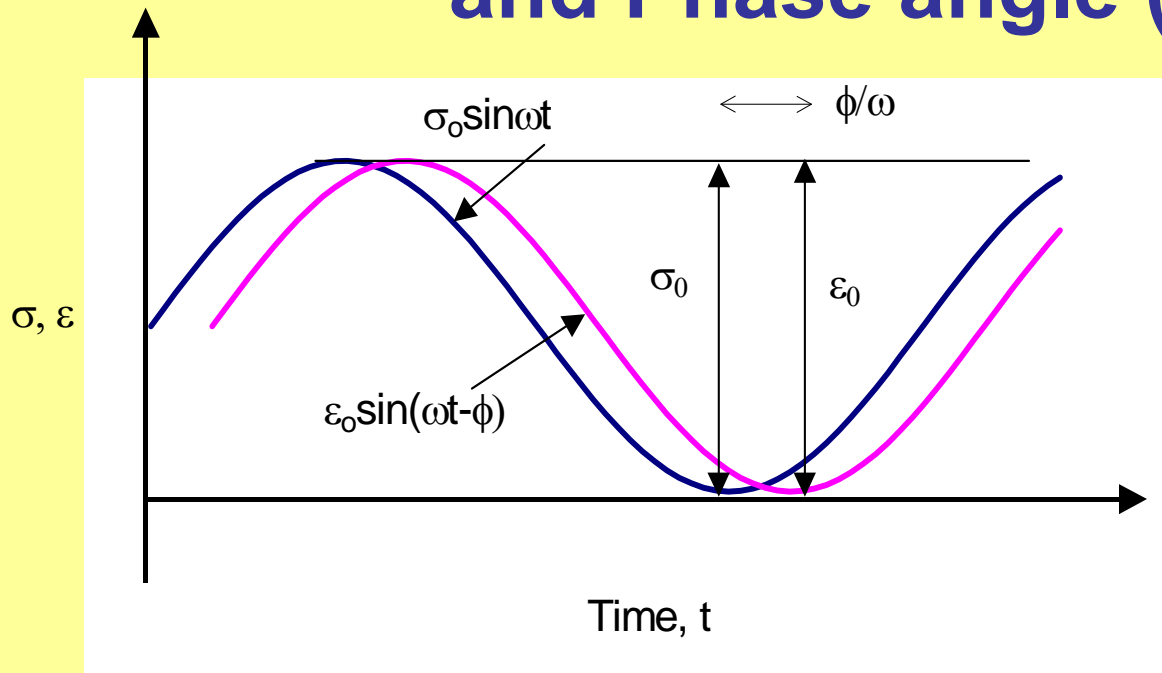


Measured Mr_1 in subgrade is used as input data in calculation of Mr_2 in subbase

TEST METHODS

bituminous bound layers

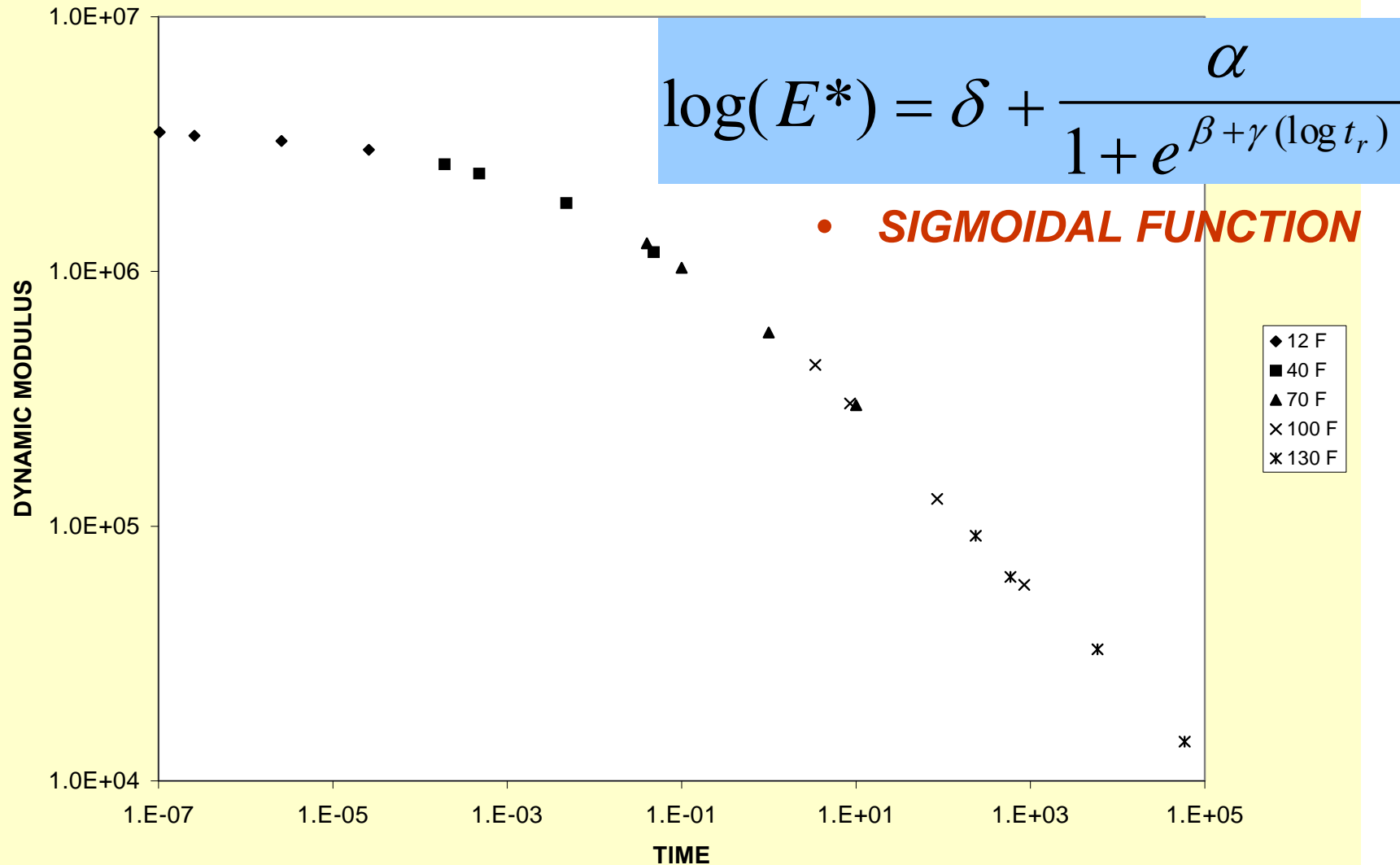
Compressive Dynamic Modulus ($|E^*|$) and Phase angle (ϕ)



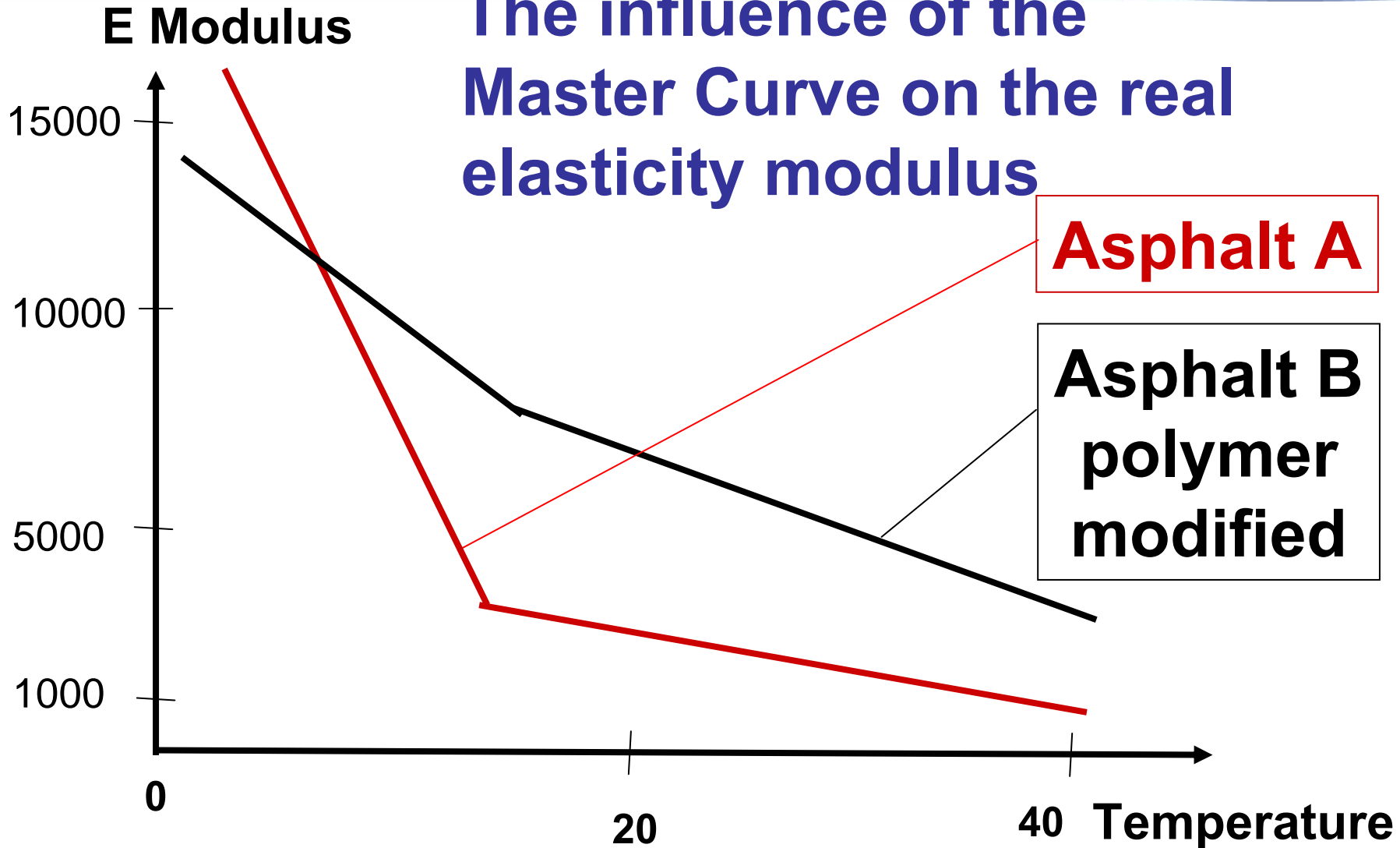
$$|E^*| = \frac{\sigma_0}{\epsilon_0}$$

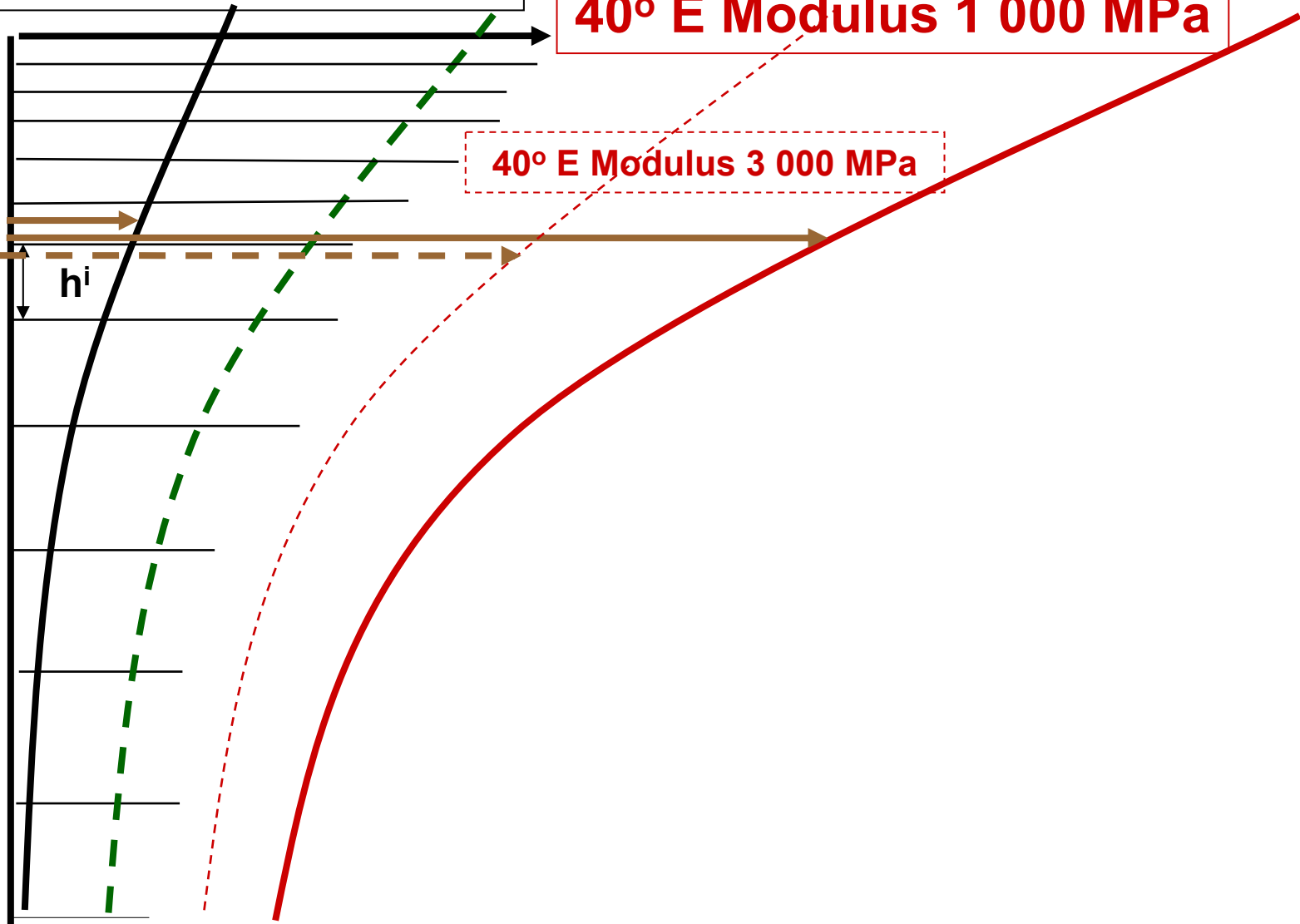
$$\phi = \omega t_i$$

Dynamic Modulus Master Curve



The influence of the Master Curve on the real elasticity modulus

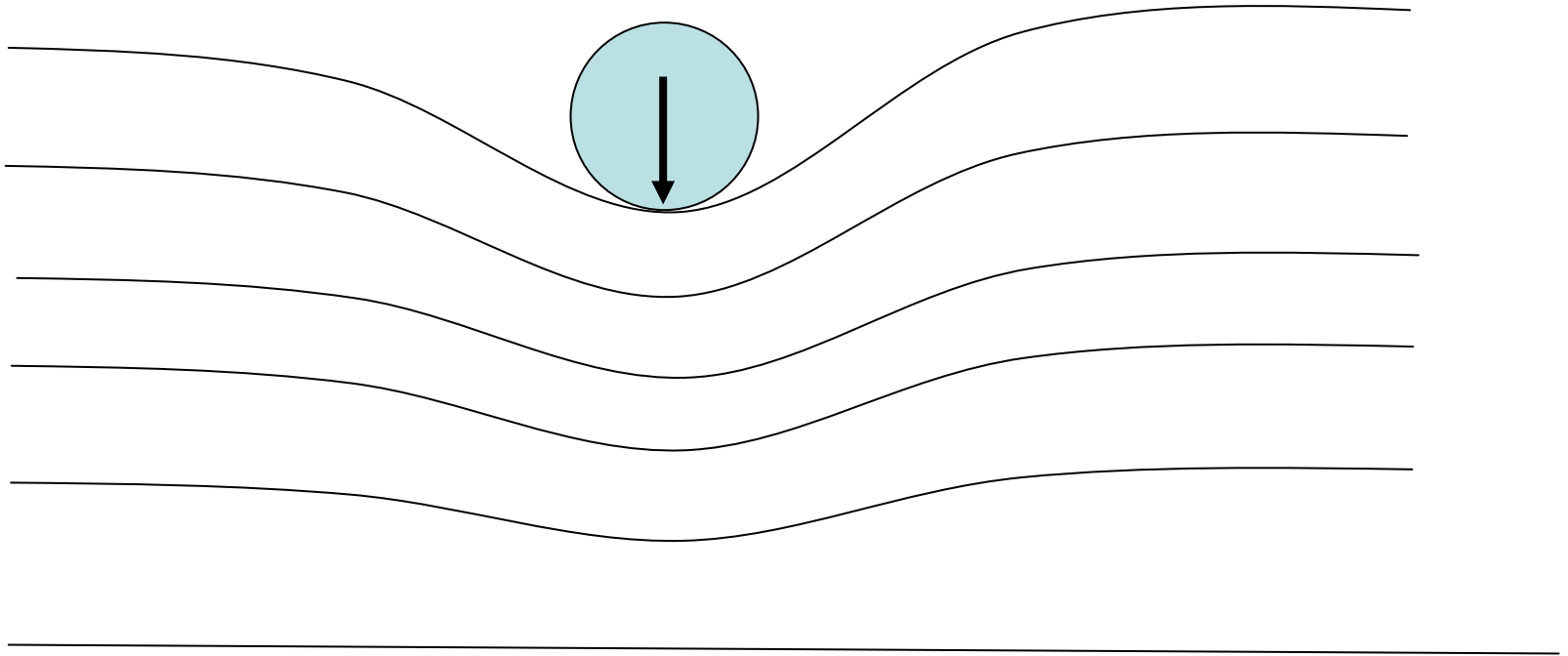


5° E Modulus 15 000 MPa**40° E Modulus 1 000 MPa****40° E Modulus 3 000 MPa****Asfalt****Obundna
Lager**

Calculation of rutting

Elastic deflection from a heavy vehicle

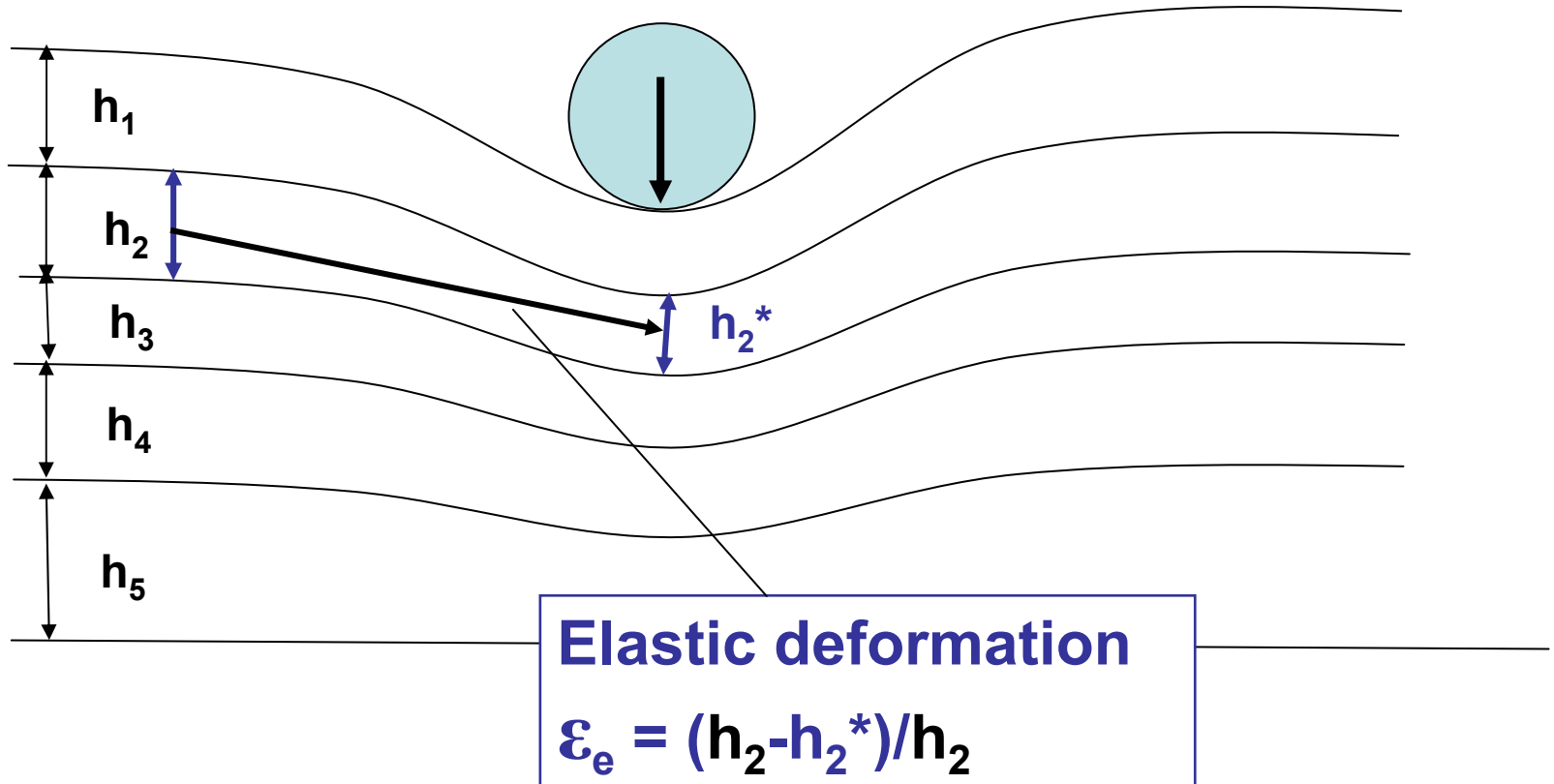
Elastic deflection from a heavy vehicle



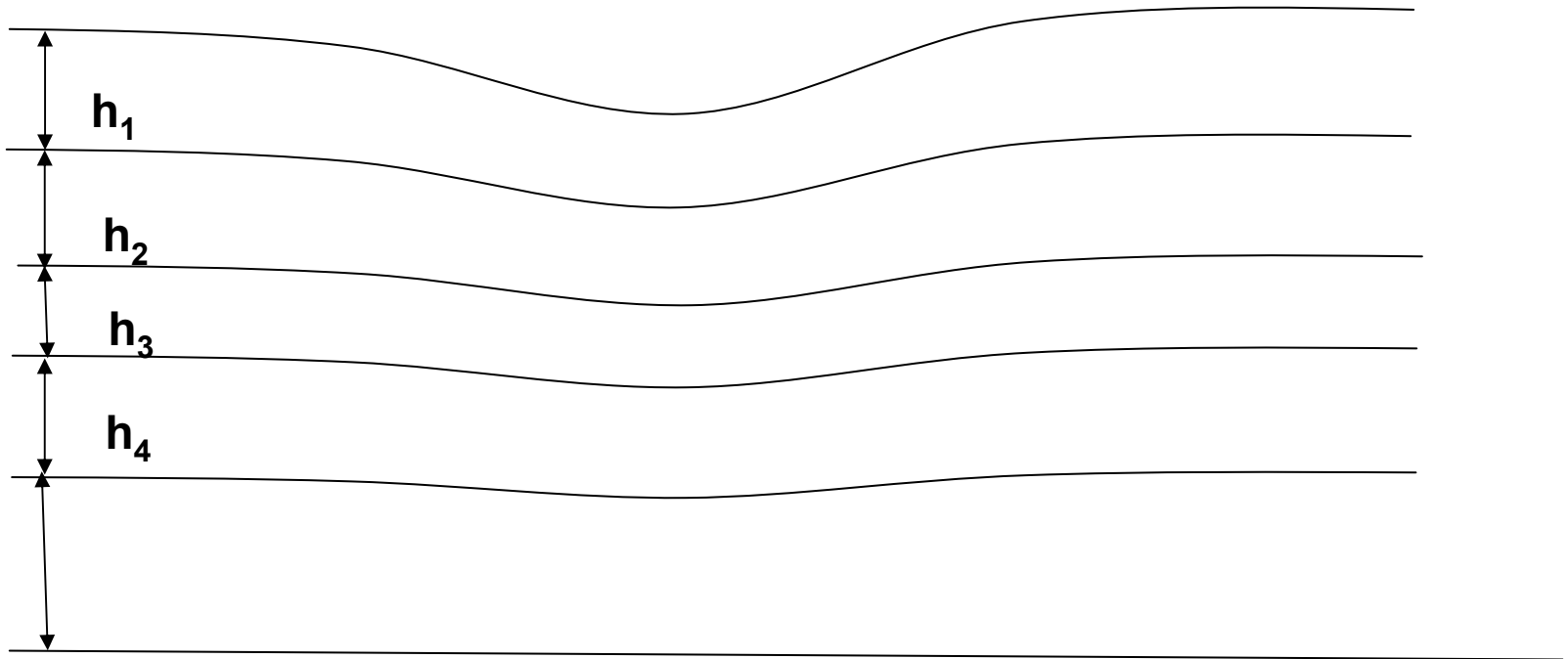
Elastic deflection from a heavy vehicle



Elastic deflection from a heavy vehicle

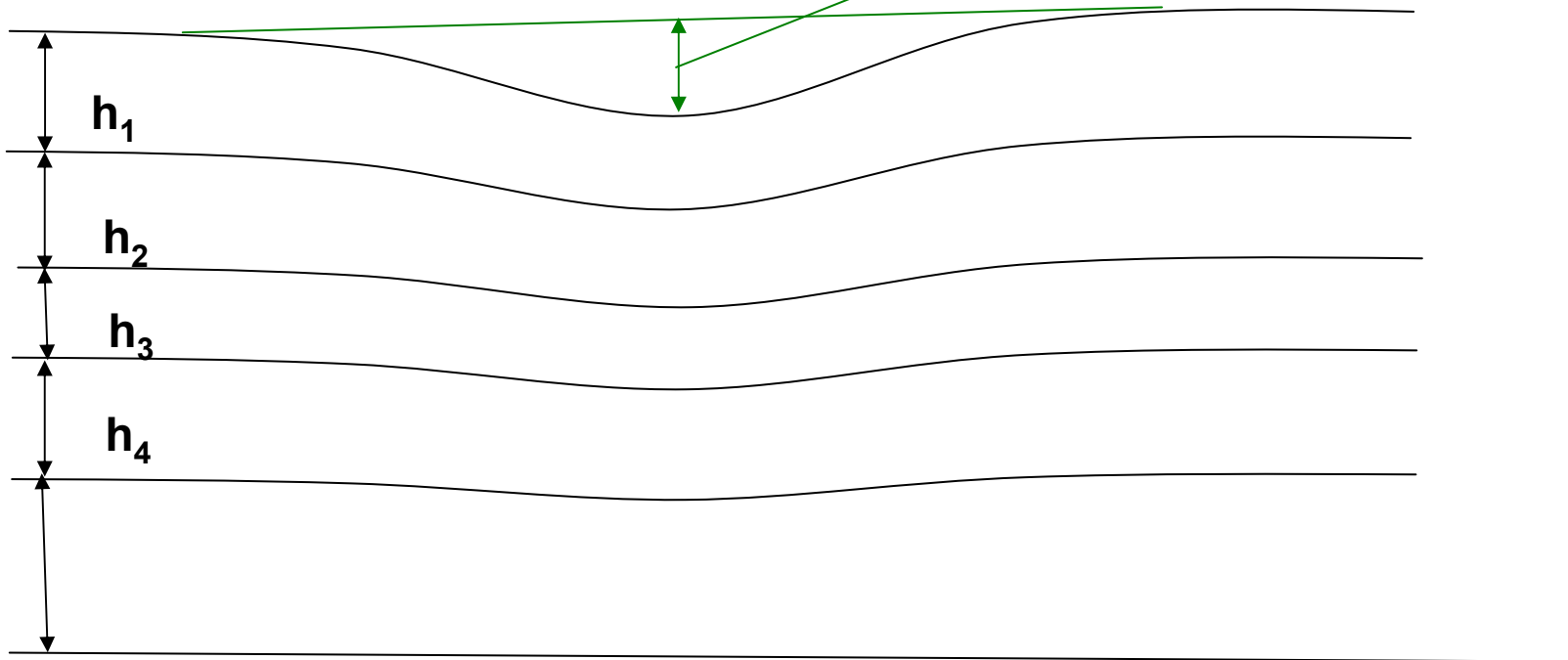


Permanent rutting from heavy vehicle

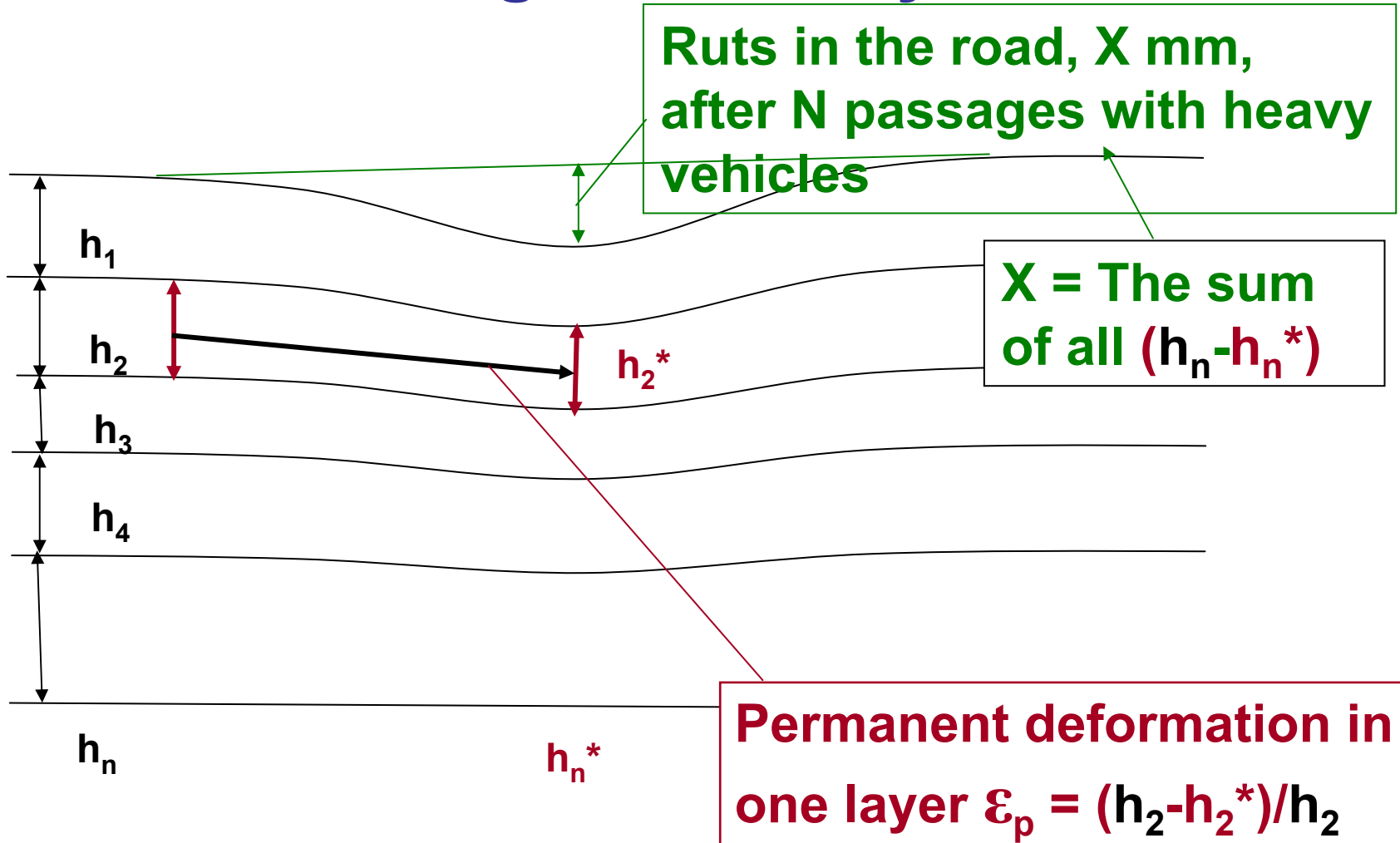


Permanent rutting from heavy vehicle

Ruts in the road after N passages with heavy vehicle



Permanent rutting from heavy vehicle



Triaxial test

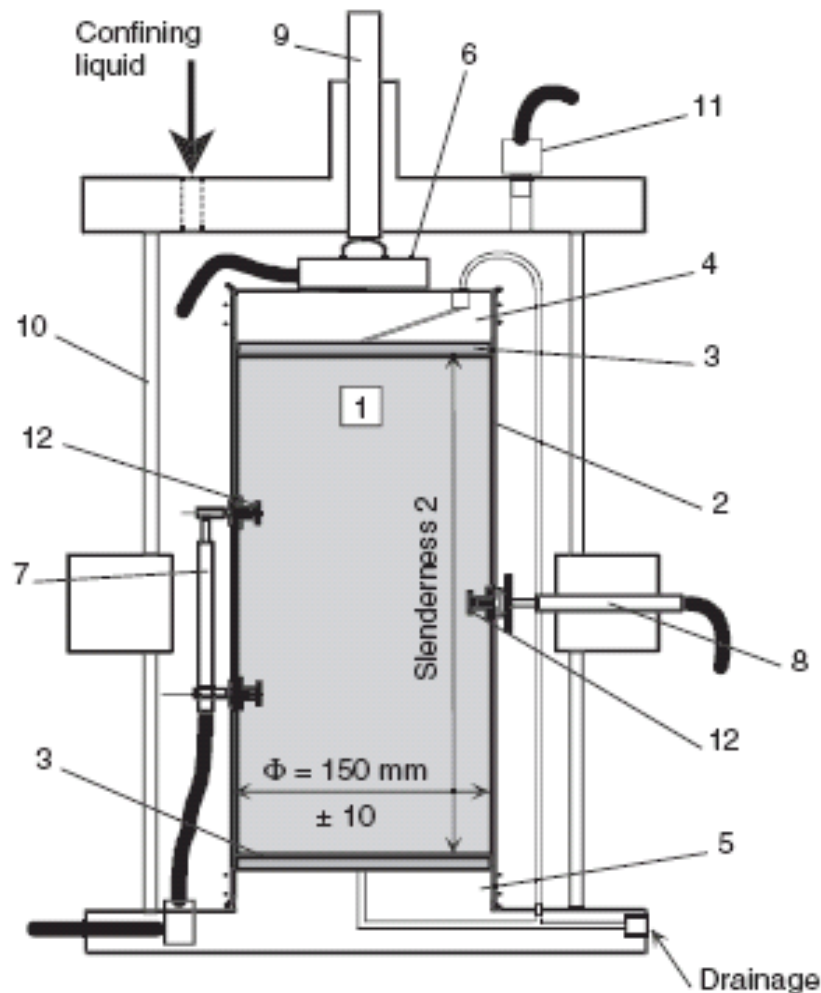


Fig. 1 - The triaxial cell of the repeated load triaxial apparatus.

1. Specimen.
2. Membrane.
3. Porous disc.
4. Cell top.
5. Base.
6. Force sensor.
7. Axial strain measurement device.
8. Radial strain measurement device.
9. Loading ram.
10. Triaxial cell casing.
11. Pressure sensor.
12. Displacement transducer fixings.

Cyclic loadings

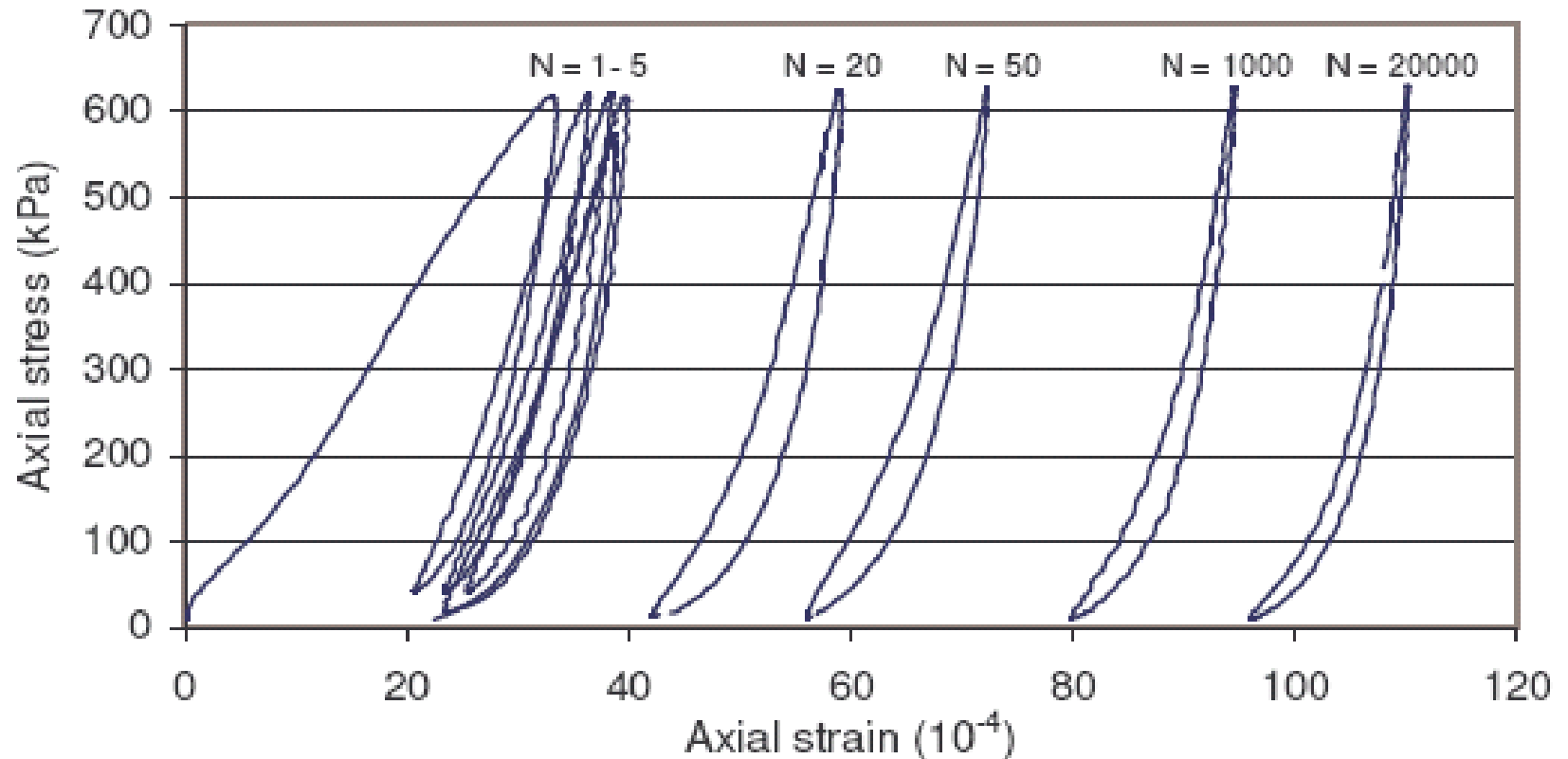
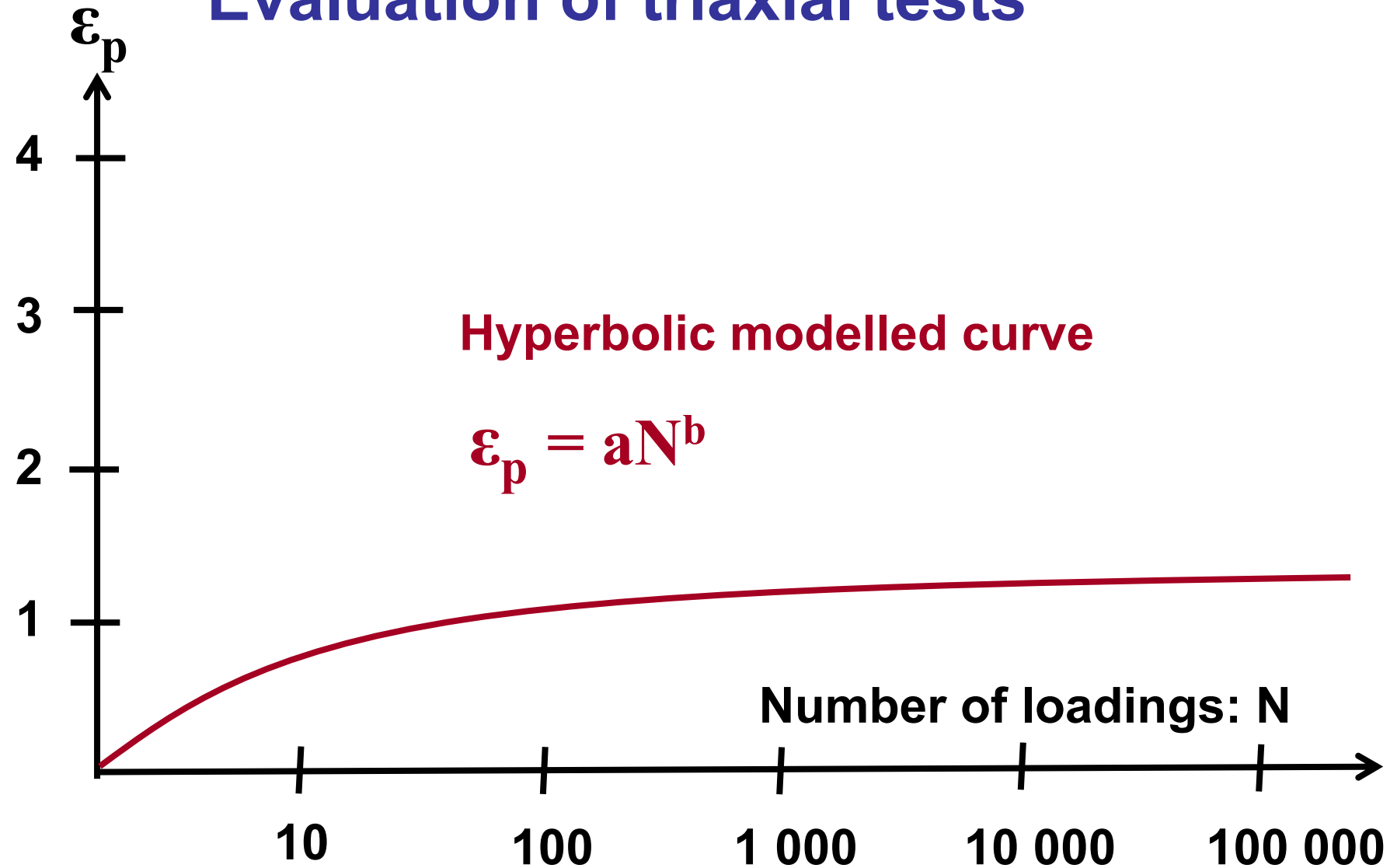


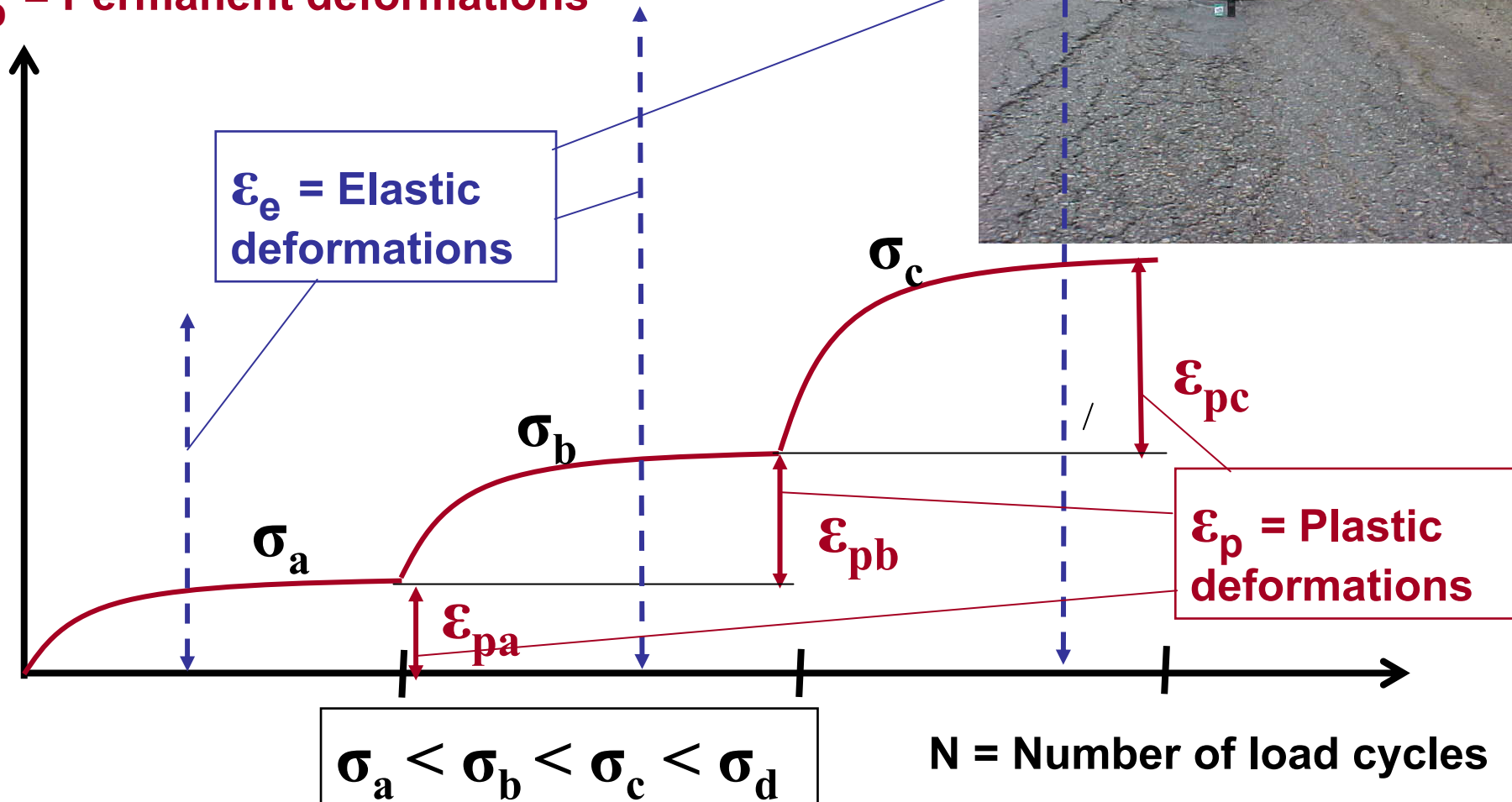
Figure 1. Axial stress – axial strain cycles obtained in a cyclic triaxial test on a UGM.

Evaluation of triaxial tests

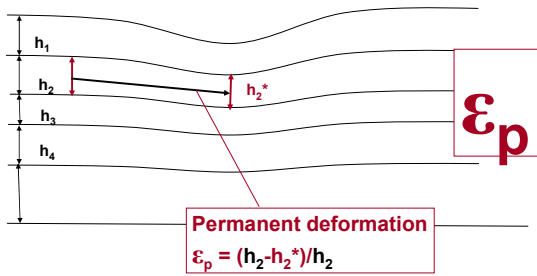


Triaxial test – Real ruts

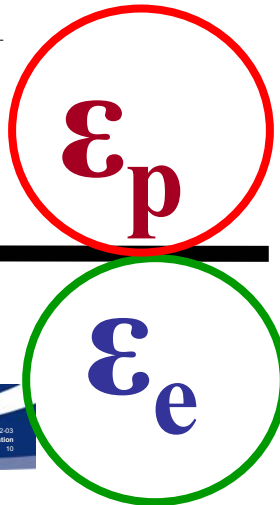
ϵ_p = Permanent deformations



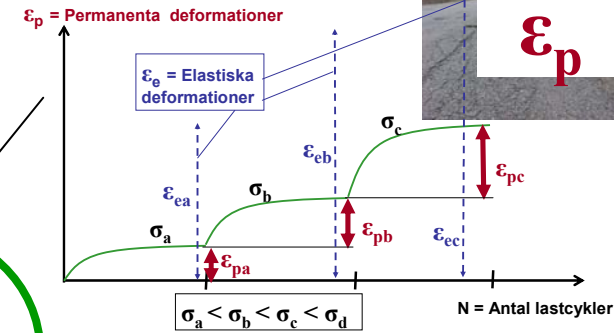
Permanent spårbildning av tunga fordon



Real ruts

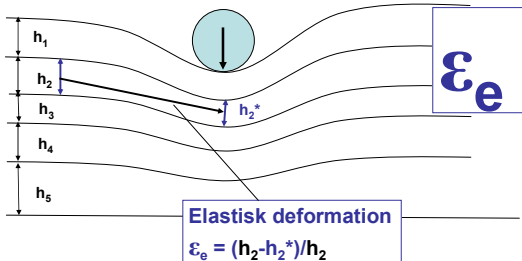


Treaxial test – Verkliga spår



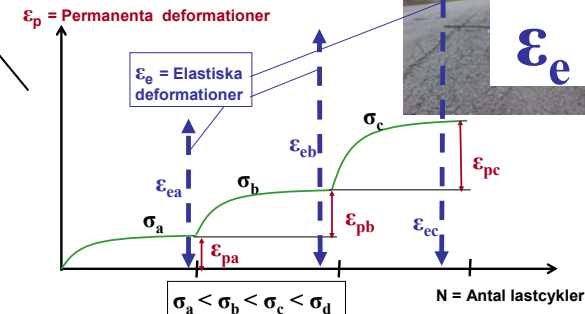
Triaxial test

Elastisk nedböjning av tungt fordon



VagFEM

Treaxial test – Verkliga spår



MATERIAL MODELS

Rutting in unbound materials

Dresden

Plastic Model

Plastic DRESDEN-Model

$$\varepsilon_p(N) = A \cdot \left(\frac{N}{1000} \right)^B + C \left(e^{D \frac{N}{1000}} - 1 \right)$$

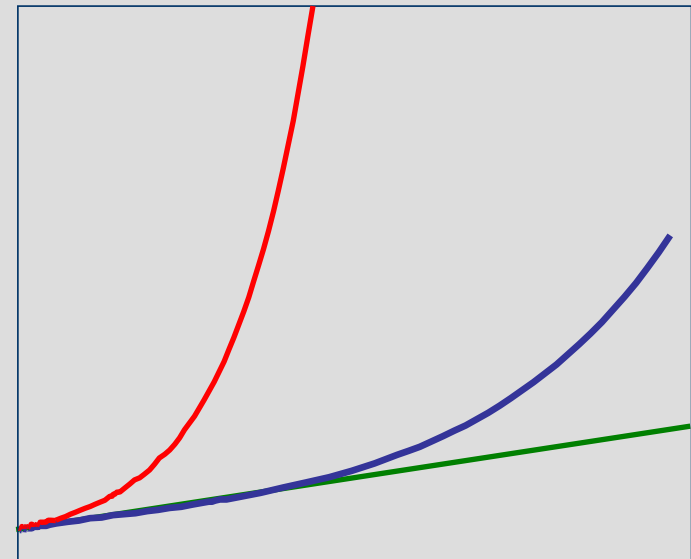
Stable behaviour
Range A

Collapse

Range B and C

$A, B, C, D = f(\sigma_1 \text{ and } \sigma_3)$

Permanent strains $\log(\varepsilon_p)$



Load cycles $\log(N)$

(HUURMAN 1997)

Prof Frohmüt Wellner
Sabine Werkmeister

MATERIAL MODELS

Rutting in unbound materials

SAMARIS

Calculation of permanent deformations – LCPC

$$\varepsilon_1^p(N) = \varepsilon_{10}^p \cdot \left[1 - \left(\frac{N}{N_0} \right)^{-B} \right] \cdot \left[\frac{L_{\max}}{p_a} \right]^n \cdot \frac{1}{\left(m + \frac{s}{p_{\max}} - \frac{q_{\max}}{p_{\max}} \right)}$$

ε_1^p : permanent axial strain; N : number of load cycles;

p_{\max} , q_{\max} : maximum values of the mean normal stress p and deviatoric stress q ;

$$L_{\max} = \sqrt{p_{\max}^2 + q_{\max}^2}$$

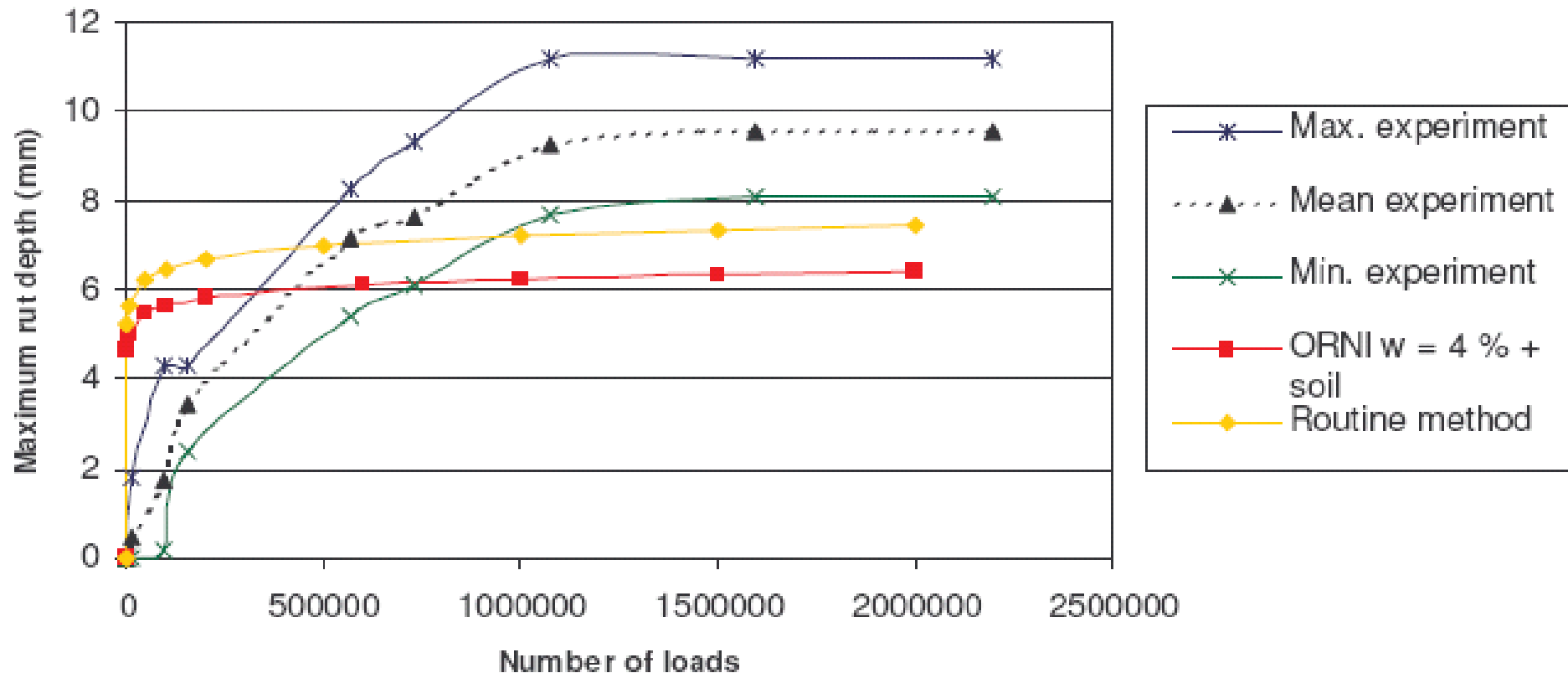
p_a : reference pressure equal to 100 kPa;

ε_1^{p0} , B , n model parameters;

m, s parameters of the failure line of the material, of equation $q = m \cdot p + s$;
(from experience, $m=2.5$ to 2.6 and $s=20$ kPa)

Samaris

Result: Prediction of permanent deformation, rutting



MATERIAL MODELS

Rutting in unbound materials

Design Guide

Theoretical background

**Original model for calculation
of permanent deformations,
Tseng and Lytton**

$$\delta_a(N) = \beta_{GB} \left(\frac{\varepsilon_0}{\varepsilon_r} \right) e^{-\left(\frac{\rho}{N} \right)^\beta} \varepsilon_v h$$

**Problems with some strange results
made that the choice in Design Guide is
a more empirical and statistical model**

Modeling permanent deformation – Unbound material

modified models for $\varepsilon_0/\varepsilon_r$, β and ρ developed in NCHRP Project 1-37A for granular and subgrade materials

Granular

$$\log\left(\frac{\varepsilon_0}{\varepsilon_r}\right) = 0.80978 - 0.06626 \cdot W_c - 0.003077 \cdot \sigma_\theta + 0.000003 \cdot E_r$$

$$\log(\beta) = -0.9190 + 0.03105 \cdot W_c + 0.001806 \cdot \sigma_\theta - 0.0000015 \cdot E_r$$

$$\log(\rho) = -1.78667 + 1.45062 \cdot W_c + 0.0003784 \cdot \sigma_\theta^2 - 0.002074 \cdot W_c^2 \sigma_\theta - 0.0000105 \cdot E_r$$

Subgrade

$$\log\left(\frac{\varepsilon_0}{\varepsilon_r}\right) = -1.69867 + 0.09121 \cdot W_c - 0.11921 \cdot \sigma_d + 0.91219 \cdot \log E_r$$

$$\log(\beta) = -0.9730 - 0.0000278 \cdot W_c^2 \sigma_d + 0.017165 \cdot \sigma_d - 0.0000338 \cdot W_c^2 \sigma_\theta$$

$$\log(\rho) = 11.009 + 0.00068 \cdot W_c^2 \sigma_d - 0.40260 \cdot \sigma_d + 0.0000545 \cdot W_c^2 \sigma_\theta$$

MATERIAL MODELS

Rutting in bituminous bound materials

Design Guide

Modeling permanent deformation

Asphalt layer – Design Guide

$$\frac{\varepsilon_p}{\varepsilon_r} = a_1 \cdot N^{a_2} \cdot T^{a_3}$$

**Choose a_1 , a_2 and a_3
with help of results
from triaxial test**

- ε_p – Accumulated plastic strain at N repetitions of load
- ε_r – Resilient strain of the asphalt material
- N – Number of load repetitions
- T – Temperature (10°C)
- a_i – Non-linear regression coefficients (from NCHRP 1-37A)

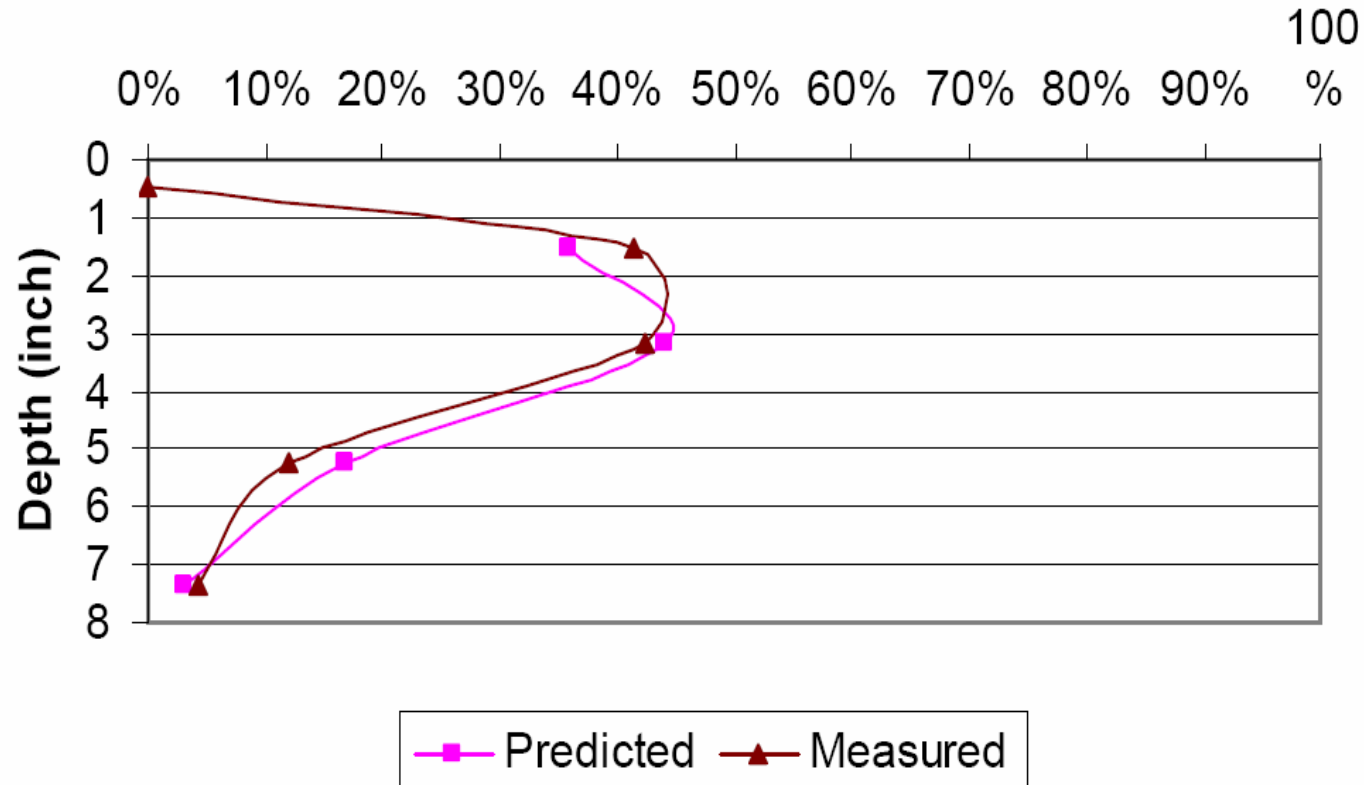
MEPDG – Calibration to Mnroad

$$C_1 = -0.1039 * h_{ac}^2 + 2.4868 * h_{ac} - 17.342$$

$$k_1 = (C_1 + C_2 * depth) * 0.328196^{depth}$$

$$C_2 = 0.0172 * h_{ac}^2 - 1.7331 * h_{ac} + 27.428$$

Average % AC Rutting with Depth



Test methods!

- **It is important that the test methods is synchronized to the design models.**
- **It must be possible to use results from the test methods as input data in the design models.**

We can predict future performance today

- **Rutting!**
- **Unevenness: MMOPP in Denmark**
- **Cracks? (Tensile strength and fatigue)**

Why don't we do that?

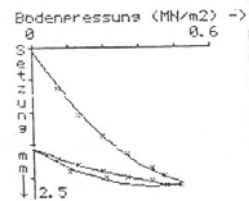
Calculations in practice

- Possible to use actual knowledge and technique: Complete with new Excel programs
- Use the technique of today, and improve it
- Help for understanding – education
- Help for implementation of new technique

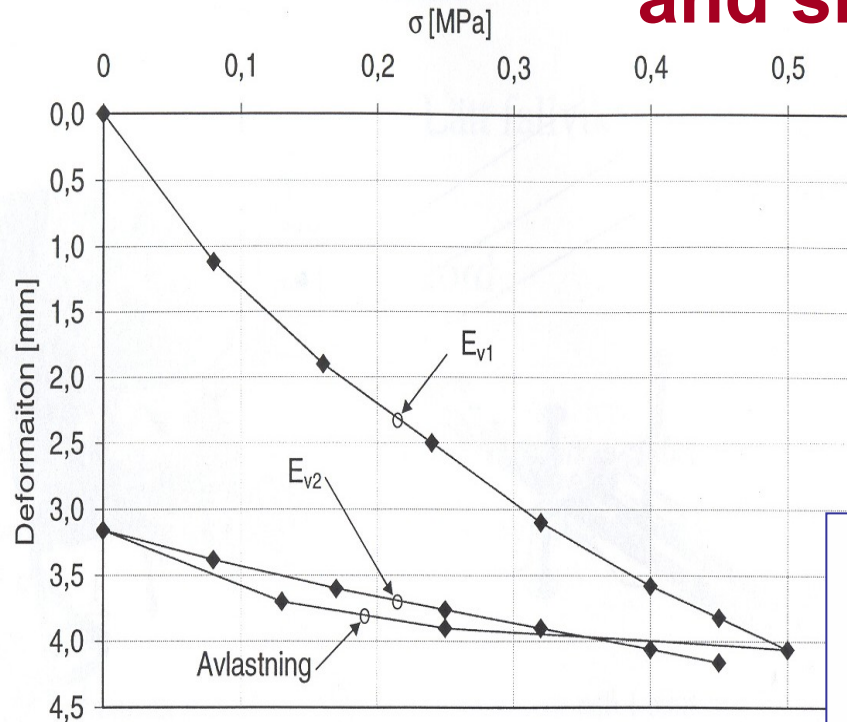
Test: Plate loading

Result from Plate loading and simulation in VagFEM

PLATTENDRUCKVERSUCH nach DIN 18134	
Projekt: HEBERG/LANGAS	
Meßstelle: 022/003 U10.2 T26	
Datum: 09.08.91 10:54	
Plattendurchm.: 300 mm	
Laensenverh.: 1:2.0	
Normal- span- nung	Setzung
MN/m2	0.01 mm
*** Belastung ***	
0.08	721
0.16	1141
0.24	1461
0.32	1751
0.40	1981
0.45	2121
0.50	2271
*** Entlastung ***	
0.25	2151
0.13	2031
0.08	1651
*** Belastung ***	
0.08	1831
0.16	1941
0.24	2021
0.32	2151
0.40	2211
0.45	2281

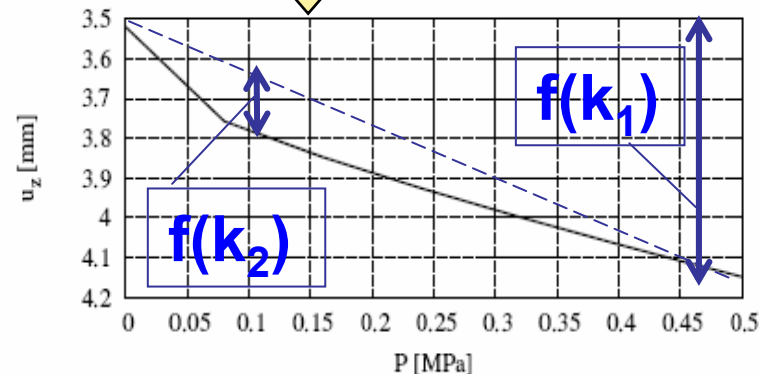


Ergebnisse: neue DIN		
Kurve	a1	a2
1	5.87	-3.85
2	1.45	-0.46
Ev1	= 57.00 MN/m2	
Ev2	= 184.44 MN/m2	
Ev2/Ev1	= 3.24	



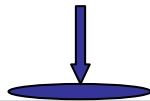
Resilient Module

$$Mr = k_1 \Theta^{k_2}$$



Measured Mr_1 in subgrade is used as input data in calculation of Mr_2 in base material

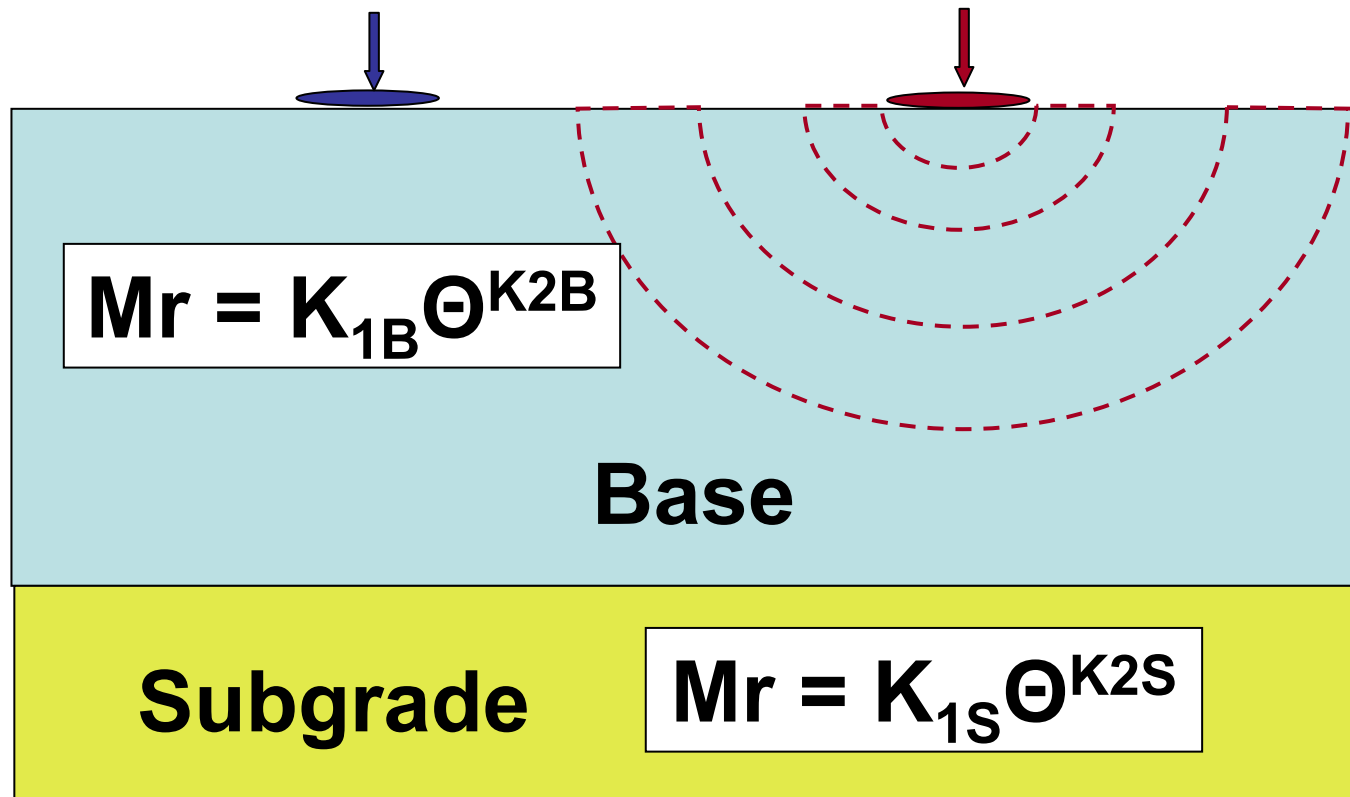
Calculate the resilient modulus in the subgrade material?



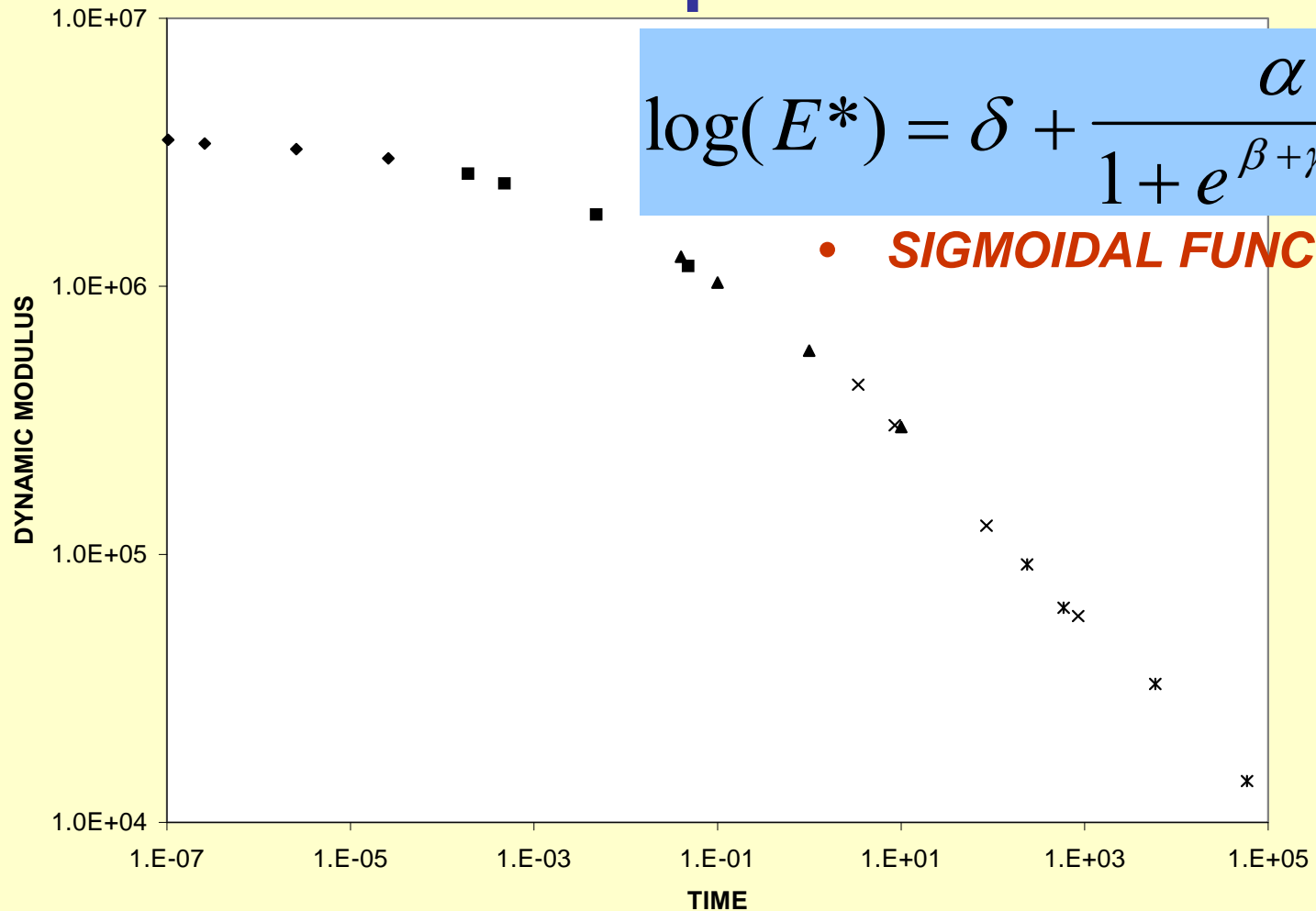
Subgrade

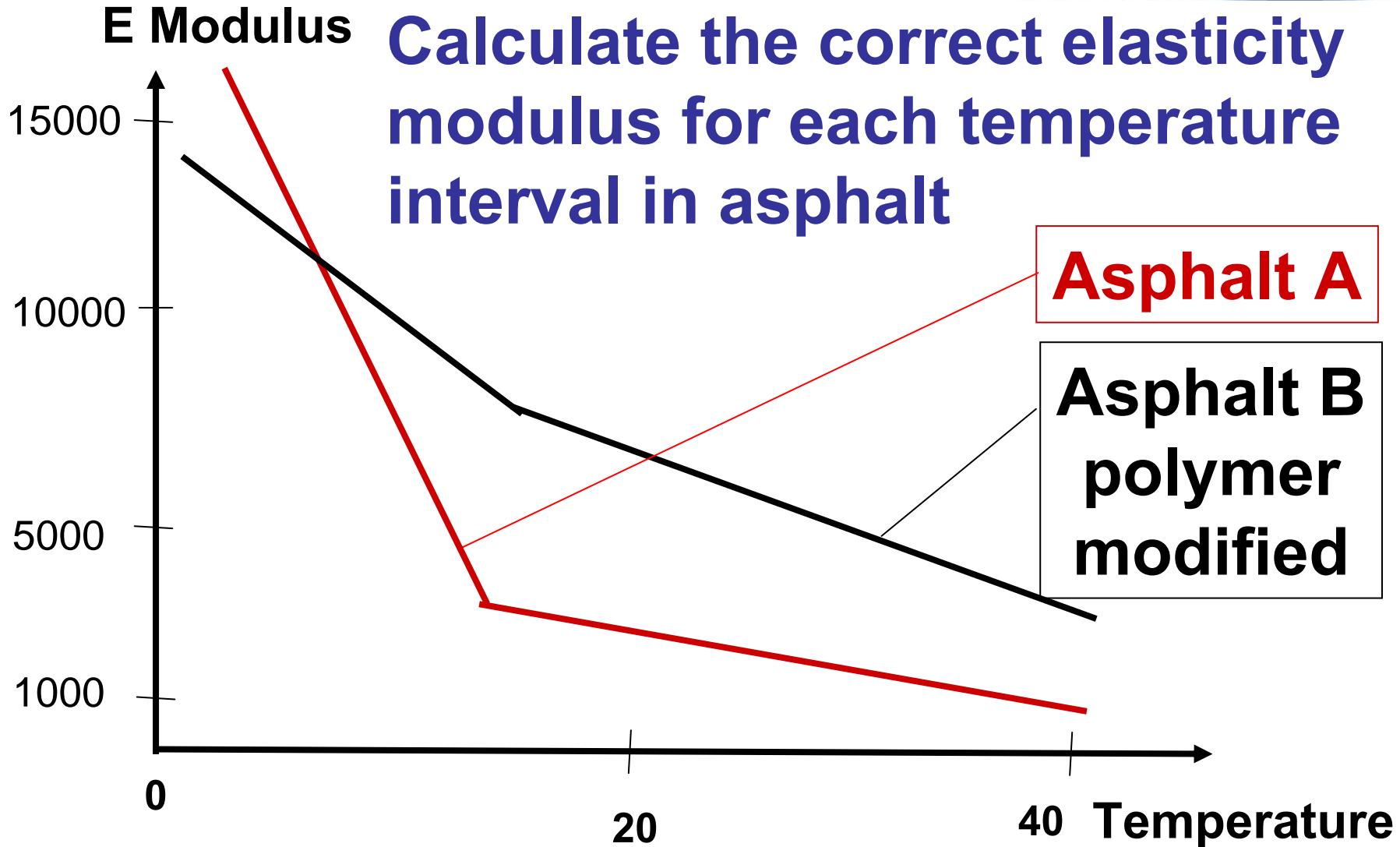
$$M_r = K_{1s} \Theta^{K2s}$$

Calculate the resilient modulus in the base material?



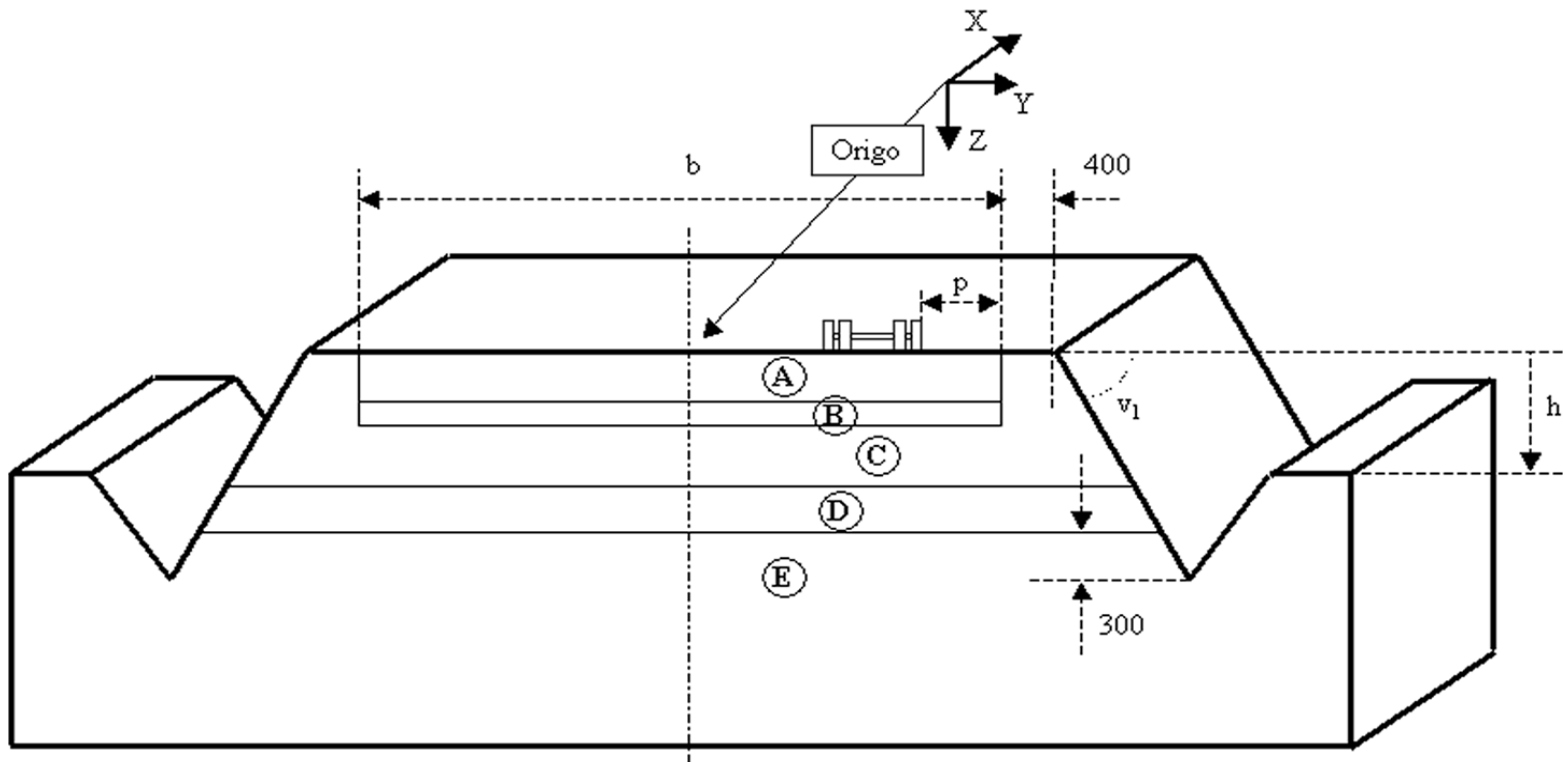
Calculate the Dynamic Modulus Master Curve in Asphalt



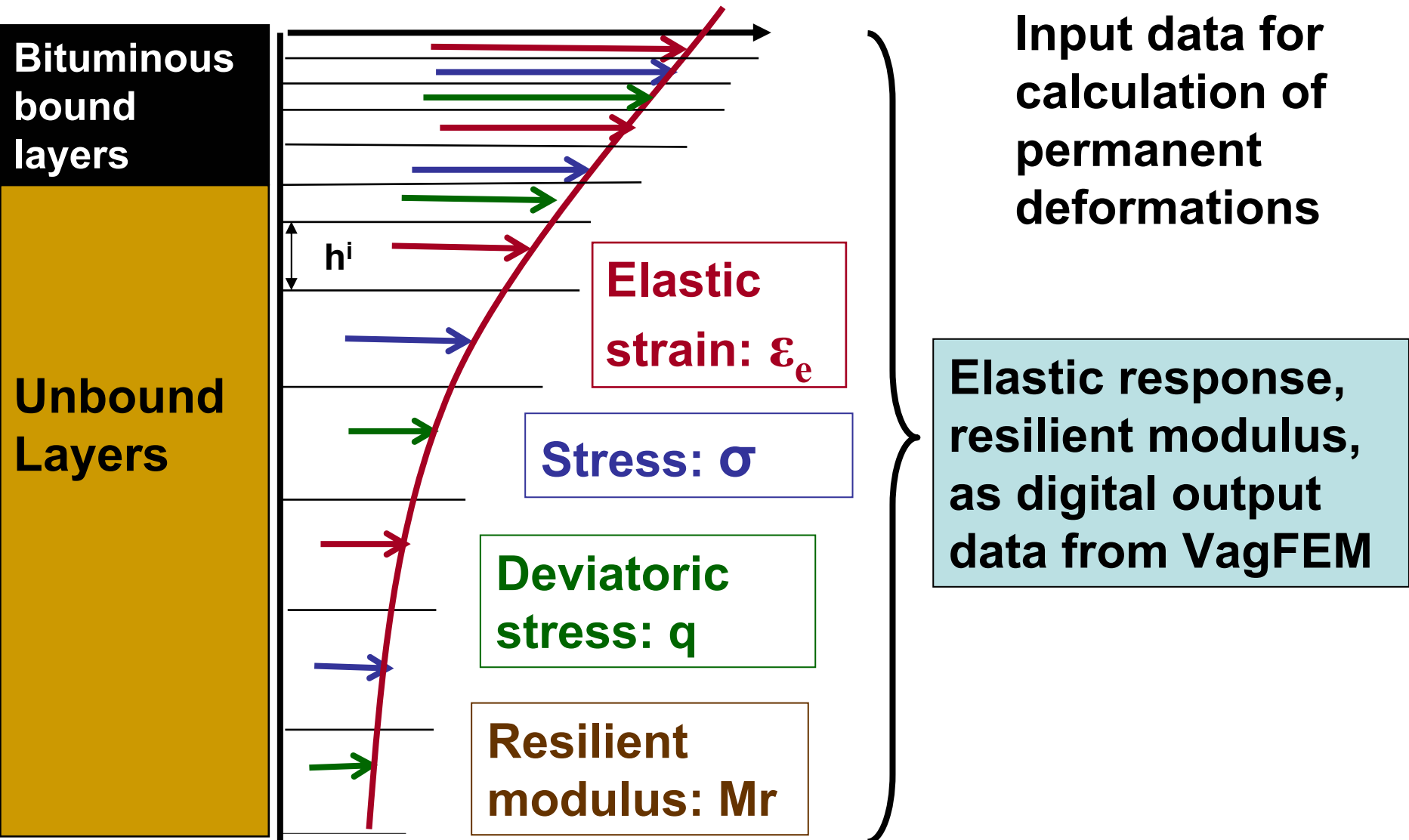


VagFEM

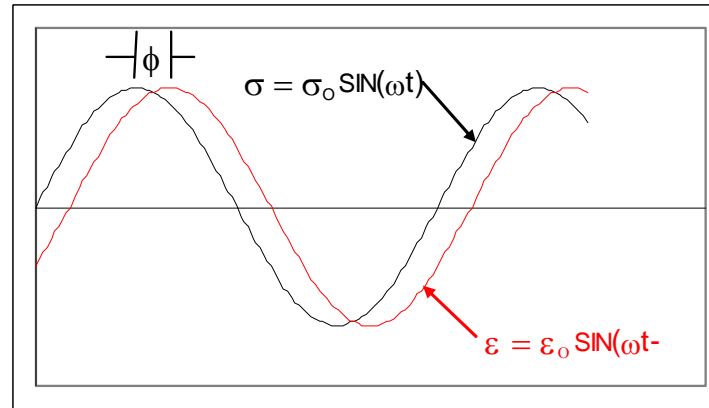
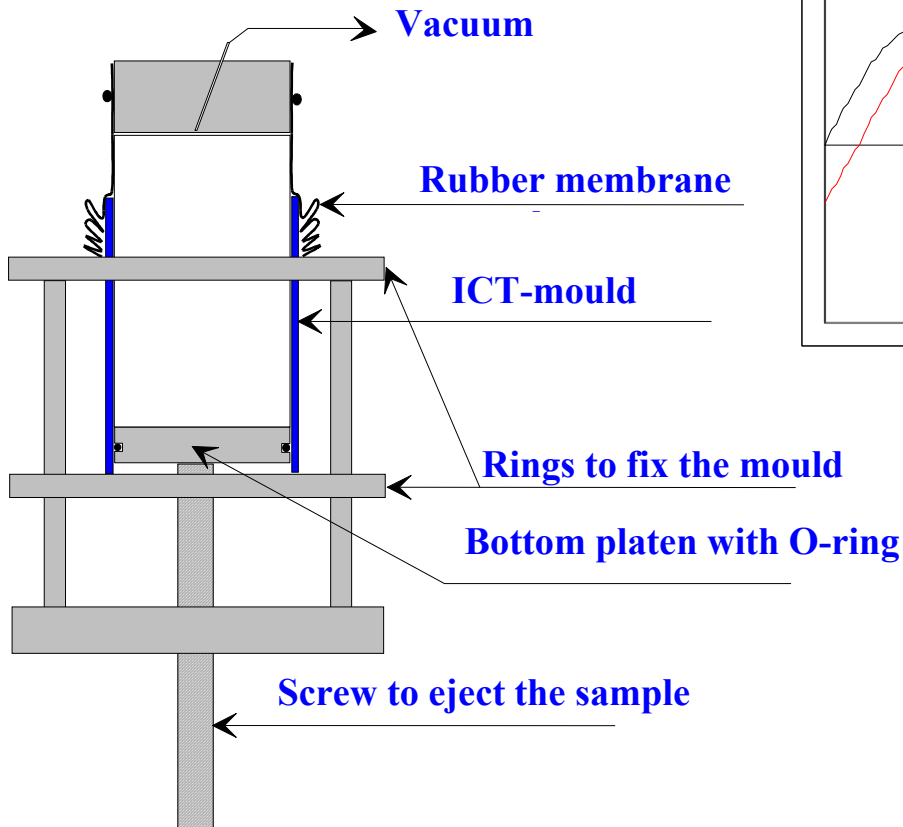
Calculate stress, strain and resilient modulus with VagFEM



Mått i mm

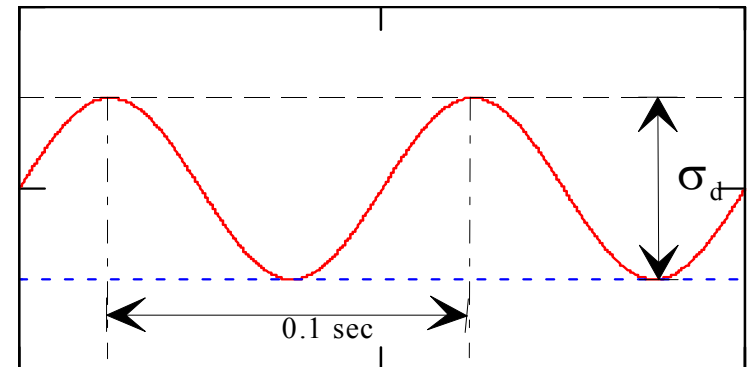
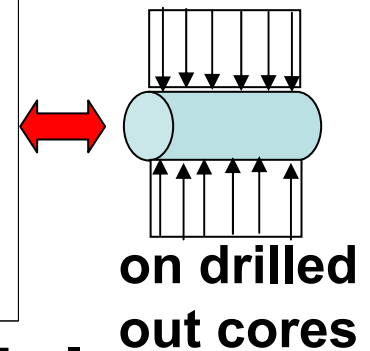


Calculation of parameters from triaxial tests



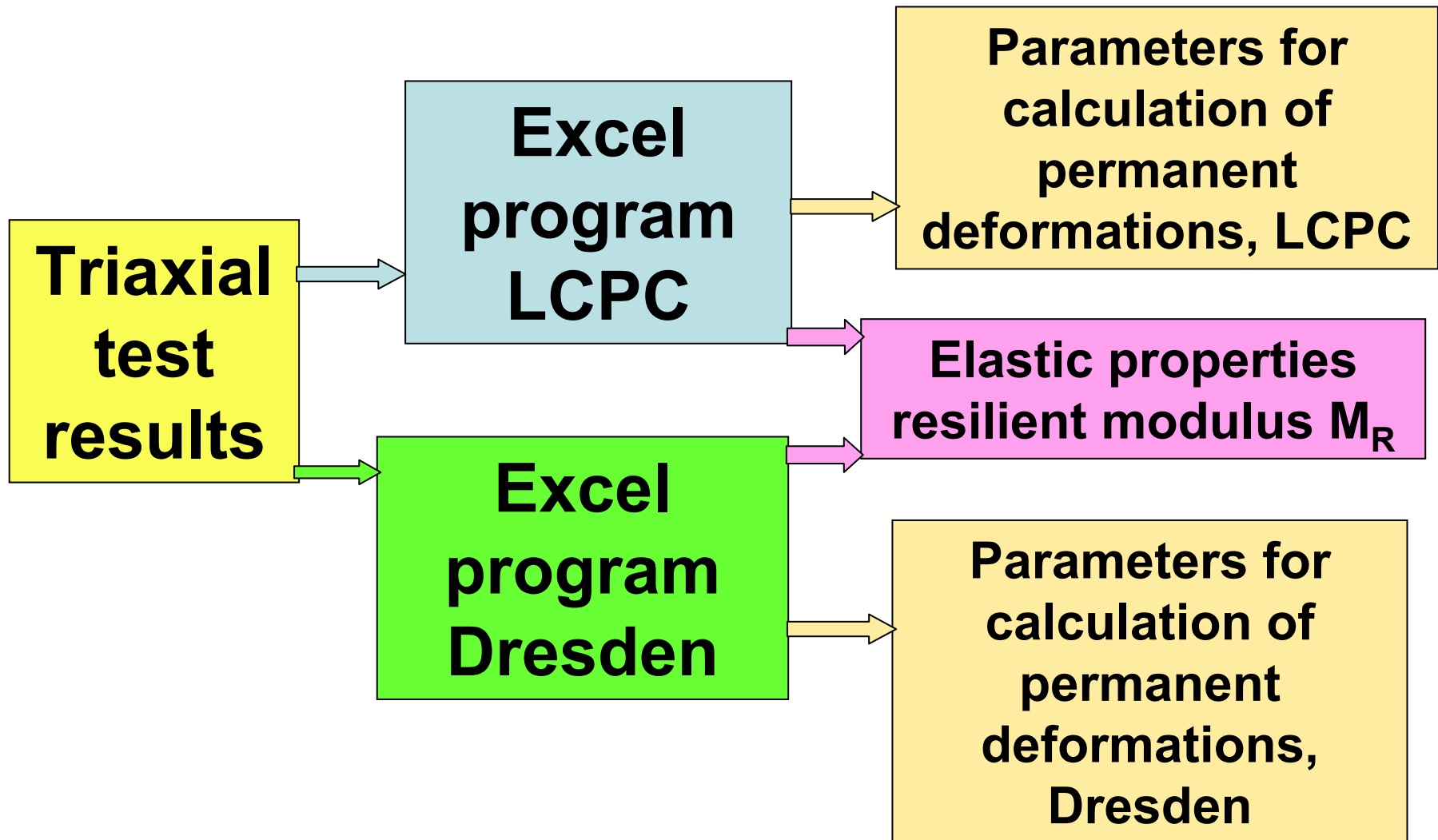
Asphalt material

Site tests



Unbound material

Evaluation of triaxial tests



Calculate future rutting with VagFEM

Parameters for
calculation of permanent
deformations, LCPC

Parameters for
calculation of permanent
deformations, Dresden

Parameters for calculation
of permanent deformations,
Design guide, unbound mtrl

Parameters for calculation
of permanent deformations,
Design guide, asphalt mtrl

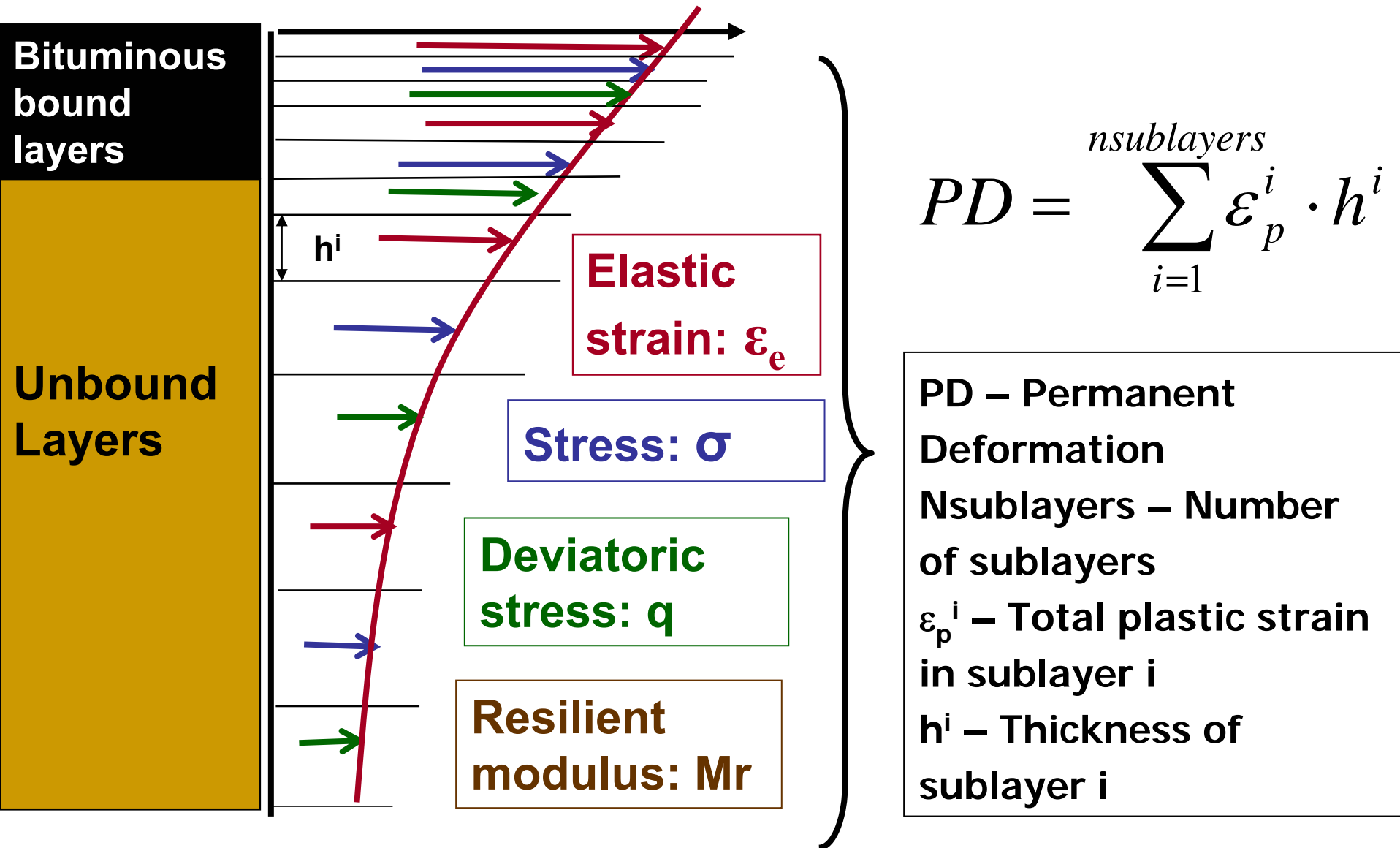
Elastic response, resilient
modulus, as digital output
data from VagFEM

**Excel programs for
calculation of
future rutting**

$$\epsilon_1^p(N) = \epsilon_{10}^p \cdot \left[1 - \left(\frac{N}{N_0} \right)^{-B} \right] \cdot \left[\frac{L_{\max}}{p_a} \right]^n \cdot \frac{1}{\left(m + \frac{s}{p_{\max}} - \frac{q_{\max}}{p_{\max}} \right)}$$

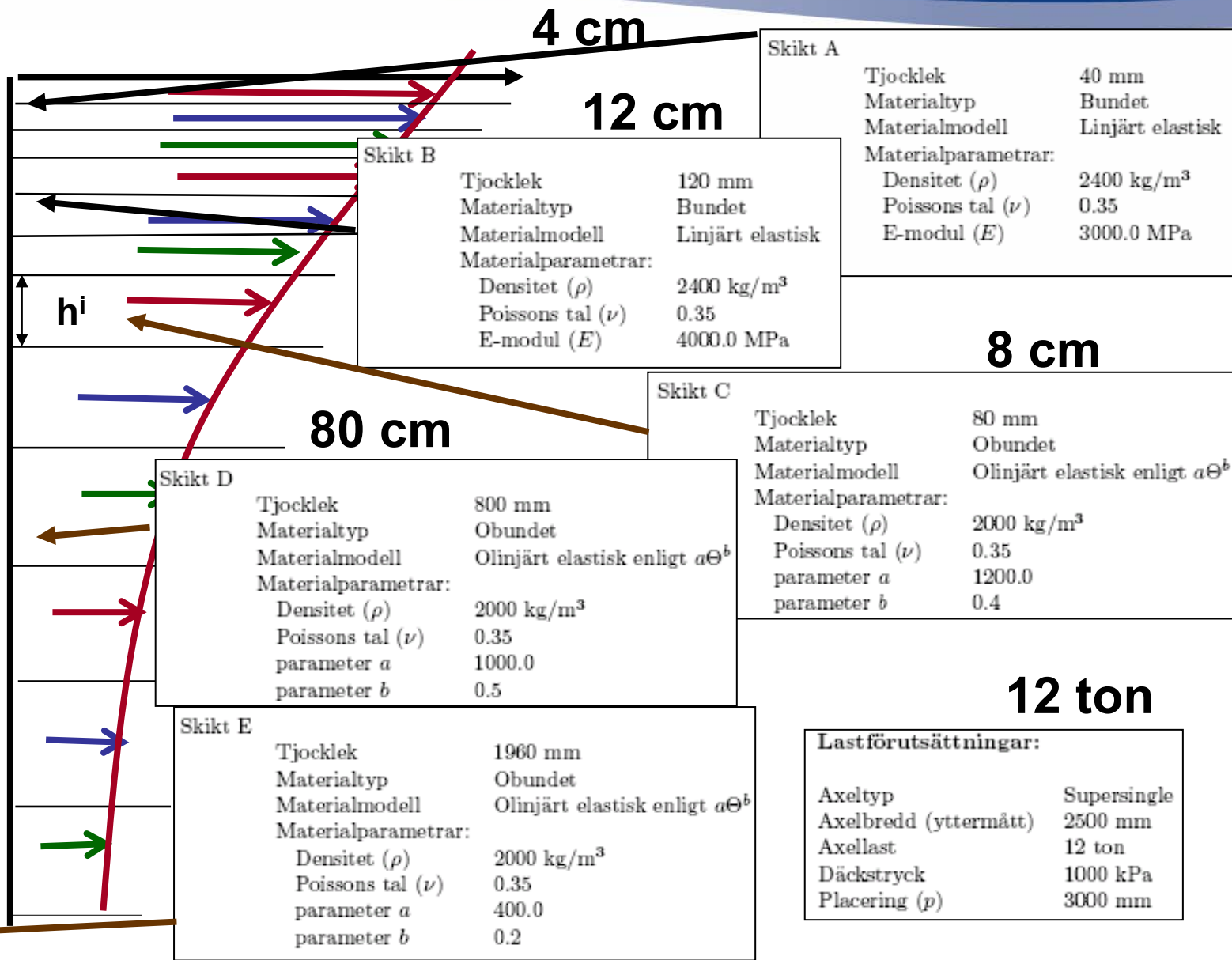
$$\frac{\epsilon_p}{\epsilon_r} = a_1 \cdot N^{a_2} \cdot T^{a_3}$$

$$\epsilon_p(N) = A \cdot \left(\frac{N}{1000} \right)^B + C \left(e^{D \frac{N}{1000}} - 1 \right)$$



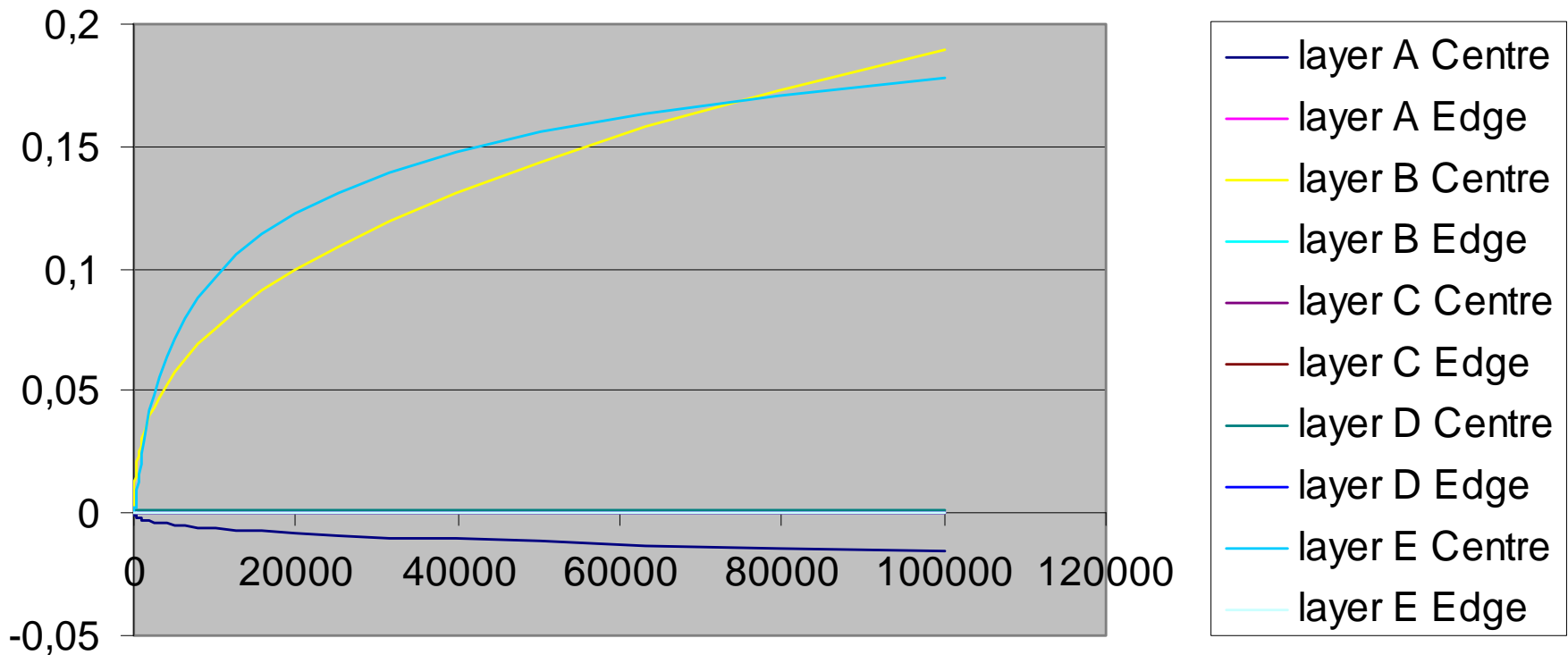
Bituminous bound layers

Unbound Layers



Results from VagFEM

Permanent deformation v.s. number of load repetitions.



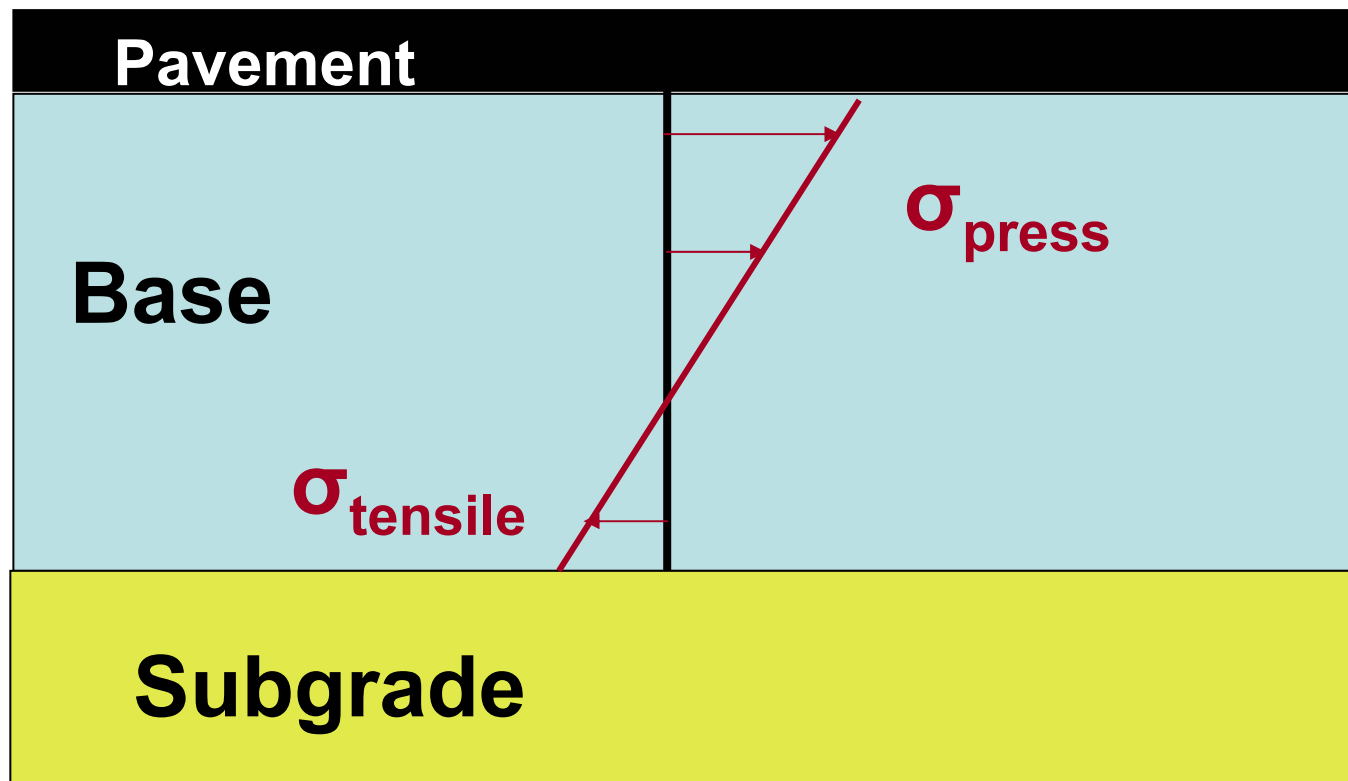
**So, why do we not use
this knowledge, test
methods and models?**

Future development

NordFoU

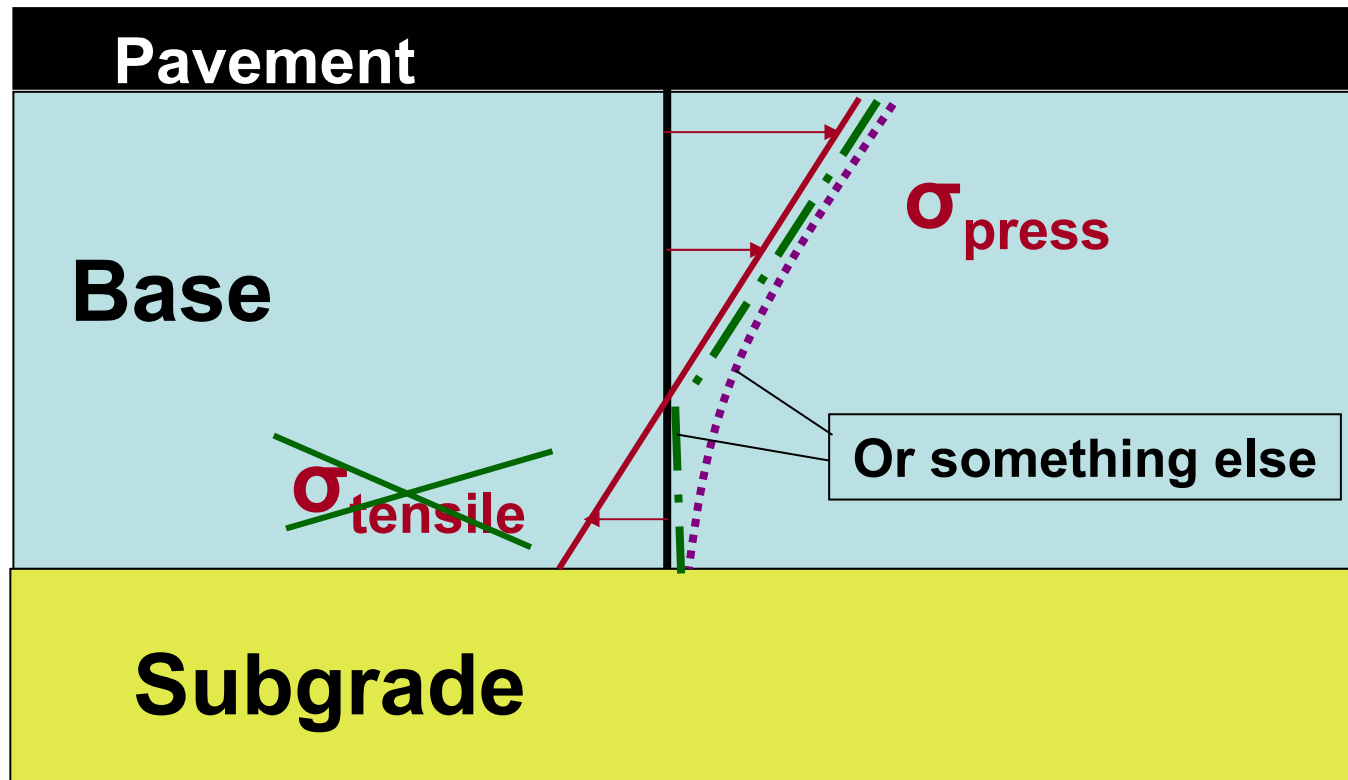
Sweden, Norway, Denmark and Island

Tensile stress in the bottom of unbound layers?

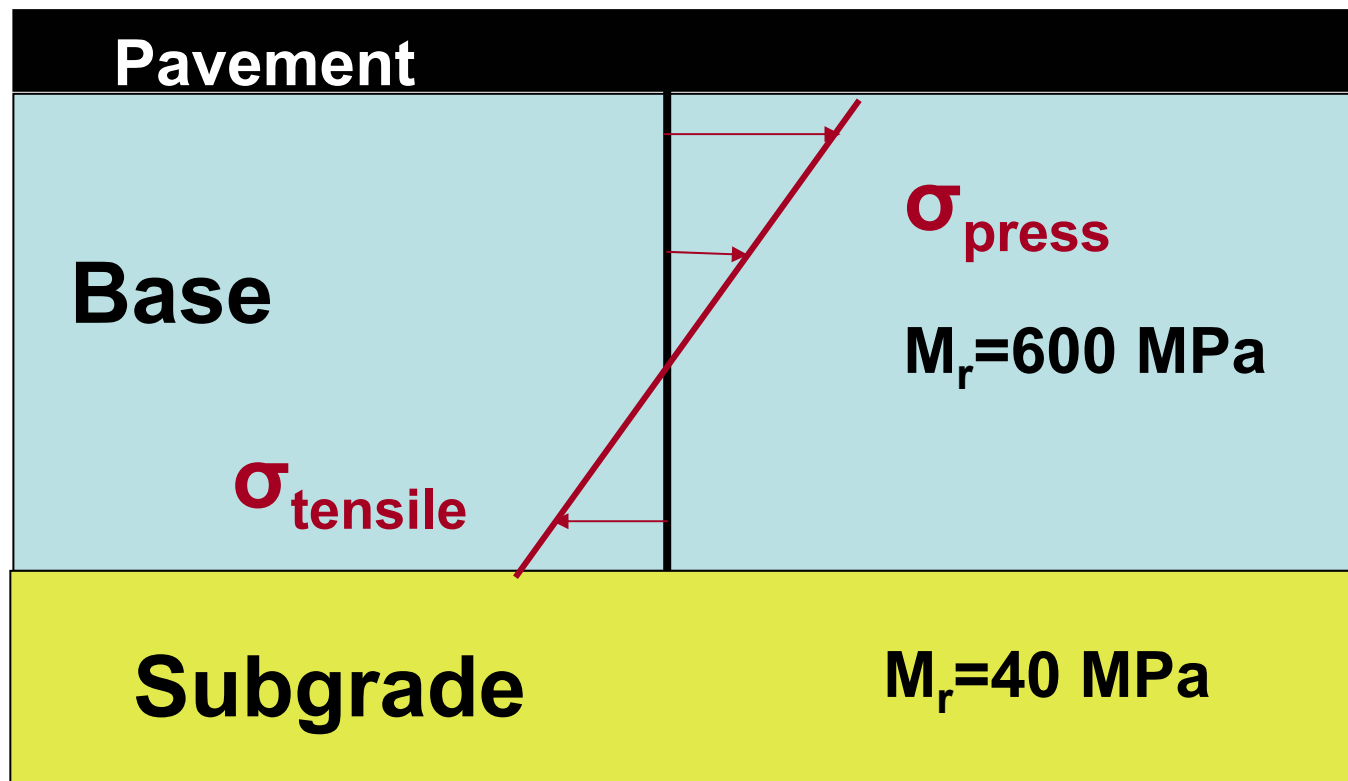


Tensile stress in the bottom of unbound layers?

Which is the real stress distribution?

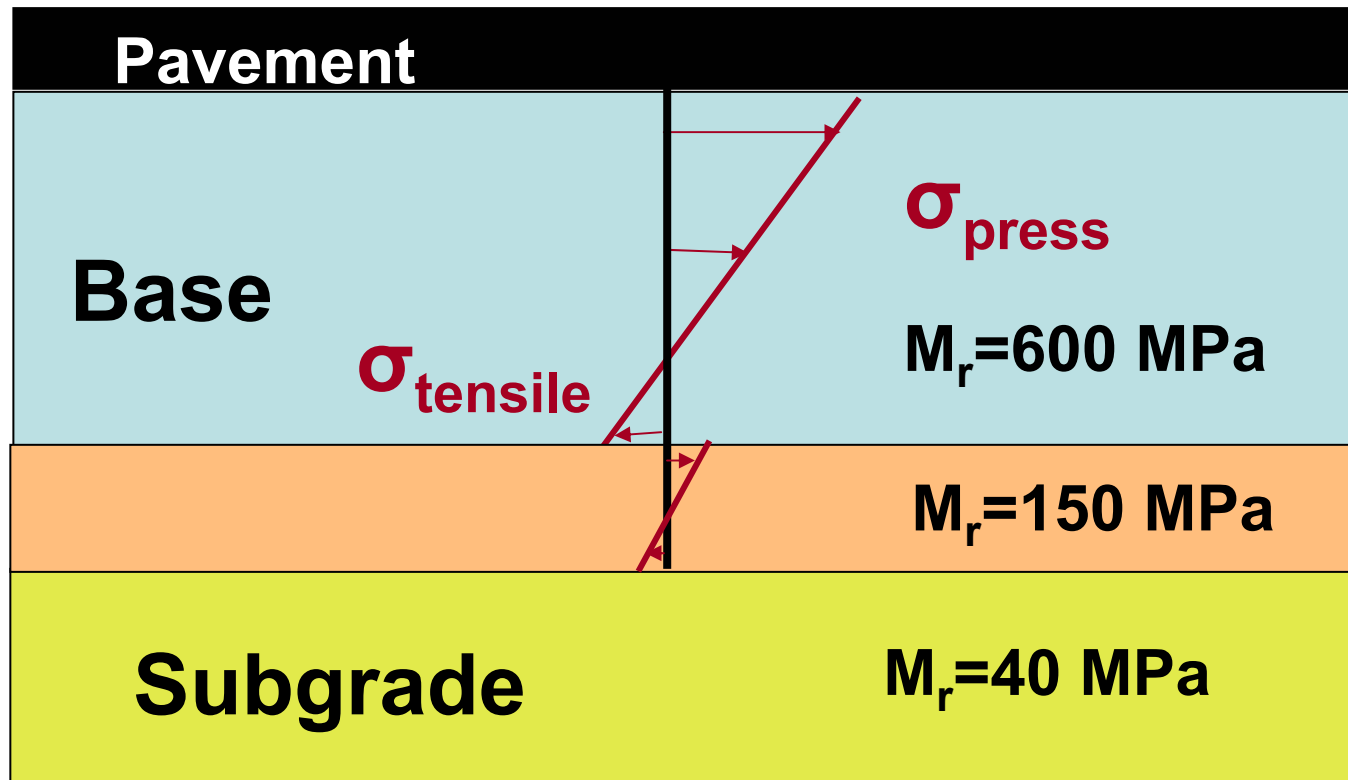


Unbound layers with large difference in resilient modulus?

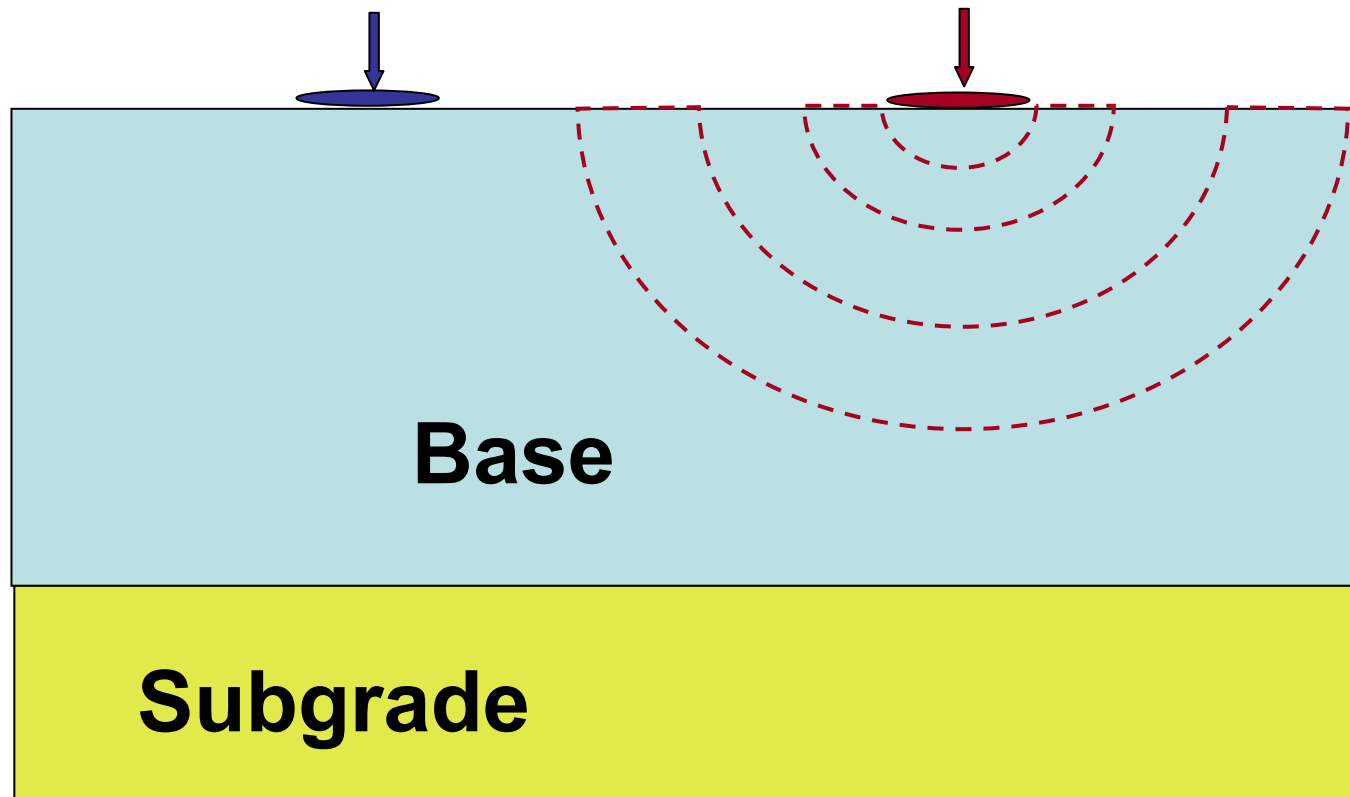


Unbound layers with large difference in resilient modulus?

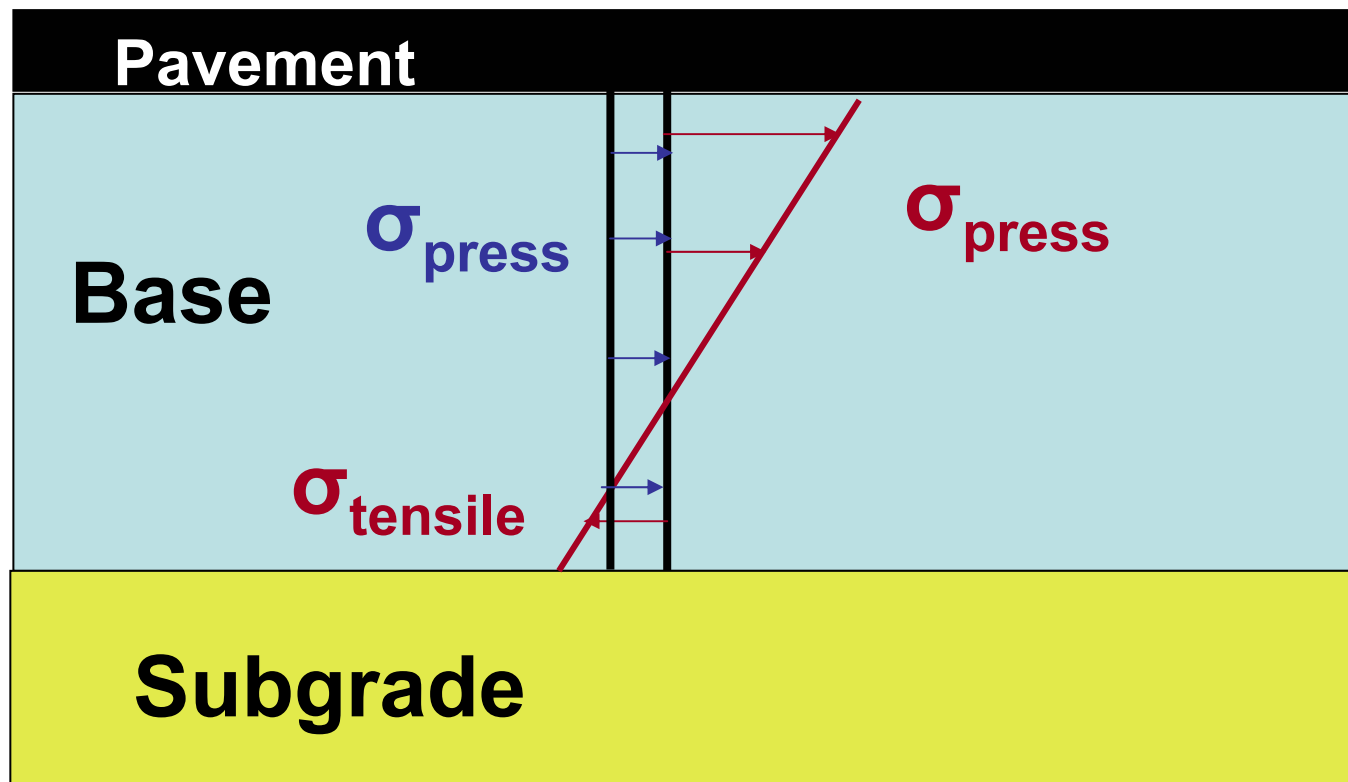
Old experience: Insert a layer with medium resilient modulus!



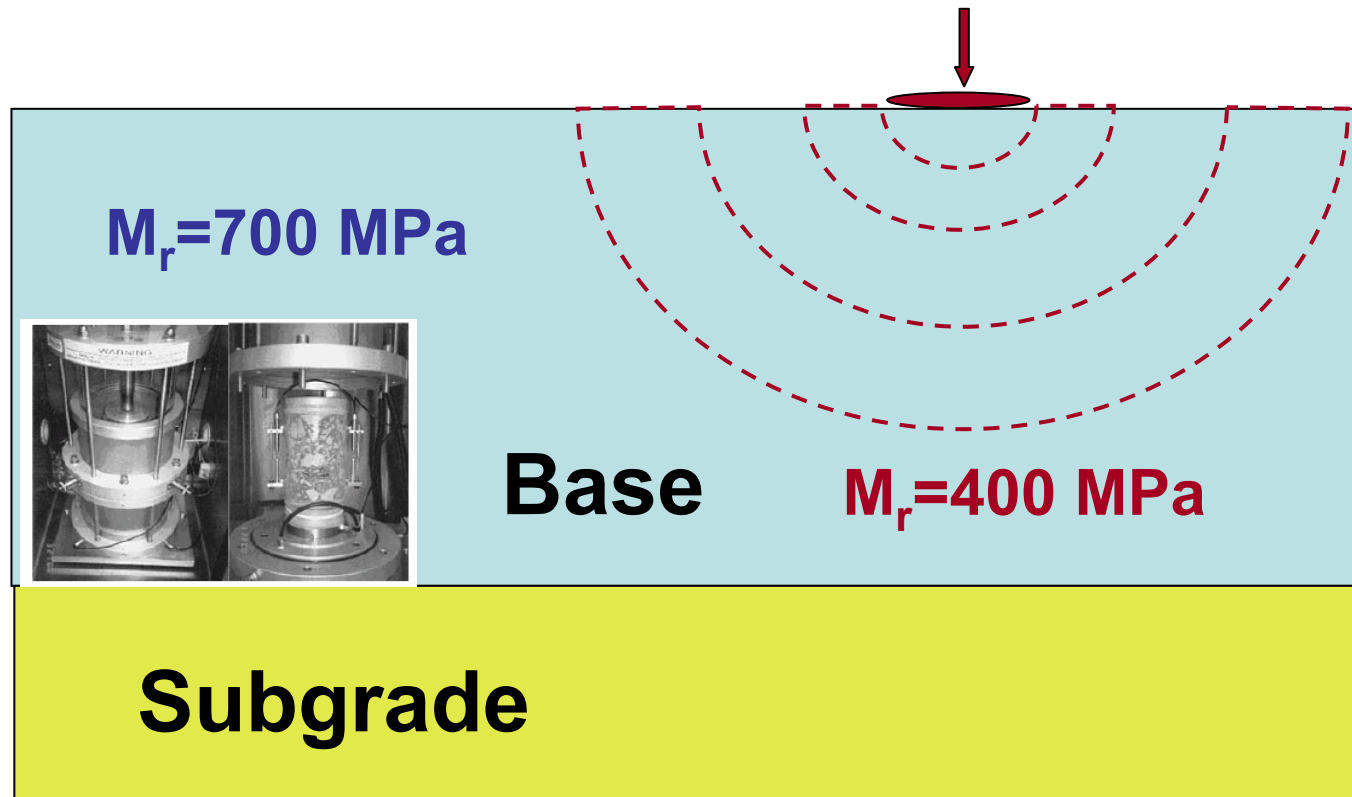
Difference/connection between static and dynamic resilient modulus?



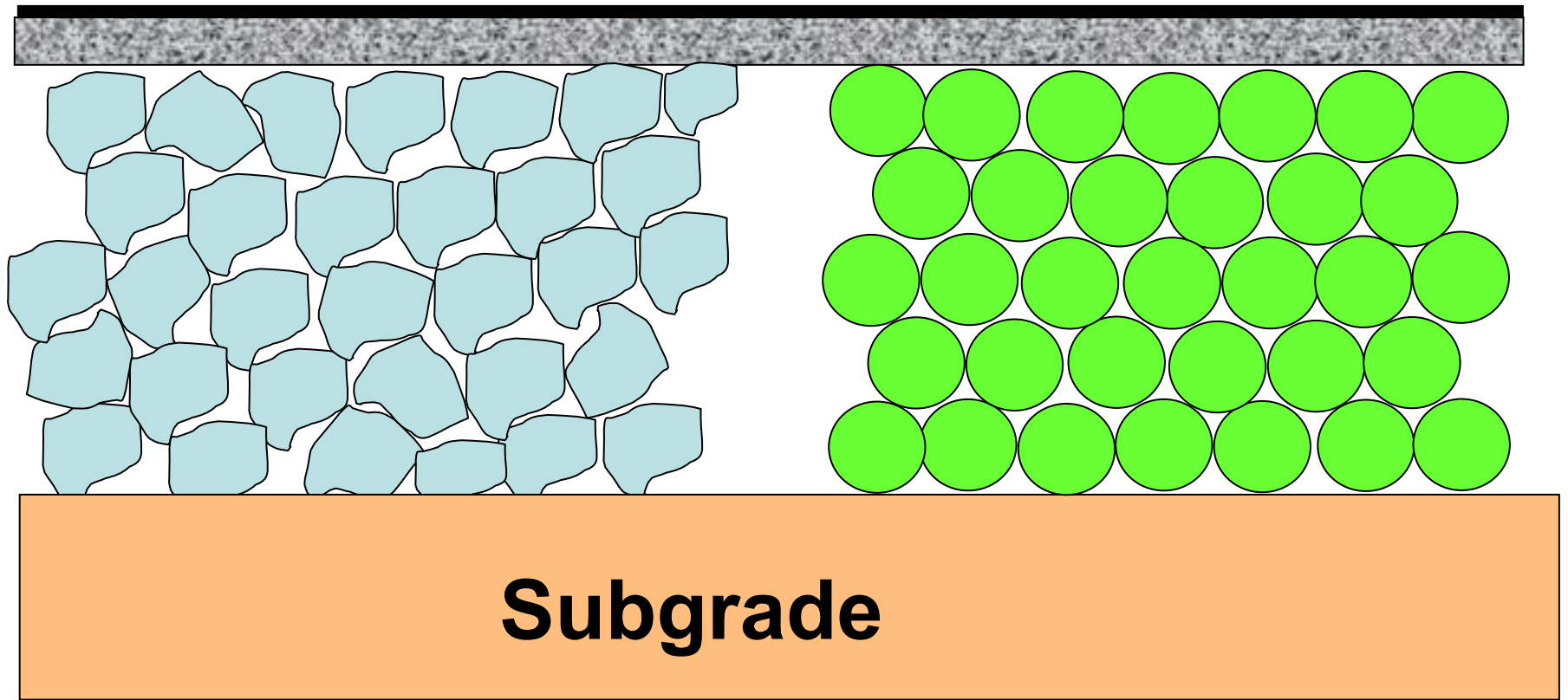
Horizontal stress depending on compaction and traffic ?



Difference/connection between resilient modulus measured with triaxial test and on site with plate loading etc.?



Material models different for crushed and uncrushed material?



Why does high plate loading values give small rutting?

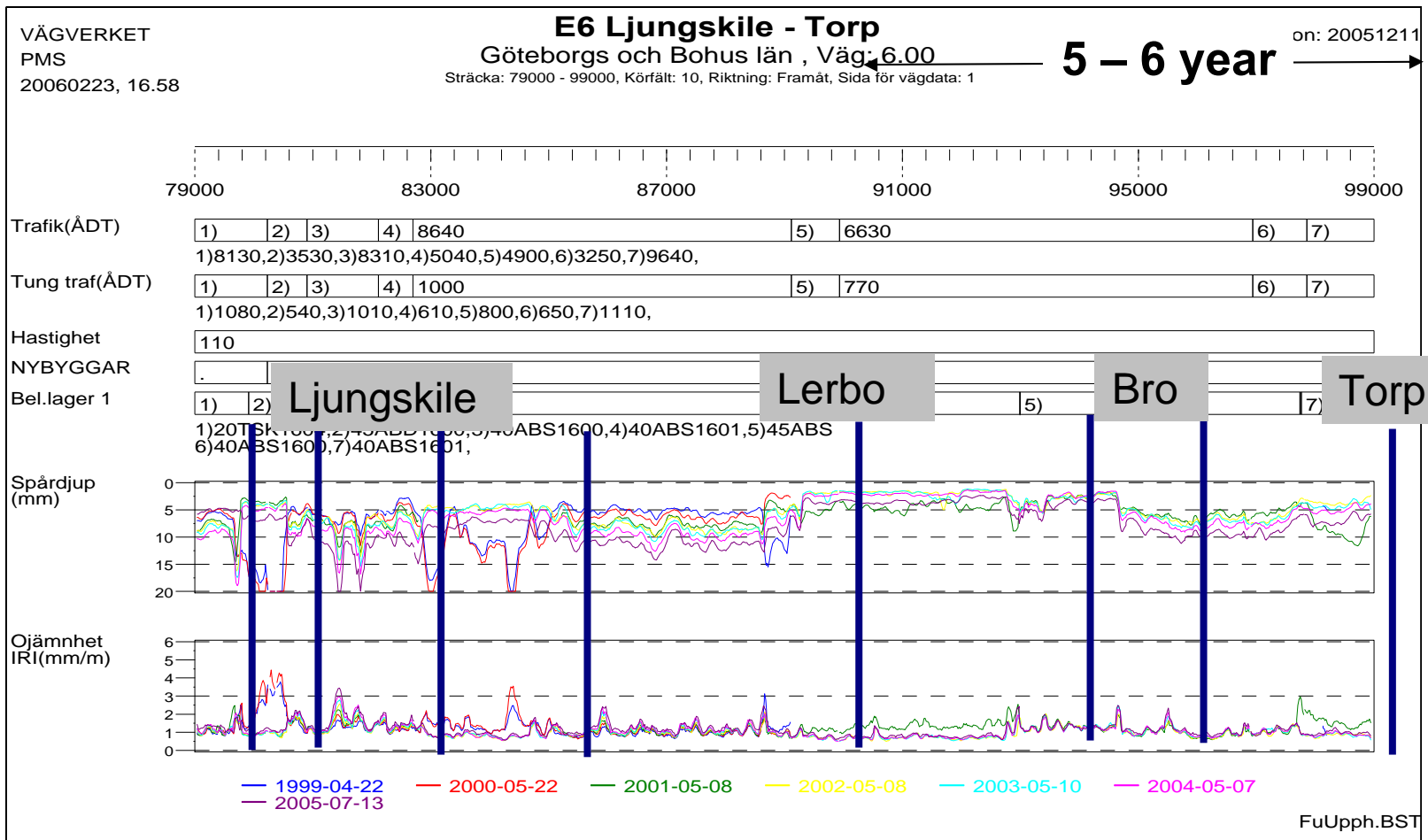


Plate loading: **ca 90 MPa** **250 – 500 MPa** **ca 150 MPa**

Adjust the compactors vibrators for compaction on a certain depth

**Possible to
measure response
in different levels**



Vertical or/and horizontal vibrations with different amplitude and frequency

Base layer

Connection between aggregate characteristics etc. and permanent rutting?

- **Grain maximum size**
- **Aggregate gradation**
- **Rock material, Geology**
- **Moisture content**

M_R Model Including Moisture and Density

Moisture? **Pore volume?**

$$M_R = F_{moisture} \cdot F_{density} \cdot k_1 \cdot p_a \cdot \left(\frac{\theta}{p_a} \right)^{k_2} \cdot \left(\frac{\tau_{oct}}{p_a} + 1 \right)^{k_3}$$

$$F_{moisture} = a + \frac{b - a}{1 + \text{EXP} \left(\ln_e \left(\frac{-b}{a} \right) + k_s \cdot (S - S_{opt}) \right)}$$

Is it possible
to simplify:
k₃ = - 0.2

$$F_{density} = \left(\frac{\gamma_d}{\gamma_{d \max}} \right)^{k_\gamma}$$

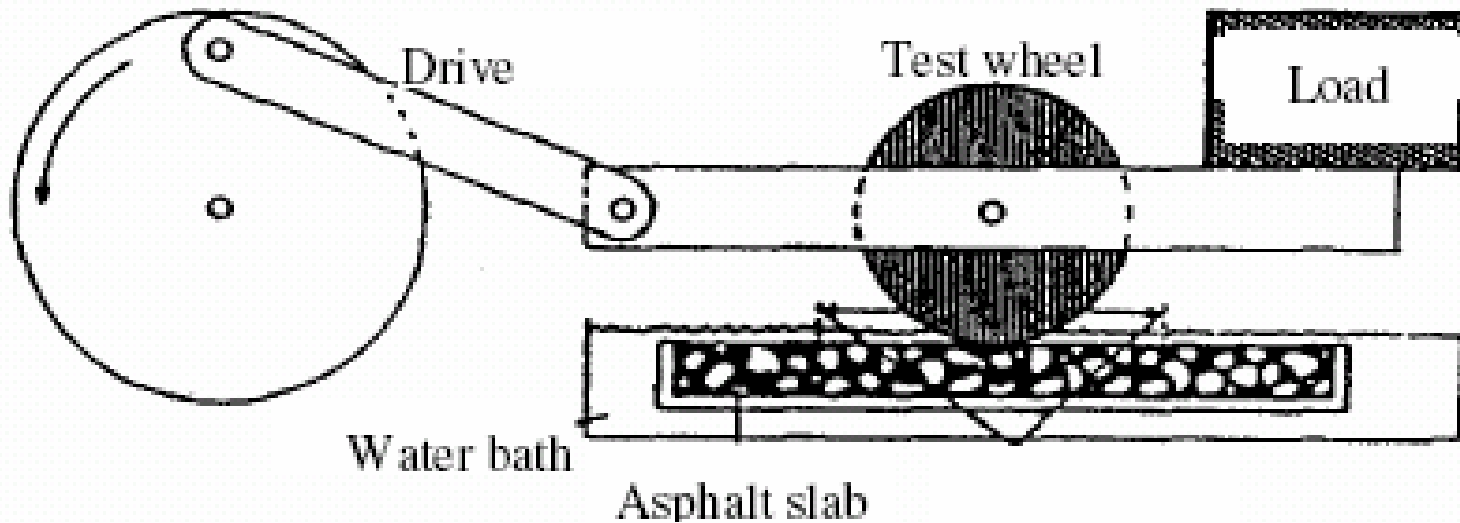
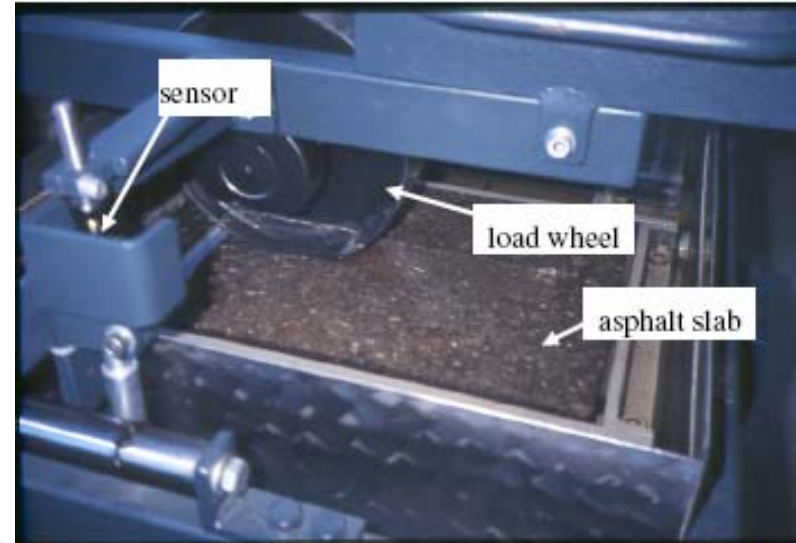
Where: S = degree of saturation

γ_d = dry unit weight

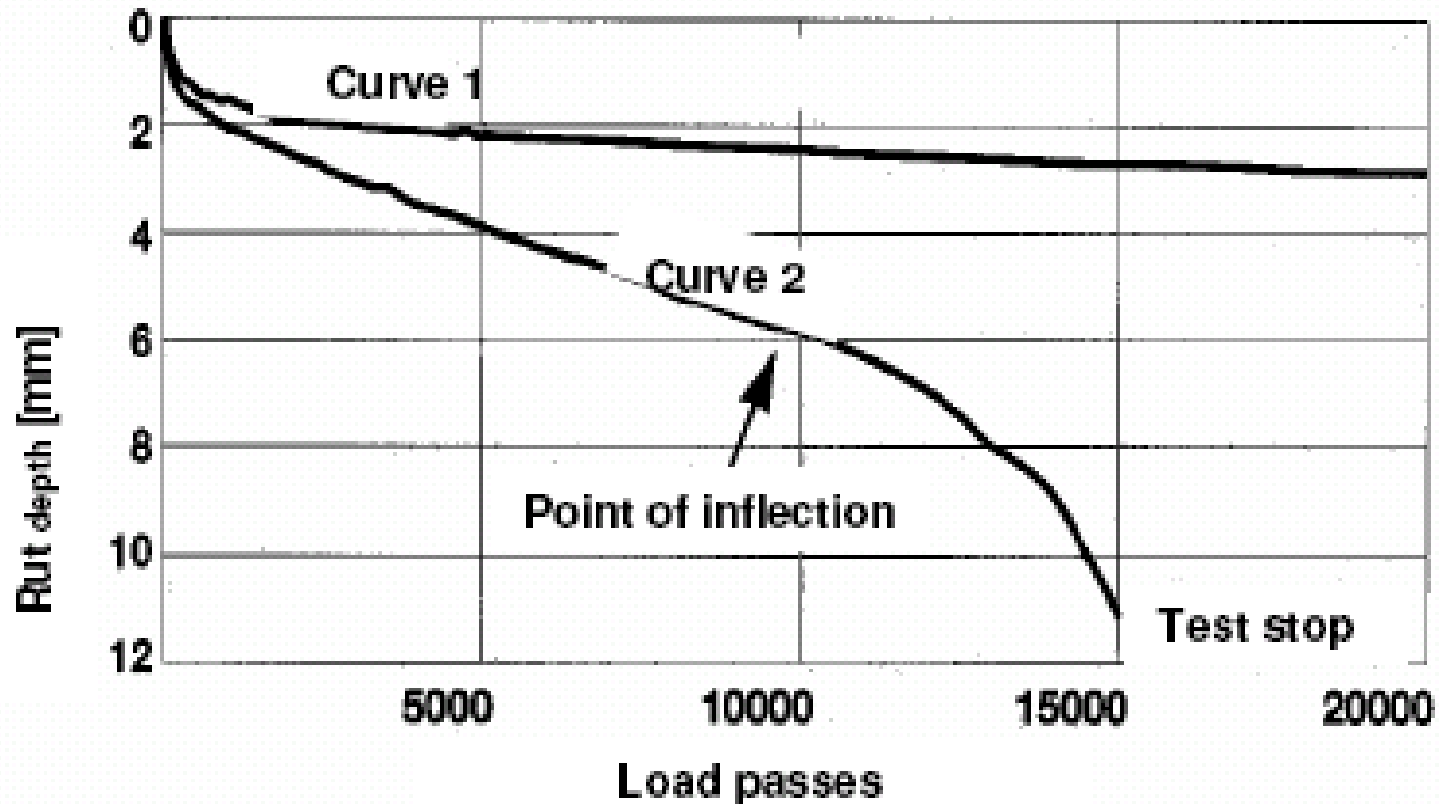
k_s, k_γ = regression constants

a, b = constants (function of soil type)

Wheel Tracking Test



Wheel tracking; Result



Is it possible to backcalculate parameters from Wheel track tests in order to get parameters for calculation of permanent deformations in asphalt?

Effect of stabilisation



MATERIAL MODELS

Rutting in bituminous bound materials

SAMARIS

***THANK YOU FOR
YOUR ATTENTION***

Anders Huvstig

Swedish Road Administration (SRA)